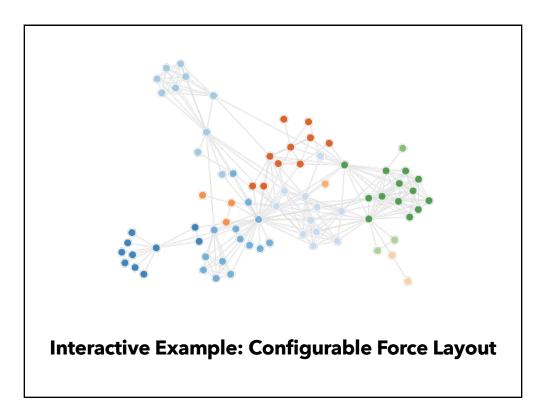
Network Analysis

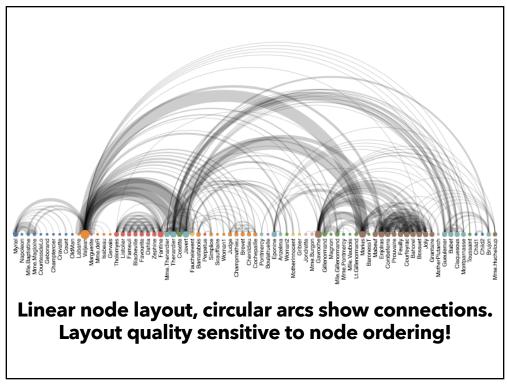
Maneesh Agrawala

CS 448B: Visualization
Winter 2020

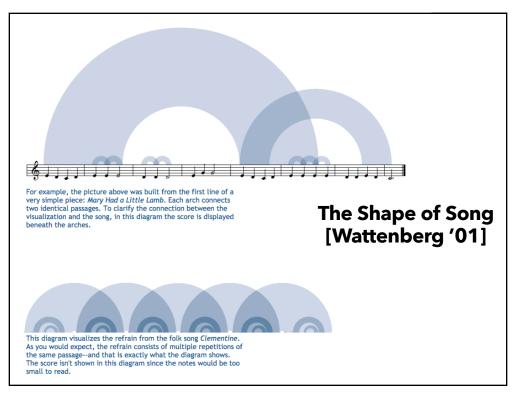
1

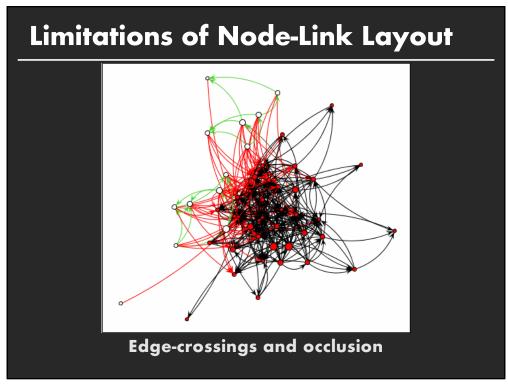
Last Time: Network Layout

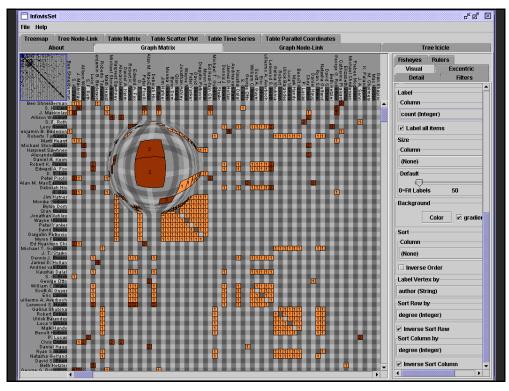


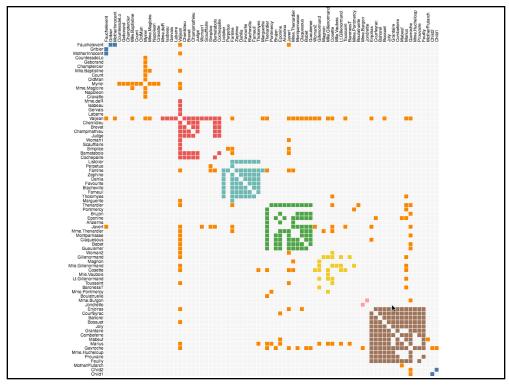


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Seriation/Ordination Permutation

Goal: Ensure similar items placed near each other. E.g., minimize sum of distances of adjacent items.

Requires combinatorial optimization: NP-Hard!

Instead, approximate / heuristic approaches used:

Perform hierarchical clustering, sort cluster tree Apply approximate traveling salesperson solver

Seriation initially used in <u>archaeology</u> for relative dating of artifacts based on observed properties

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Attribute-Driven Layout

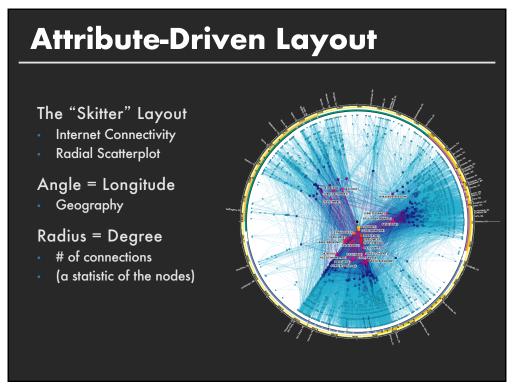
Large node-link diagrams get messy!

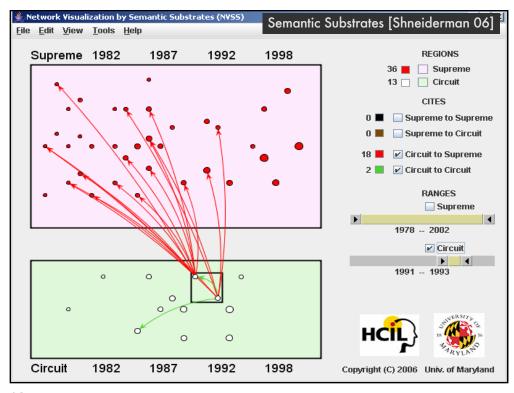
Is there additional structure we can exploit?

Idea: Use data attributes to perform layout

e.g., scatter plot based on node values

Dynamic queries and/or brushing can be used to explore connectivity





Summary



Tree Layout

Indented / Node-Link / Enclosure / Layers How to address issues of scale?

■ Filtering and Focus + Context techniques

Graph Layout

Tree layout over spanning tree Hierarchical "Sugiyama" Layout Optimization (Force-Directed Layout) Attribute-Driven Layout

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Announcements

Final project

New visualization research or data analysis project

- **Research**: Pose problem, Implement creative solution
- Data analysis: Analyze dataset in depth & make a visual explainer

Deliverables

- **Research**: Implementation of solution
- Data analysis/explainer: Article with multiple interactive visualizations
- 6-8 page paper

Schedule

- Project proposal: Wed 2/19
- Design review and feedback: 3/9 and 3/11
- Final presentation: 3/16 (7-9pm) Location: TBD
- Final code and writeup: 3/18 11:59pm

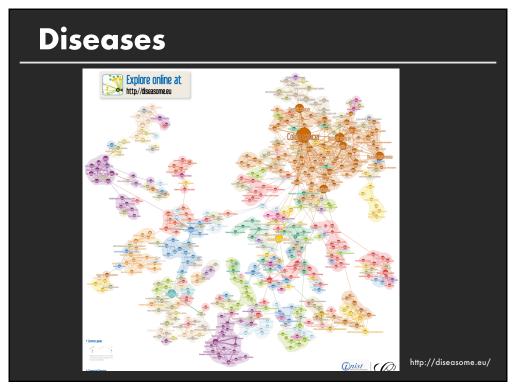
Grading

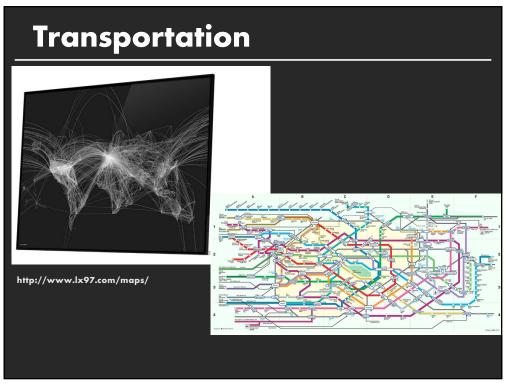
- Groups of up to 3 people, graded individually
- Clearly report responsibilities of each member

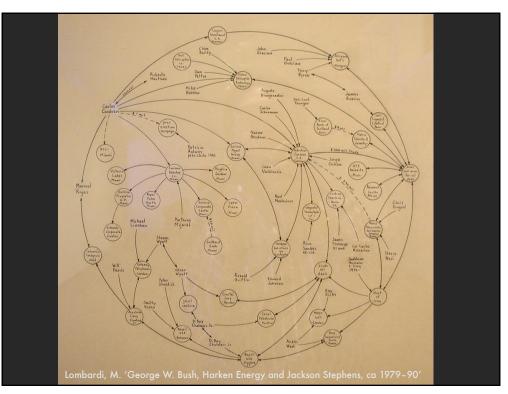
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Network Analysis

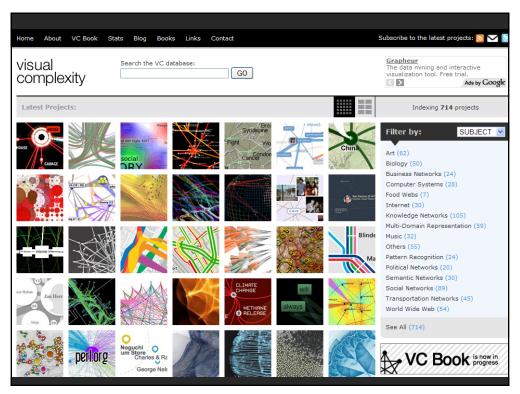
*Slides adapted from E. Adar's / L. Adamic's Network Theory and Applications course slides.

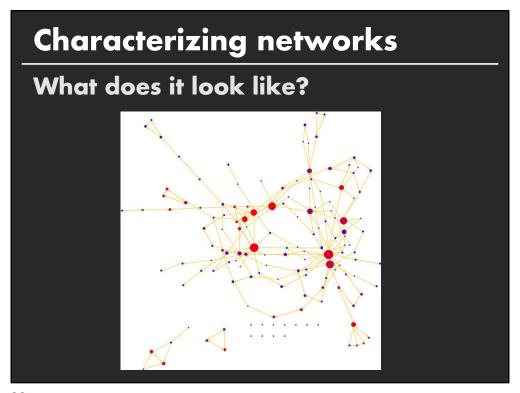


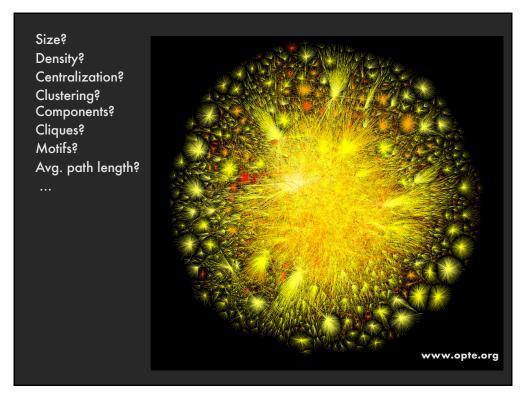








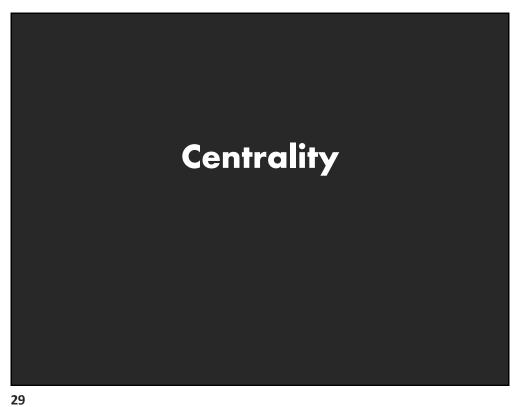


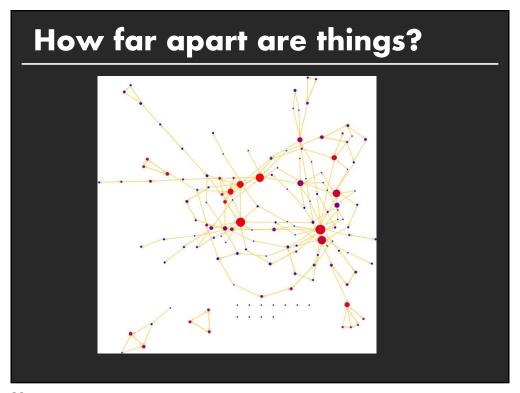


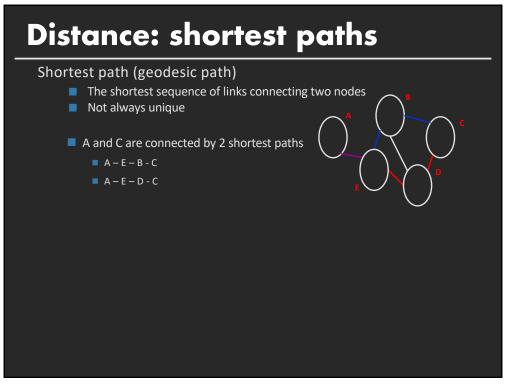
Topics

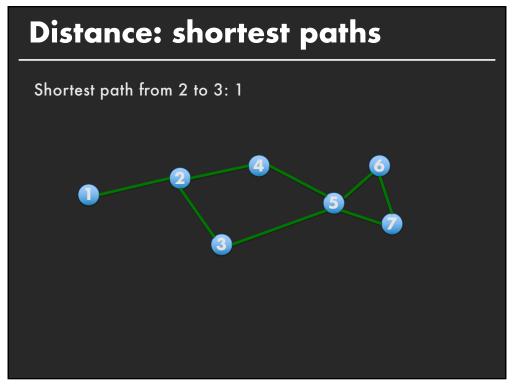
Network Analysis

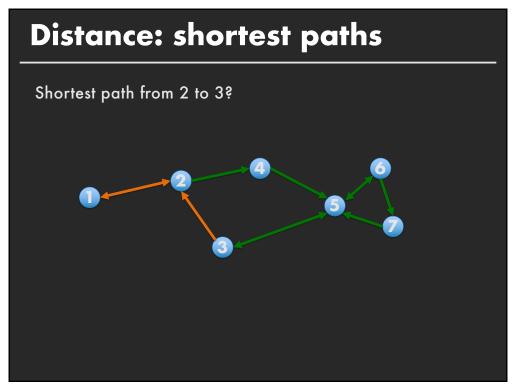
- Centrality / centralization
- Community structure Pattern identification
- Models

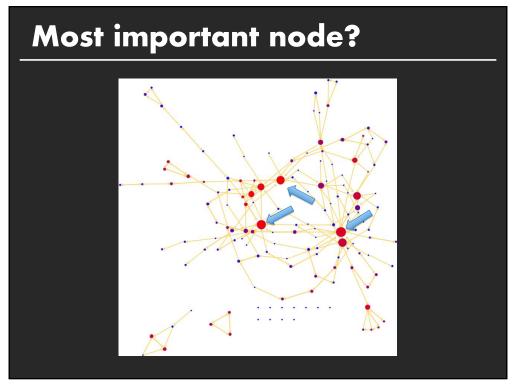


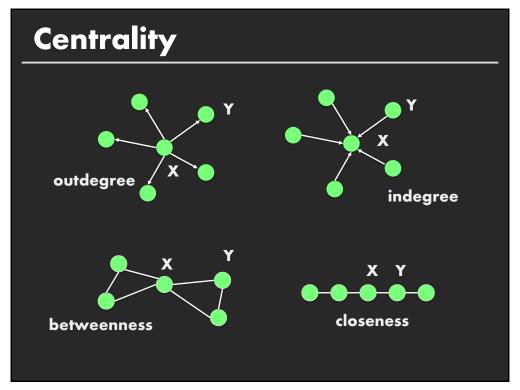


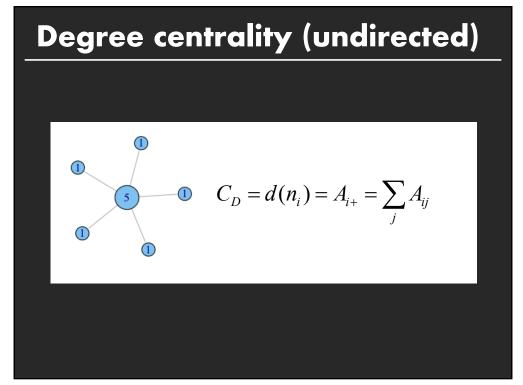




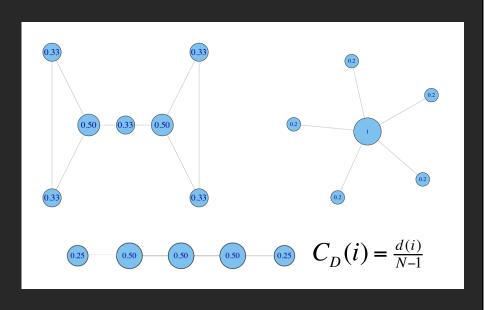








Normalized degree centrality



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When is degree not sufficient?

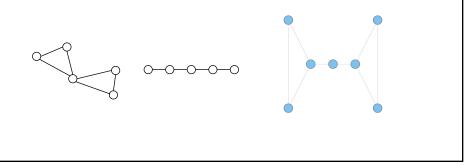
Does not capture

Ability to broker between groups

Likelihood that information originating anywhere in the network reaches you

Betweenness

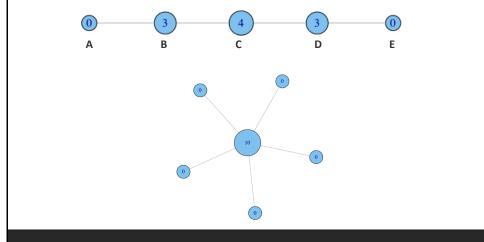
Assuming nodes communicate using the most direct (shortest) route, how many pairs of nodes have to pass information through target node?



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Betweenness - examples

non-normalized:



Betweenness: definition

$$C_B(i) = \sum_{j,k \neq i,j < k} g_{jk}(i) / g_{jk}$$

 g_{jk} = the number of paths connecting jk $g_{jk}(i)$ = the number that node i is on.

Normalization:

$$C_B(i) = C_B(i)/[(n-1)(n-2)/2]$$

number of pairs of vertices excluding the vertex itself

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When are C_d, C_b not sufficient?

Do not capture

Likelihood that information originating anywhere in the network reaches you

Closeness: definition

Being close to the center of the graph

Closeness Centrality:

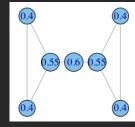
$$C_c(i) = \left[\sum_{j=1, j\neq i}^{N} d(i, j)\right]^{-1}$$

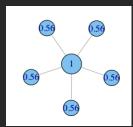
Normalized Closeness Centrality

$$C_C'(i) = (C_C(i))/(N-1) = \frac{N-1}{\sum_{j=1, j \neq i}^{N} d(i, j)}$$

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Examples - closeness





Centrality in directed networks

Prestige ~ indegree centrality

Betweenness ~ consider directed shortest paths

Closeness ~ consider nodes from which target node can be reached

Influence range ~ nodes reachable from target node

Straight-forward modifications to equations for non-directed graphs





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Characterizing nodes

	Low Degree	Low Closeness	Low Betweenness
High Degree		Node embedded in cluster that is far from the rest of the network	Node's connections are redundant - communication bypasses him/her
High Closeness	Node links to a small number of important/active other nodes.		Many paths likely to be in network; node is near many people, but so are many others
High Betweenness	Node's few ties are crucial for network flow	Rare. Node monopolizes the ties from a small number of people to many others.	

Centralization – how equal

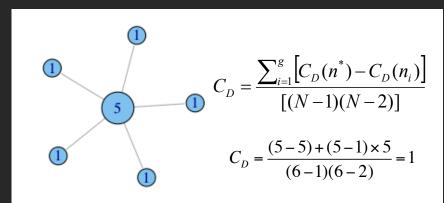
Variation in the centrality scores among the nodes

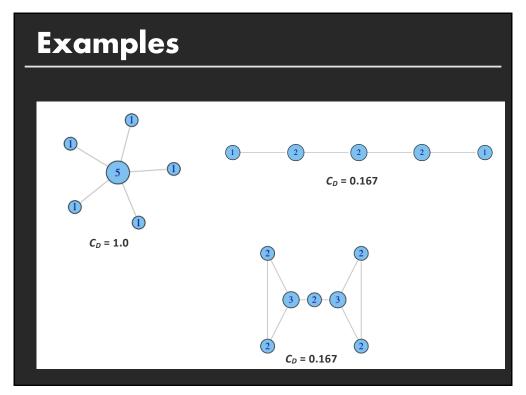
Freeman's general formula for centralization:

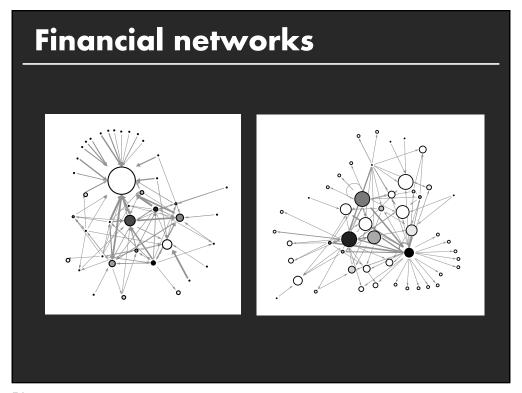
$$C_D = \frac{\sum_{i=1}^g \left[C_D(n^*) - C_D(i) \right]}{\left[(N-1)(N-2) \right]}$$

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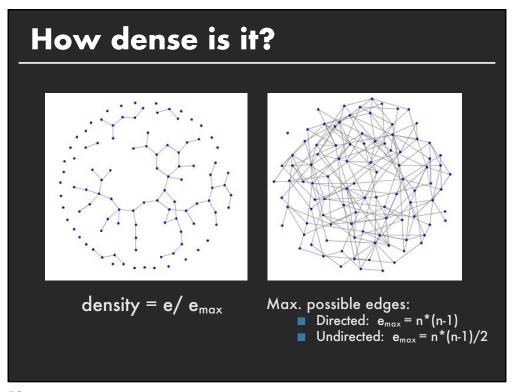
Examples

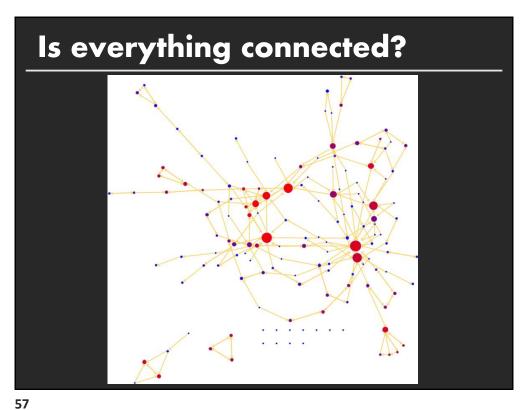




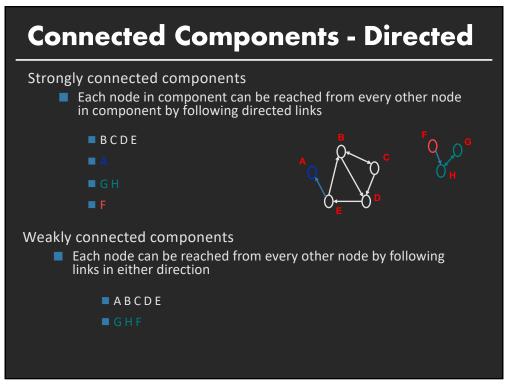


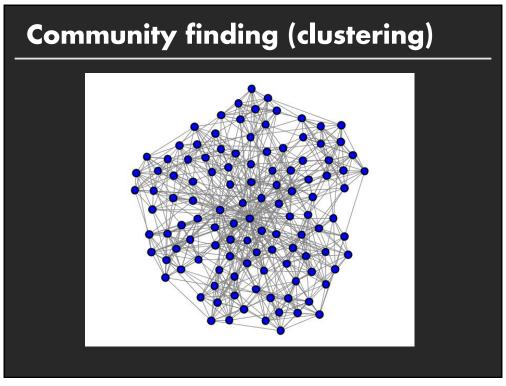






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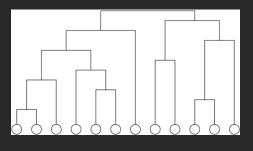


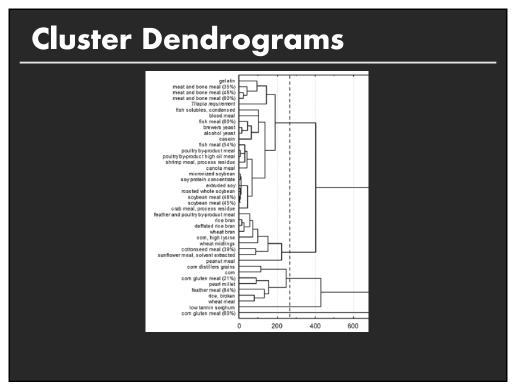


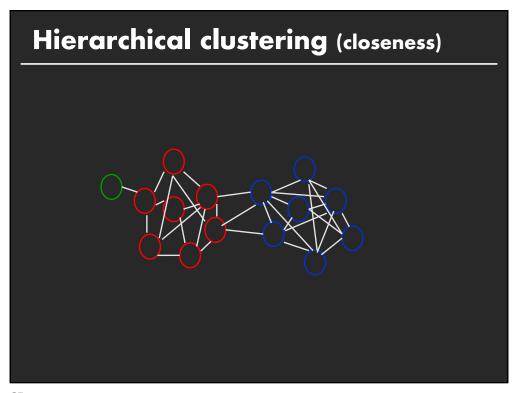
Hierarchical clustering

Process:

- Calculate affinity weights W for all pairs of vertices
- Start: N disconnected vertices
- Adding edges (one by one) between pairs of clusters in order of decreasing weight (use closest distance to compare clusters)
- Result: nested components



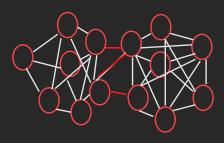




Betweenness clustering

Girvan and Newman 2002 iterative algorithm:

- Compute C_b of all edges
- Remove edge i where $C_b(i) == max(C_b)$
- Recalculate betweenness



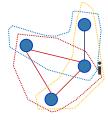
66

Clustering coefficient



Local clustering coefficient:

 $C_i = \frac{\text{number of closed triplets centered on i}}{\text{number of connected triplets centered on i}}$

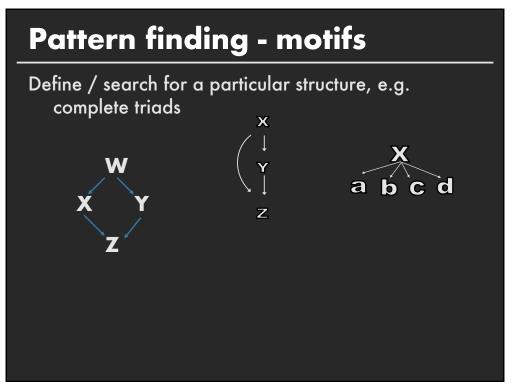


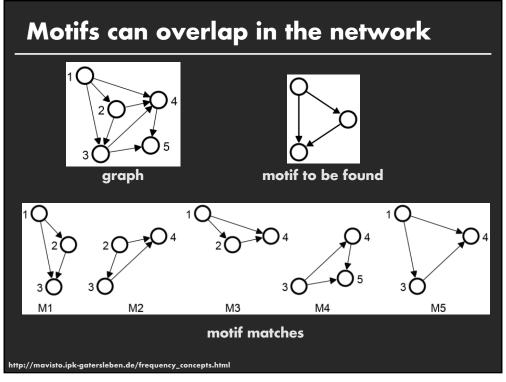
Global clustering coefficient:

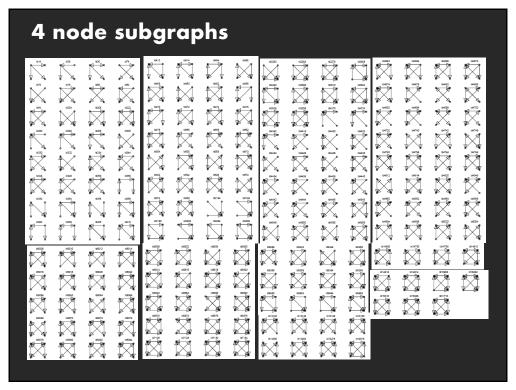
$$C_i = 1/3 = 0.33$$

 $C_G = \frac{3* \text{ number of closed triplets}}{\text{number of connected triplets}}$

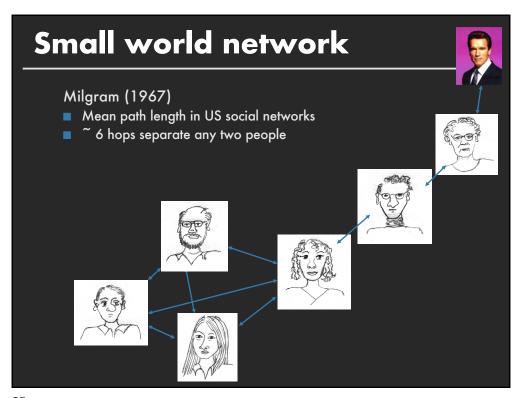
$$C_G = 3*1/5 = 0.6$$

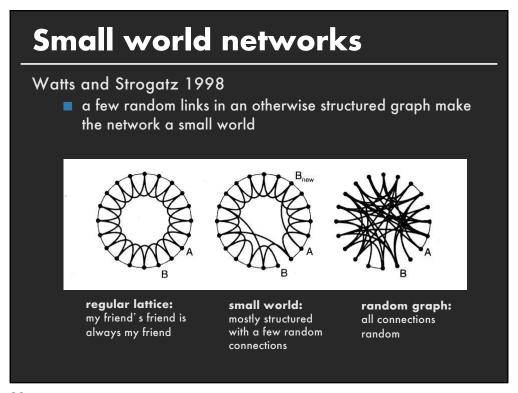






Simulating network models

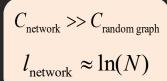




Defining small world phenomenon

Pattern:

- high clustering
- low mean shortest path



Examples

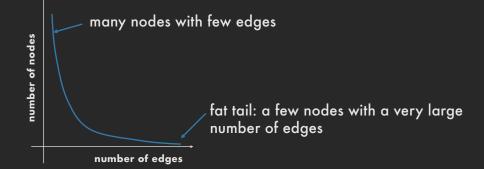
- neural network of C. elegans,
- semantic networks of languages,
- actor collaboration graph
- food webs

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Power law networks

Many real world networks contain hubs: highly connected nodes

Usually the distribution of edges is extremely skewed



Summary

Structural analysis

- Centrality
- Community structure
- Pattern finding
- → Widely applicable across domains