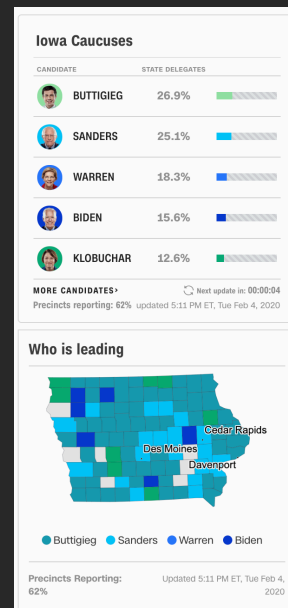
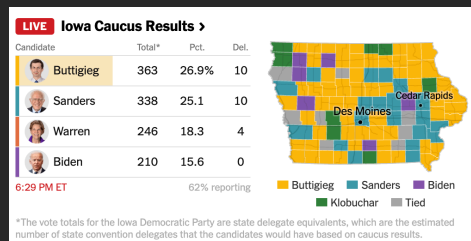


# Color

Maneesh Agrawala

CS 448B: Visualization  
Winter 2020

1



2

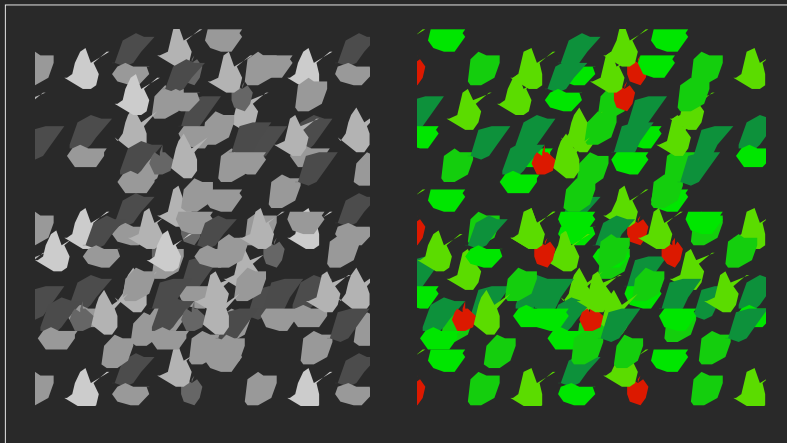
# Color

3

## Color in Visualization

---

Identify, Group, Layer, Highlight



Colin Ware

4

## **Purpose of Color**

---

**To label**

**To measure**

**To represent and imitate**

**To enliven and decorate**

*"Above all, do no harm."*

**- Edward Tufte**

5

## **Topics**

---

**Color Perception**

**Color Naming**

**Using Color in Visualization**

6

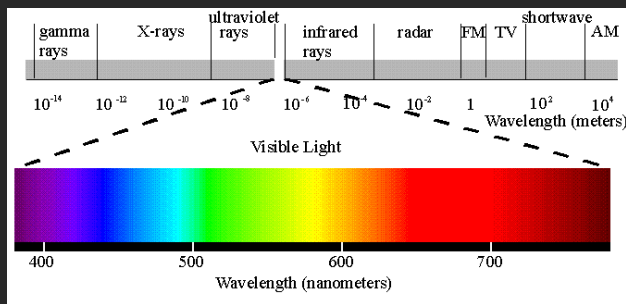
# Color Perception

Physical World, Visual System, Mental Models

7

## Physical World

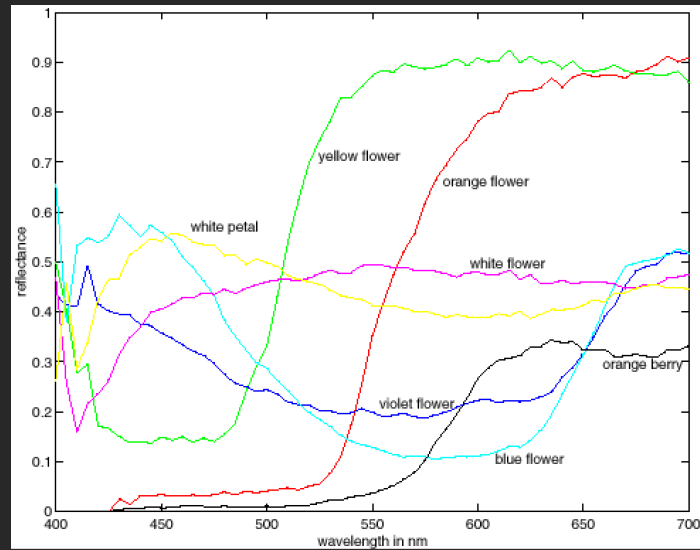
Light is radiation in range of wavelengths



Light of single wavelength is *monochromatic*

10

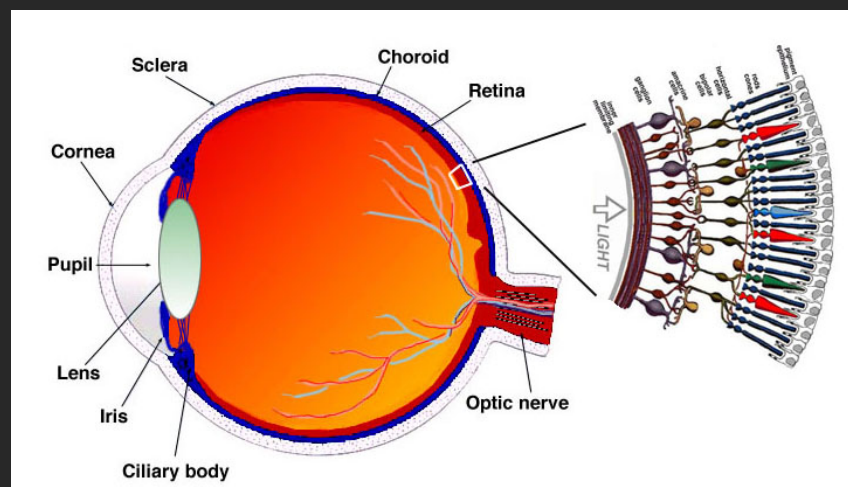
# Most Colors not Monochromatic



Curves describe spectral composition  $\Phi(\lambda)$  of stimulus

12

# Retina

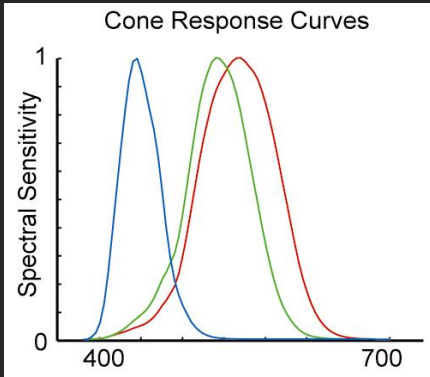


Simple Anatomy of the Retina, Helga Kolb

15

# As light enters our retina...

**LMS (Long, Middle, Short) Cones  
Sensitive to different wavelength**

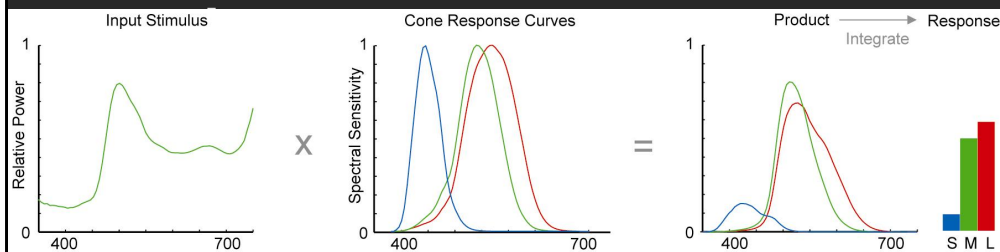


*A Field Guide to Digital Color, Maureen Stone*

18

# Cone Response

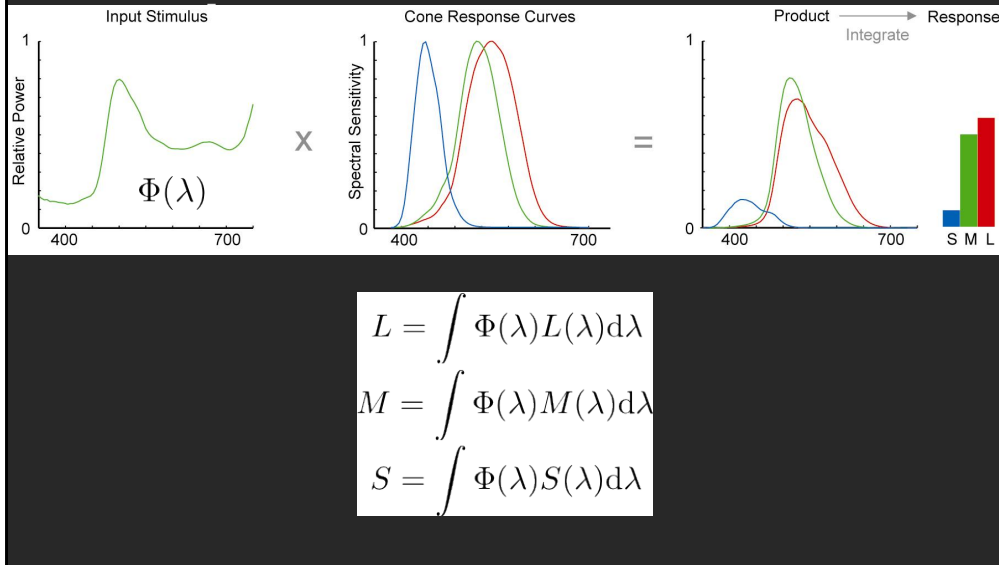
**Integrate cone response with input**



19

# Computing Cone Response

## Integrate cone response with input

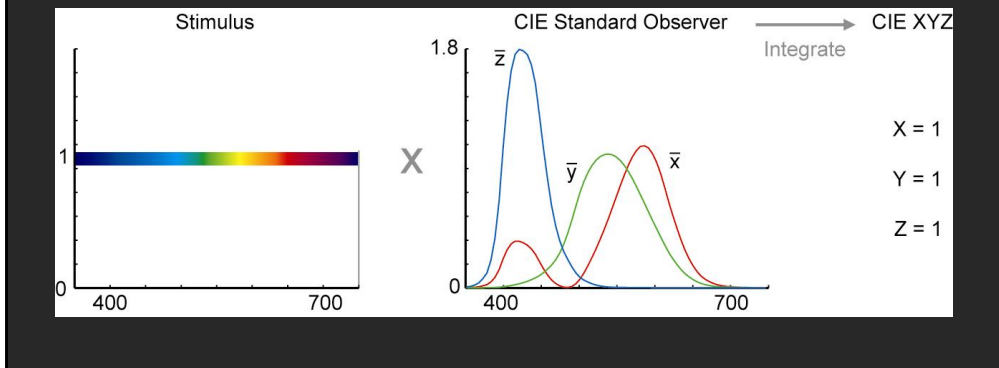


20

# CIE XYZ Color Space

Standardized in 1931 to mathematically represent tri-stimulus response

“Standard observer” response curves



22

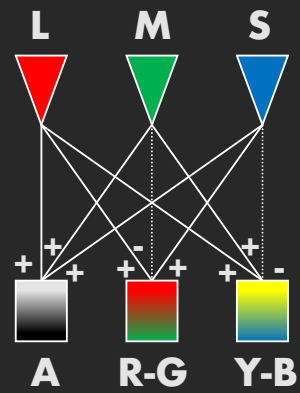
# Opponent processing

LMS are linearly combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



Fairchild

24

# Opponent processing

LMS are combined to create:

Lightness

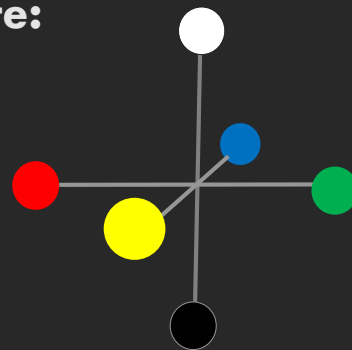
Red-green contrast

Yellow-blue contrast

Experiments:

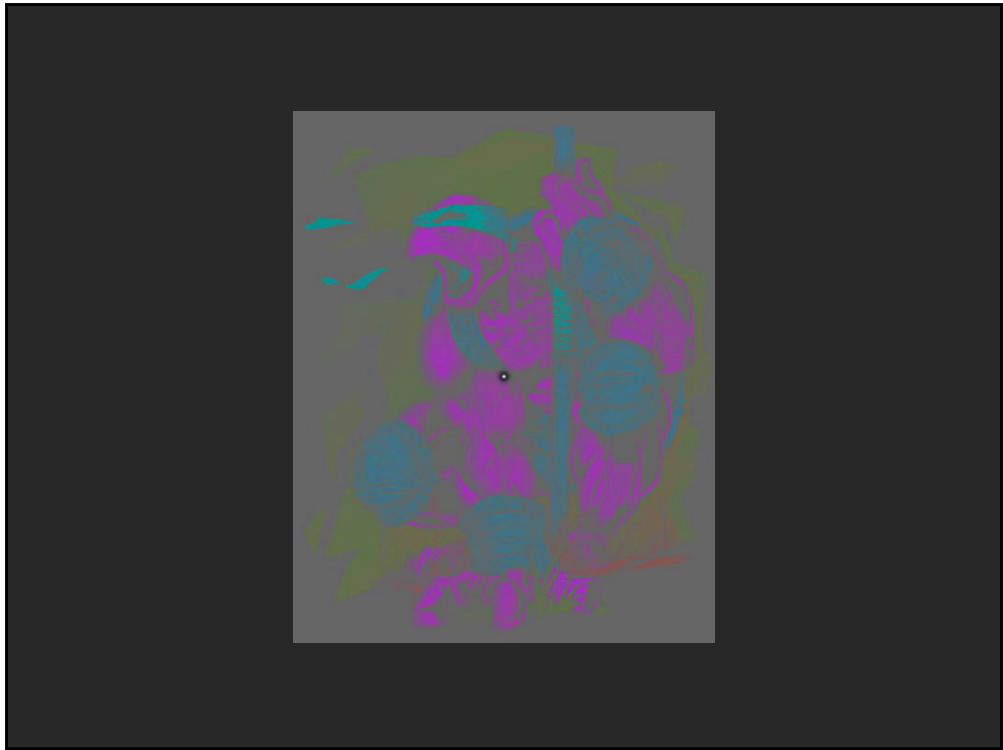
No reddish green, no bluish yellow

Color after images



26





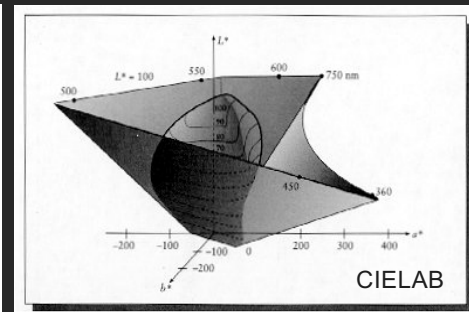
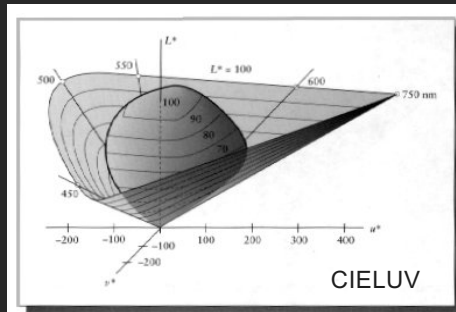
28



29

# CIE LUV and LAB color spaces

Standardized in 1976 to mathematically represent opponent processing theory



33

## Axes of CIE LAB

Correspond to opponent signals

$L^*$  = Luminance

$a^*$  = Red-green contrast

$b^*$  = Yellow-blue contrast

Scaling of axes to represent "color distance"

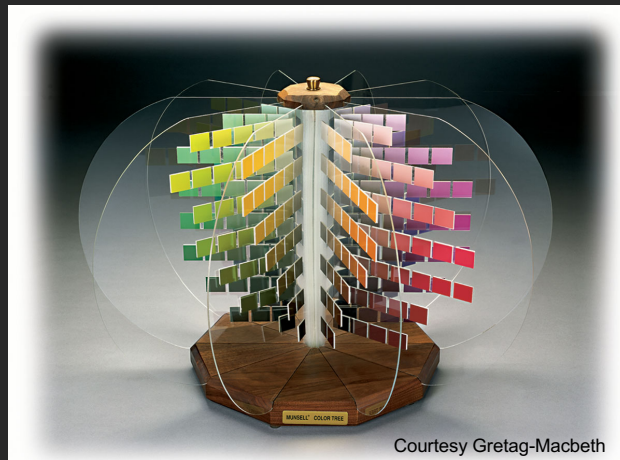
JND = Just noticeable difference ( $\sim 2.3$  units)

34

# Munsell Atlas

---

Developed the first perceptual color system based on his experience as an artist (1905)

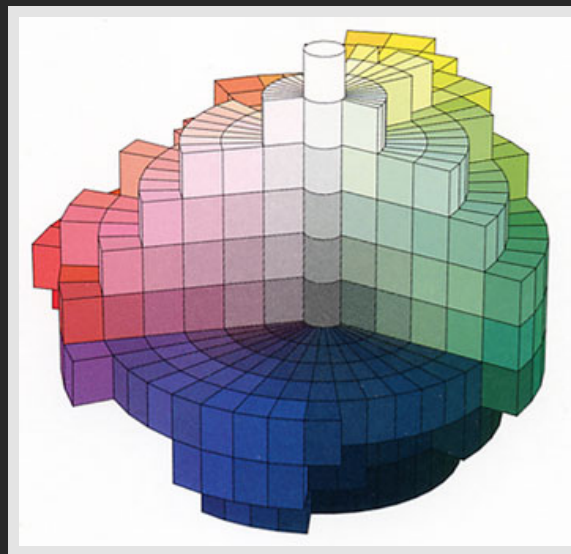


Courtesy Gretag-Macbeth

35

# Hue, Value, Chroma

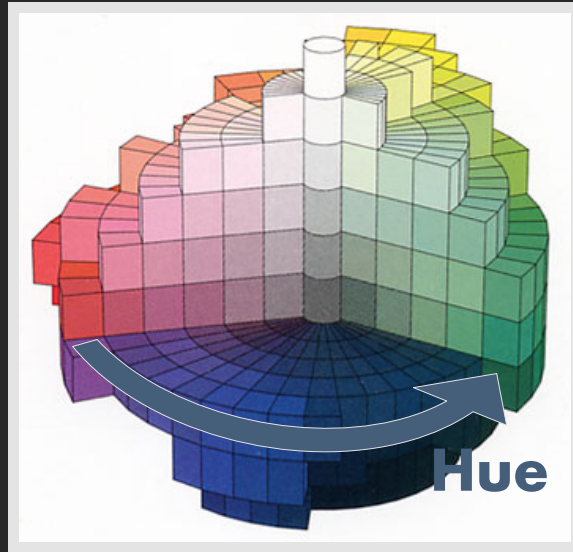
---



36

# Hue, Value, Chroma

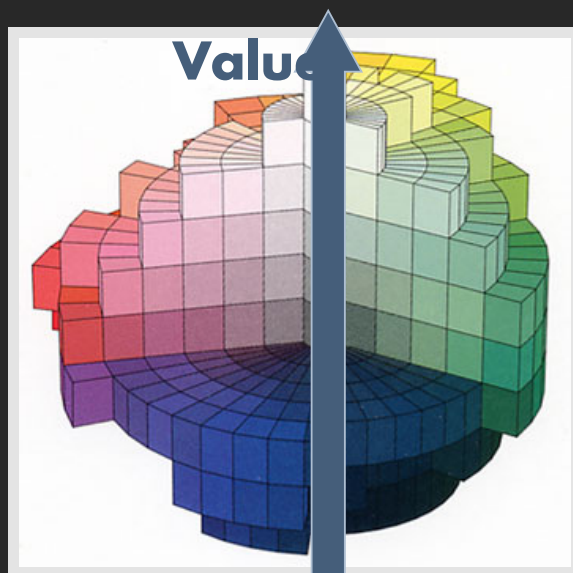
---



37

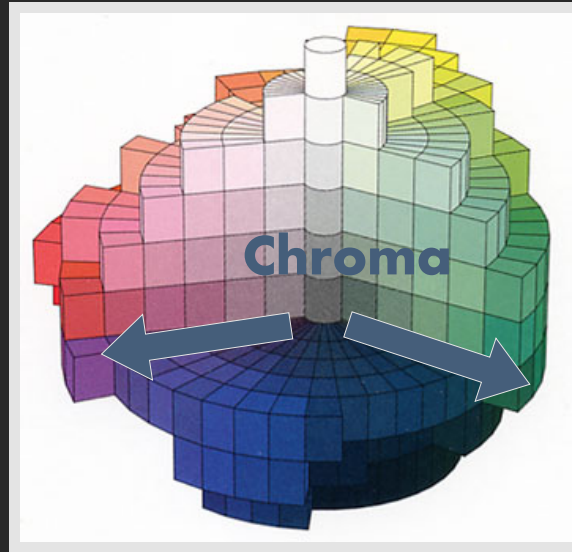
# Hue, Value, Chroma

---



38

# Hue, Value, Chroma



39

# Pseudo-Perceptual Models

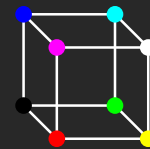
**HLS, HSV, HSB**

**NOT perceptual models**

**Simple re-notation of RGB**

- View along gray axis
- See a hue hexagon
- L or V is grayscale pixel value

**Cannot predict perceived lightness**

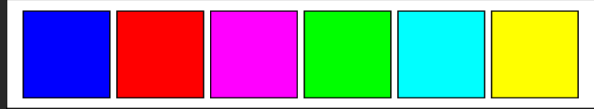


41

# Perceptual brightness

---

Color palette



HSL Lightness  
(Photoshop)

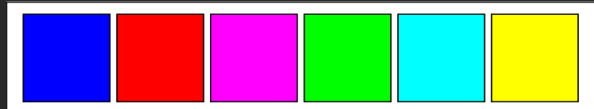


42

# Perceptual brightness

---

Color palette



Luminance Y  
(CIE XYZ)

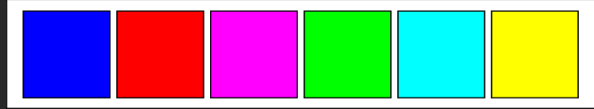


43

# Perceptual brightness

---

Color palette



Munsell Value

L\* (CIE LAB)



44

“In order to use color effectively  
it is necessary to recognize that  
it deceives continually.”

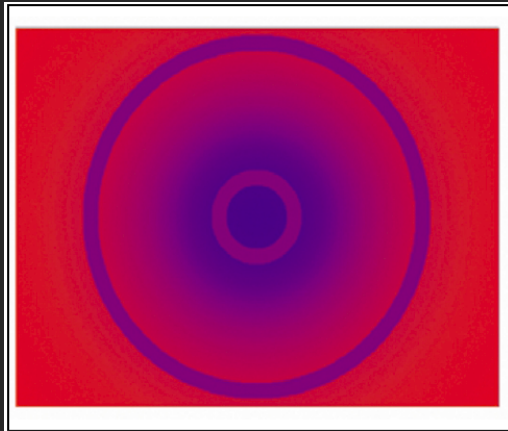
- Josef Albers, *Interaction of Color*

49

## Simultaneous Contrast

---

The inner and outer thin rings are the physical purple

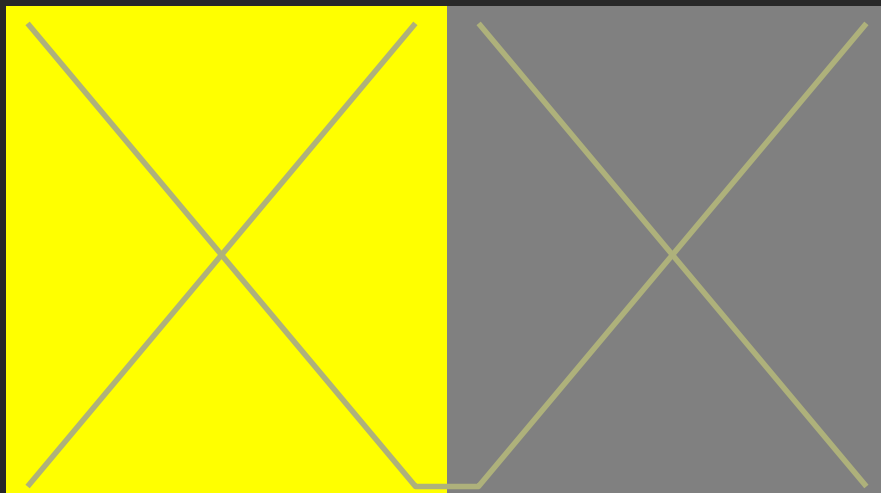


Donald MacLeod

50

## Simultaneous Contrast

---



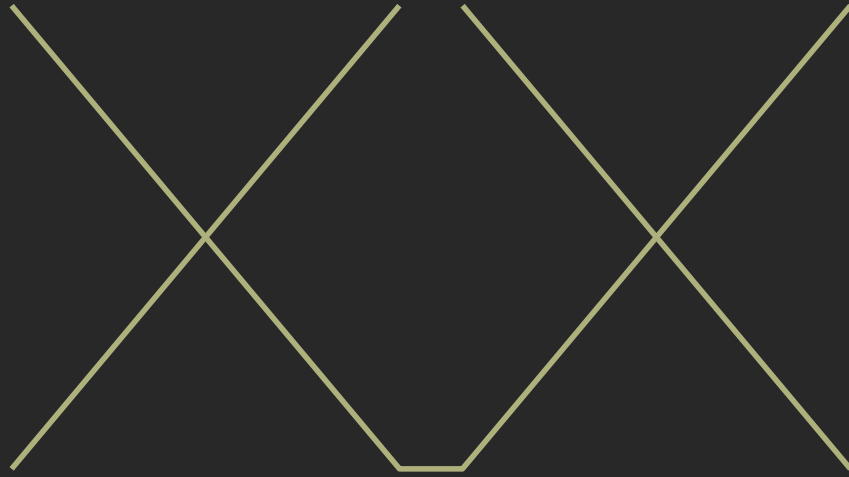
Josef Albers

53



# Simultaneous Contrast

---

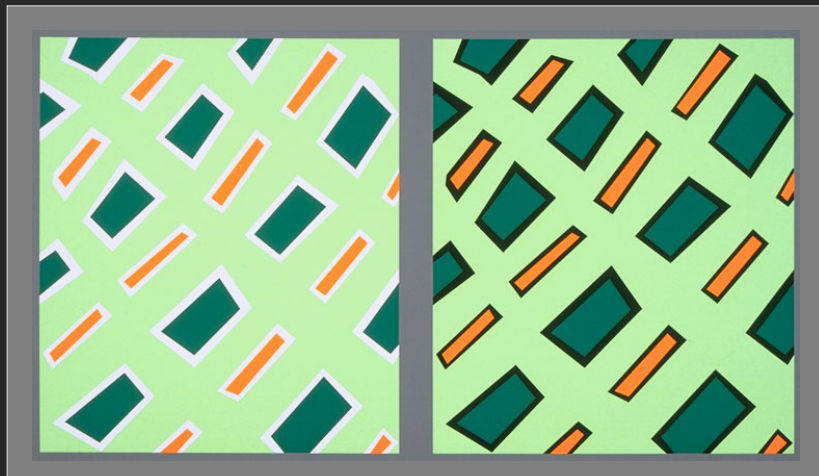


Josef Albers

54

# Bezold Effect

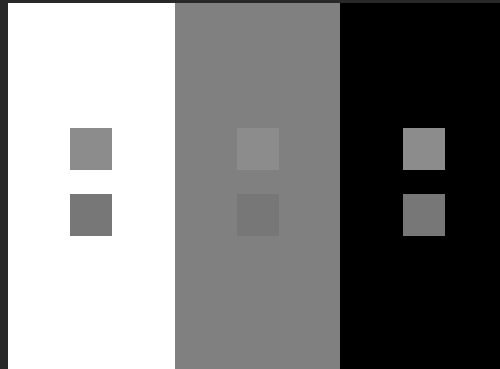
---



62

# Crispening

Perceived difference depends on background



From Fairchild, *Color Appearance Models*

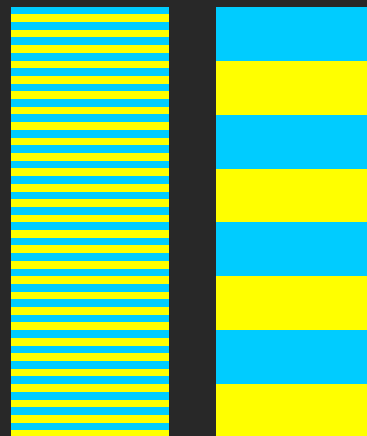
63

# Spreading

Adjacent colors blend

Spatial frequency

- The paint chip problem
- Small text, lines, glyphs
- Image colors



Redrawn from *Foundations of Vision*  
© Brian Wandell, Stanford University

64

# Announcements

70

## Final project

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### New visualization research or data analysis project

- **Research:** Pose problem, Implement creative solution
- **Data analysis:** Analyze dataset in depth & make a visual explainer

### Deliverables

- **Research:** Implementation of solution
- **Data analysis/explainer:** Article with multiple interactive visualizations
- 6-8 page paper

### Schedule

- Project proposal: **Wed 2/19**
- Design review and feedback: **3/9 and 3/11**
- Final presentation: **3/16 (7-9pm) Location: TBD**
- Final code and writeup: **3/18 11:59pm**

### Grading

- Groups of **up to 3 people**, graded individually
- Clearly report responsibilities of each member

71

## THE BROWN INSTITUTE FOR MEDIA INNOVATION

Join us for a talk and conversation with Brown Institute Director, Professor Maneesh Agrawala,  
featuring

**Sean Rameswaram**  
Host of Vox's *Today, Explained*



Tuesday, February 18 – 5pm  
Allen 101x, Cypress Auditorium  
Paul G. Allen Building  
330 Jane Stanford Way



RSVP: [http://bit.ly/bimi\\_Rameswaram](http://bit.ly/bimi_Rameswaram)

The Brown Institute is excited to welcome Sean Rameswaram, host of *Today, Explained*, Vox's daily explainer podcast. As advertised by Vox, *Today, Explained* is your all killer, no filler, Monday to Friday news. Sean, a veteran of the podcast space, will discuss Vox's novel approach to their daily show and will join Brown Institute Director Maneesh Agrawala in conversation about the state of podcasts. Before joining Vox to host its daily news podcast, Sean was a correspondent for Radiolab's *More Perfect*. He has also made radio for the CBC, NPR, and WNYC, where he hosted the fondly remembered *Sideshow* podcast for Studio 360.

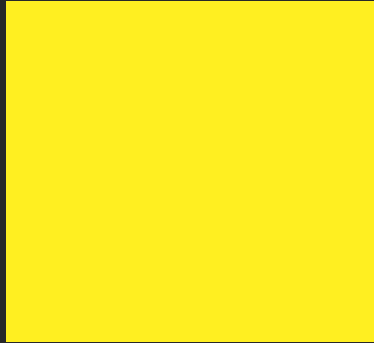
72

## Color Naming

73

**What color is this?**

---



74

**What color is this?**

---

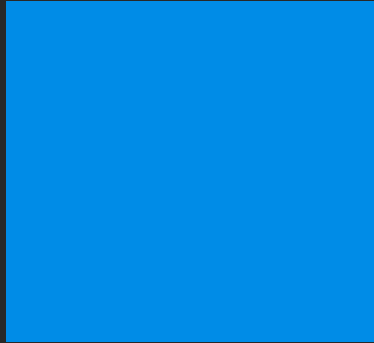


"Yellow"

75

**What color is this?**

---



76

**What color is this?**

---



"Blue"

77

**What color is this?**

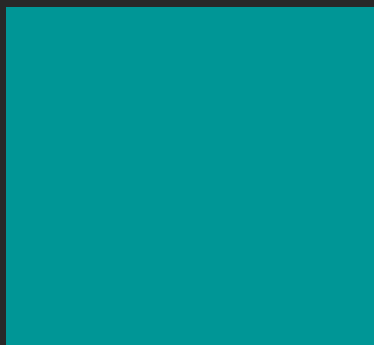
---



78

**What color is this?**

---



**"Teal" ?**

79

# Colors according to XKCD...



80

# Basic color terms

Chance discovery by Brent Berlin and Paul Kay

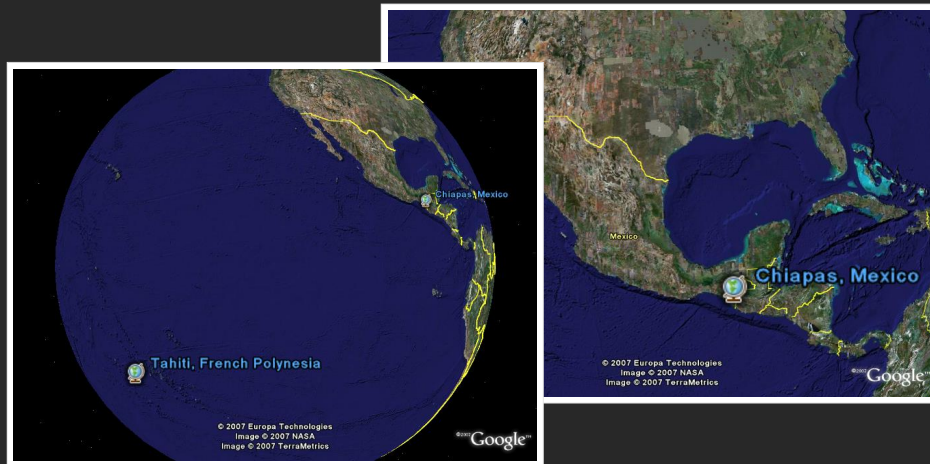


81



# Basic color terms

Chance discovery by Brent Berlin and Paul Kay



82

# Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay

Initial study in 1969

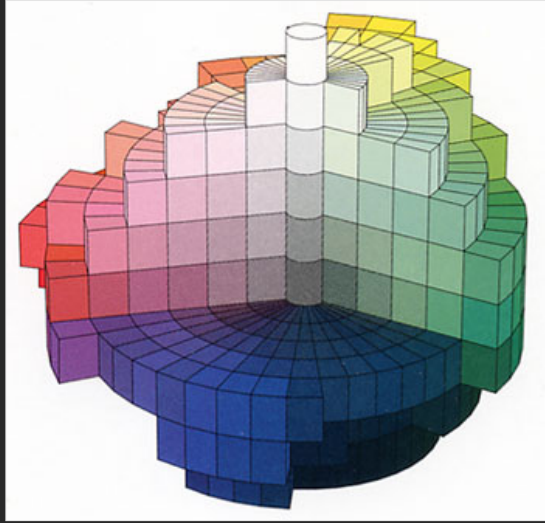
Surveyed speakers from 20 languages

Literature from 69 languages

83

# World color survey

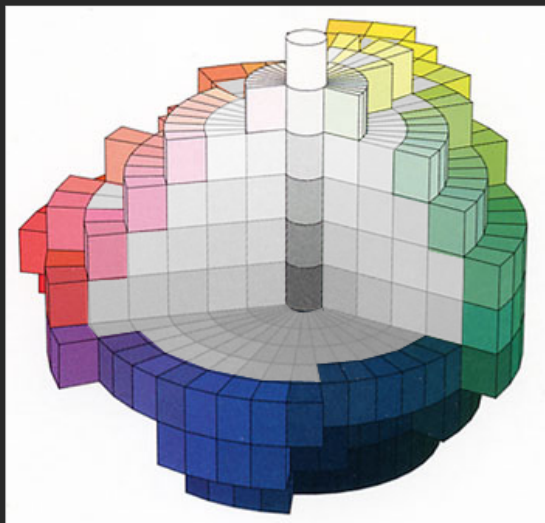
---



84

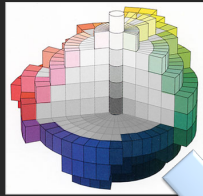
# World color survey

---

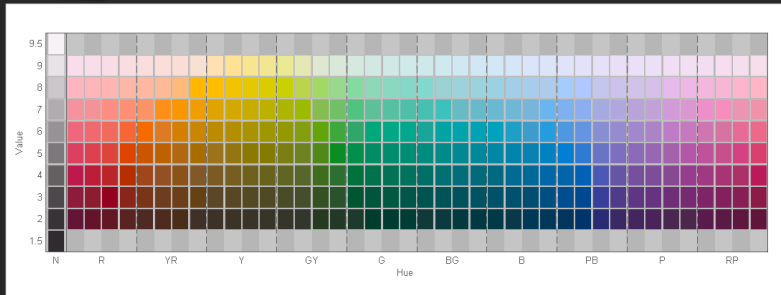


85

# World color survey

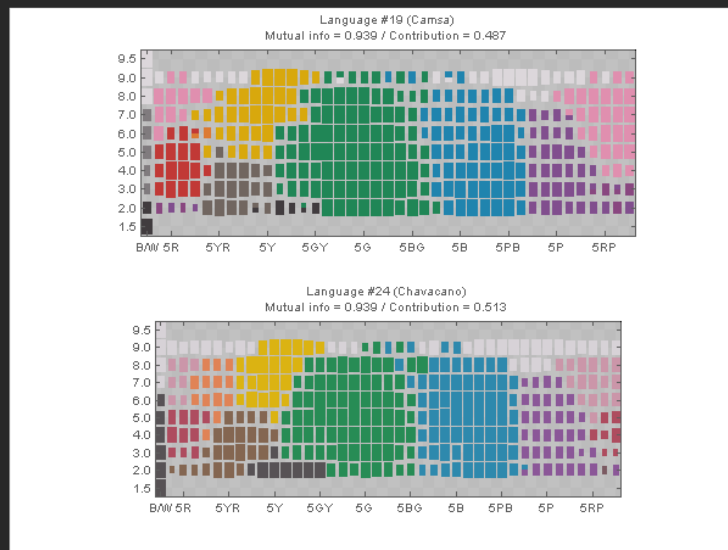


Naming information from 2616 speakers from 110 languages on 330 Munsell color chips



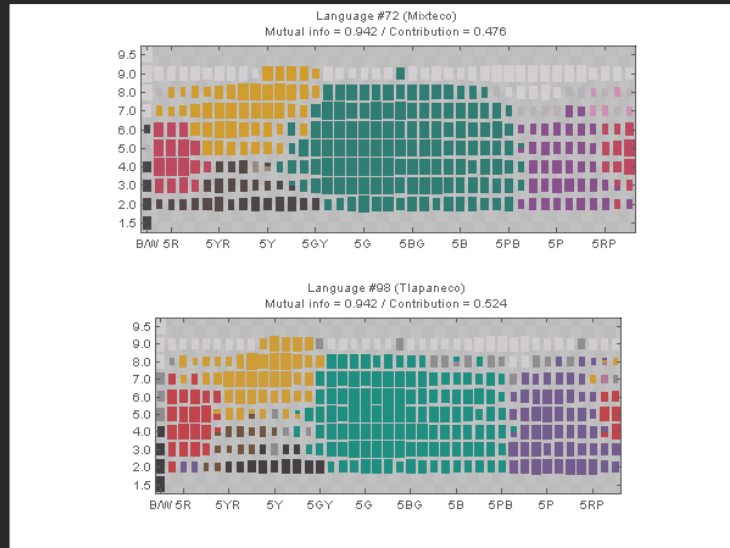
86

# Results from WCS (South Pacific)



87

# Results from WCS (Mexico)



88

# Universal (?) Basic Color Terms

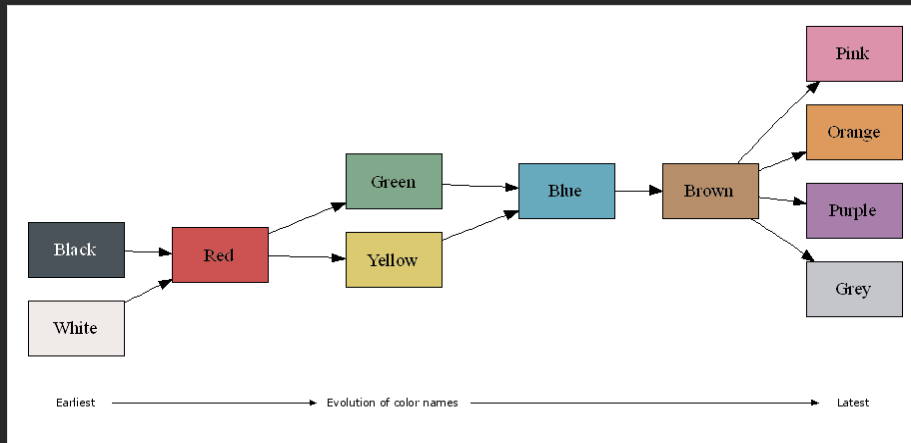
Basic color terms recur across languages



89

# Evolution of Basic Color Terms

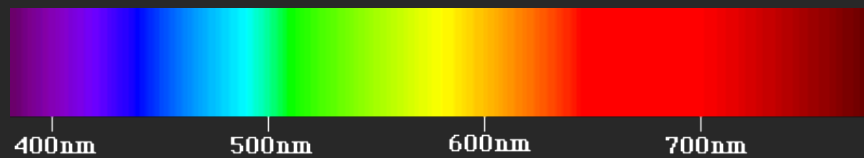
Proposed universal evolution across languages



90

# Rainbow color ramp

We associate and group colors together, often using the name we assign to the colors

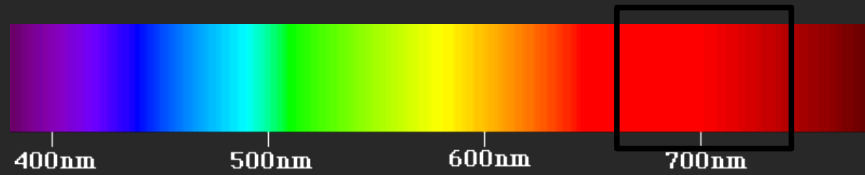


91

## Rainbow color ramp

---

We associate and group colors together, often using the name we assign to the colors

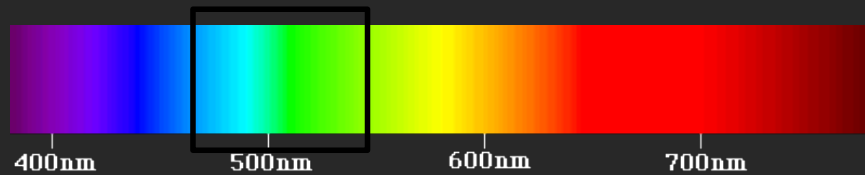


92

## Rainbow color ramp

---

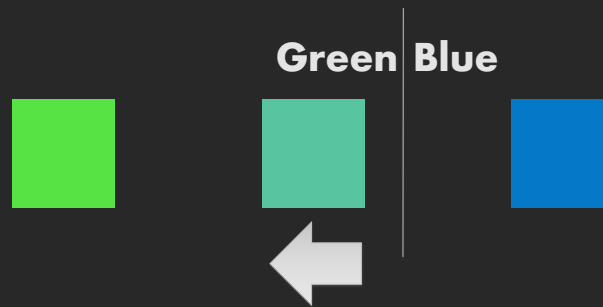
We associate and group colors together, often using the name we assign to the colors



93

# Naming affects color perception

## Color name boundaries



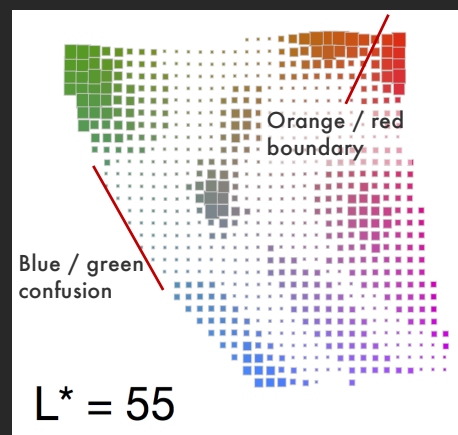
94

# Color naming models

[Heer & Stone]

Model 3 million responses from XKCD survey

Bins in LAB space  
sized by saliency:  
How much do people  
agree on color name?  
Modeled by entropy  
of  $p(\text{name} \mid \text{color})$



95

# Palette Design + Color Names

Minimize overlap and ambiguity of color names

Color Name Distance										Saliency	Name
0.00	1.00	1.00	1.00	0.98	1.00	1.00	1.00	1.00	0.20	.47	blue 62.9%
1.00	0.00	1.00	0.97	1.00	1.00	1.00	1.00	0.96	1.00	.90	orange 93.9%
1.00	1.00	0.00	1.00	1.00	1.00	1.00	1.00	0.90	0.99	.67	green 79.8%
1.00	0.97	1.00	0.00	1.00	0.95	0.99	1.00	1.00	1.00	.66	red 80.4%
0.98	1.00	1.00	1.00	0.00	0.96	0.91	0.97	1.00	0.99	.47	purple 51.4%
1.00	1.00	1.00	0.95	0.96	0.00	0.97	0.93	0.98	1.00	.37	brown 54.0%
1.00	1.00	1.00	0.99	0.91	0.97	0.00	1.00	1.00	1.00	.58	pink 71.7%
1.00	1.00	1.00	1.00	0.97	0.93	1.00	0.00	1.00	1.00	.67	grey 79.4%
1.00	0.96	0.90	1.00	1.00	0.98	1.00	1.00	0.00	1.00	.18	yellow 31.2%
0.20	1.00	0.99	1.00	0.99	1.00	1.00	1.00	1.00	0.00	.25	blue 25.4%
Tableau-10										Average	0.97
											.52

<http://vis.stanford.edu/color-names>

96

# Palette Design + Color Names

Minimize overlap and ambiguity of color names

Color Name Distance										Saliency	Name
0.00	1.00	1.00	0.89	0.07	1.00	0.35	0.99	1.00	0.89	.30	blue 50.5%
1.00	0.00	0.99	1.00	1.00	0.92	1.00	0.84	0.98	0.99	.21	red 27.8%
1.00	0.99	0.00	1.00	0.98	1.00	1.00	1.00	0.17	1.00	.34	green 36.8%
0.89	1.00	1.00	0.00	0.98	1.00	0.71	0.93	1.00	0.32	.55	purple 67.3%
0.07	1.00	0.98	0.98	0.00	1.00	0.36	1.00	0.97	0.95	.20	blue 36.6%
1.00	0.92	1.00	1.00	1.00	0.00	1.00	0.97	0.99	1.00	.39	orange 51.9%
0.35	1.00	1.00	0.71	0.36	1.00	0.00	0.95	0.92	0.42	.13	blue 15.7%
0.99	0.84	1.00	0.93	1.00	0.97	0.95	0.00	0.98	0.85	.16	pink 29.4%
1.00	0.98	0.17	1.00	0.97	0.99	0.92	0.98	0.00	0.97	.12	green 21.7%
0.89	0.99	1.00	0.32	0.95	1.00	0.42	0.85	0.97	0.00	.30	purple 23.9%
Excel-10										Average	0.87
											.27

<http://vis.stanford.edu/color-names>

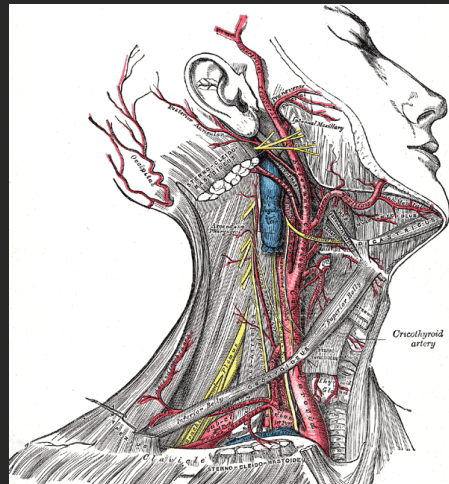
97



# Using Color in Visualization

99

## Gray's Anatomy



Superficial dissection of the right side of the neck,  
showing the carotid and subclavian arteries

<http://www.bartleby.com/107/illus520.html>

101

# Molecular Models

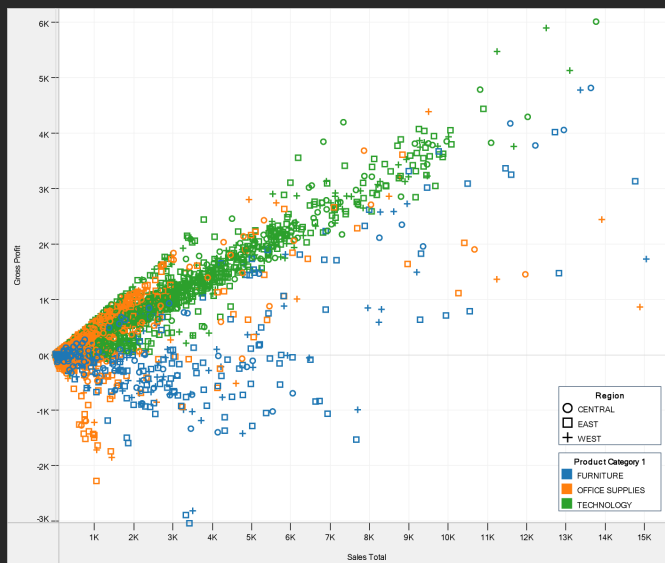


Organic Chemistry Molecular Model Set

<http://www.indigo.com/models/gphmodel/62003.html>

102

# Product Categories



Created by Tableau - Visual Analysis for Databases™

103

# Grouping, Highlighting

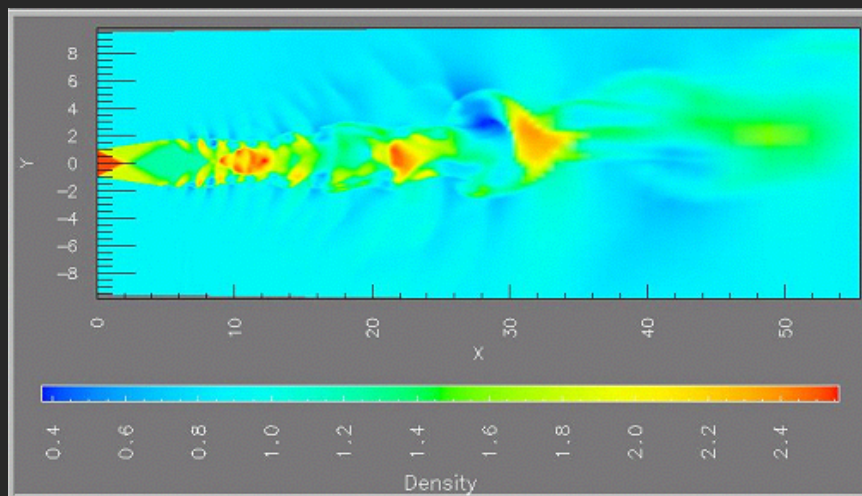
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z
red	25.37	13.70	0.05	26.27	14.13	0.04	18.41	10.16	0.05	17.43	9.30	0.00
green	22.14	51.24	0.35	20.68	49.17	0.44	21.11	46.00	0.20	16.36	37.95	0.12
blue	13.17	3.71	74.89	15.38	5.20	86.83	11.55	3.37	65.53	9.96	3.44	56.14
gray	63.46	73.30	78.05	64.66	71.99	90.08	52.96	62.49	67.99	45.54	53.65	58.14
black	0.66	0.70	0.77	0.63	0.66	1.09	0.47	0.58	0.70	0.44	0.54	0.71

	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z
red	25.37	13.70	0.05	26.27	14.13	0.04	18.41	10.16	0.05	17.43	9.30	0.00
green	22.14	51.24	0.35	20.68	49.17	0.44	21.11	46.00	0.20	16.36	37.95	0.12
blue	13.17	3.71	74.89	15.38	5.20	86.83	11.55	3.37	65.53	9.96	3.44	56.14
gray	63.46	73.30	78.05	64.66	71.99	90.08	52.96	62.49	67.99	45.54	53.65	58.14
black	0.66	0.70	0.77	0.63	0.66	1.09	0.47	0.58	0.70	0.44	0.54	0.71

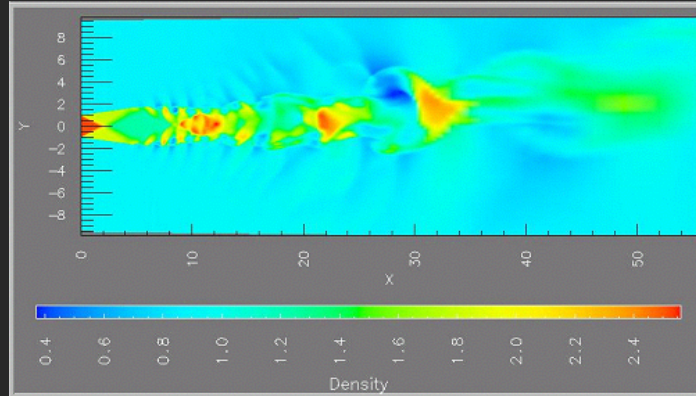
104

# Mapping Data to Color (Rainbows)



123

# Avoid rainbow color maps!



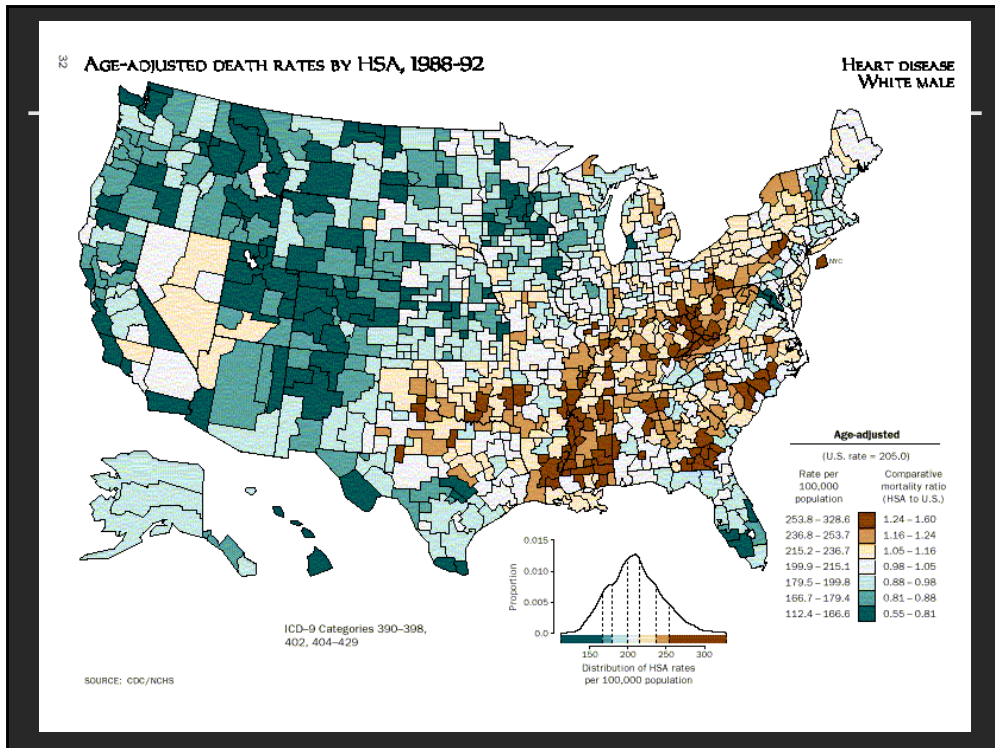
1. Hues are not naturally ordered
2. People segment colors into classes, perceptual banding
3. Naïve rainbows unfriendly to color blind viewers
4. Low luminance colors (blue) hide high frequencies

124

# Color Brewer

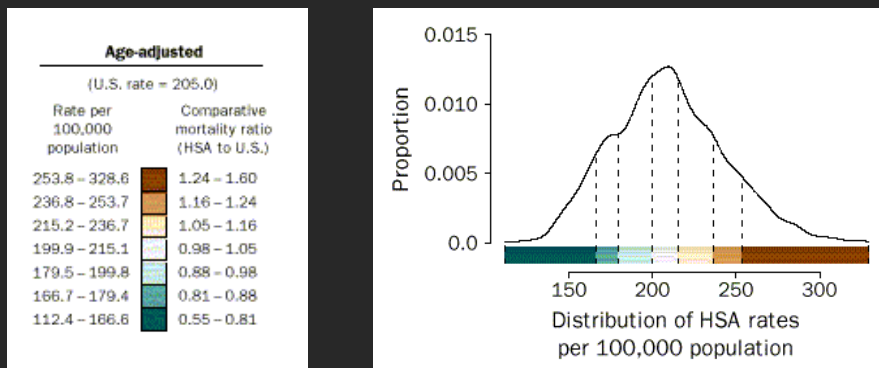
[www.colorbrewer.org](http://www.colorbrewer.org)

130



131

## Classing quantitative data



Age-adjusted mortality rates for the United States  
Common option: break into 5 or 7 quantiles

132

# Classing Quantitative Data

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Equal interval (arithmetic progression)

Quantiles (*recommended*)

Standard deviations

Clustering (Jenks' natural breaks / 1D K-Means)

Minimize within group variance

Maximize between group variance

133

# Quantitative color encoding

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## Sequential color scale

Ramp in luminance, possibly also hue

Typically higher values map to darker colors



## Diverging color scale

Useful when data has a meaningful "midpoint"

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints

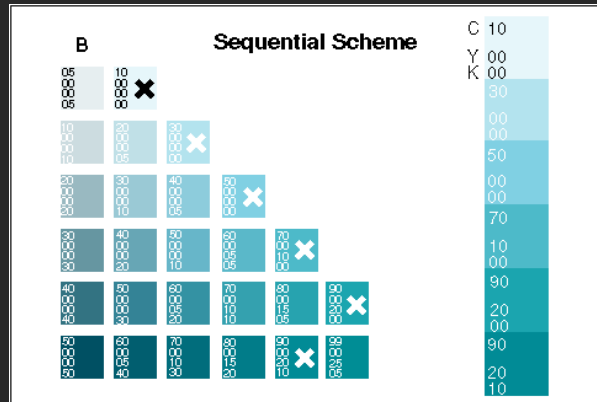


**Limit number of steps in color to 3-9**

134

# Sequential Scale Single Hue

Ramp primarily in luminance, subtle hue difference

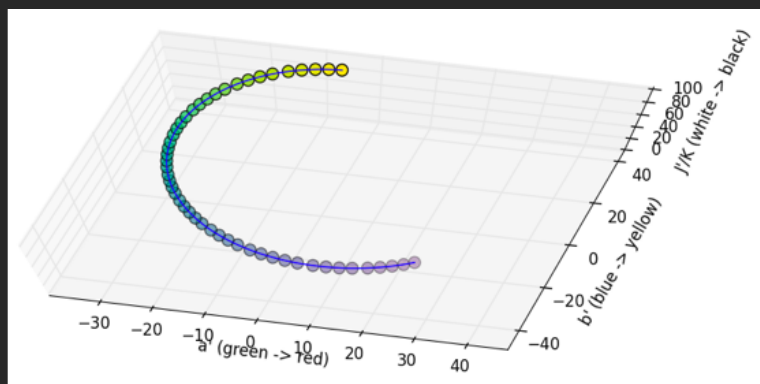


<http://www.personal.psu.edu/faculty/c/a/cab38/ColorSch/Schemes>

138

# Sequential Scale Multi Hue

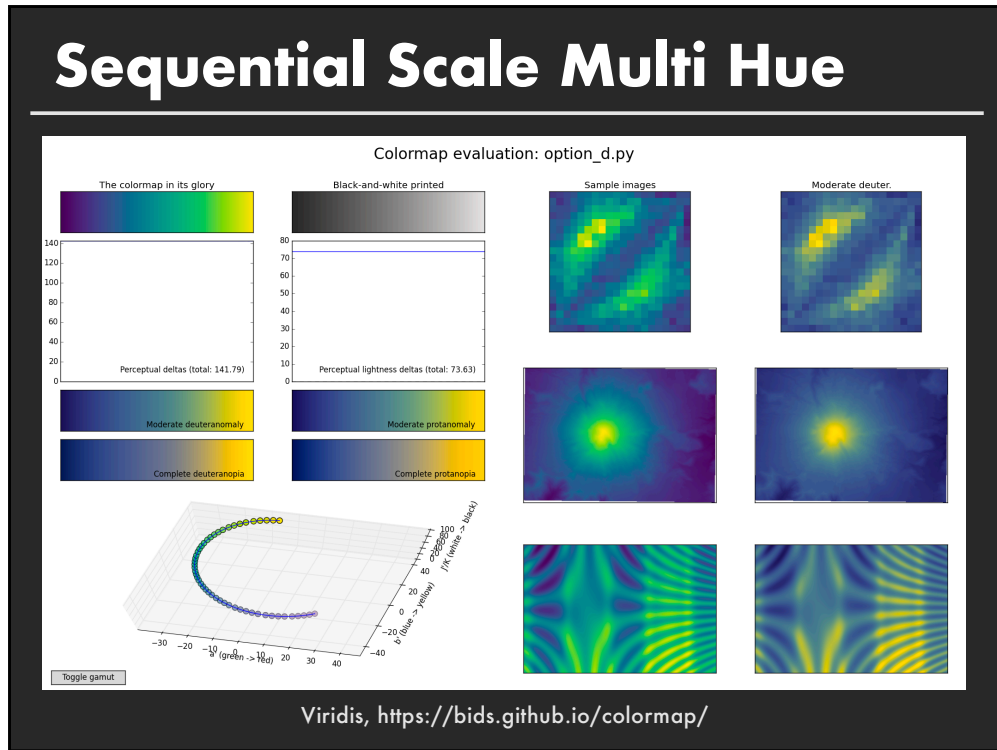
Ramp luminance & hue in perceptual color space  
Avoid contrasts subject to color blindness!



<http://www.personal.psu.edu/faculty/c/a/cab38/ColorSch/Schemes>

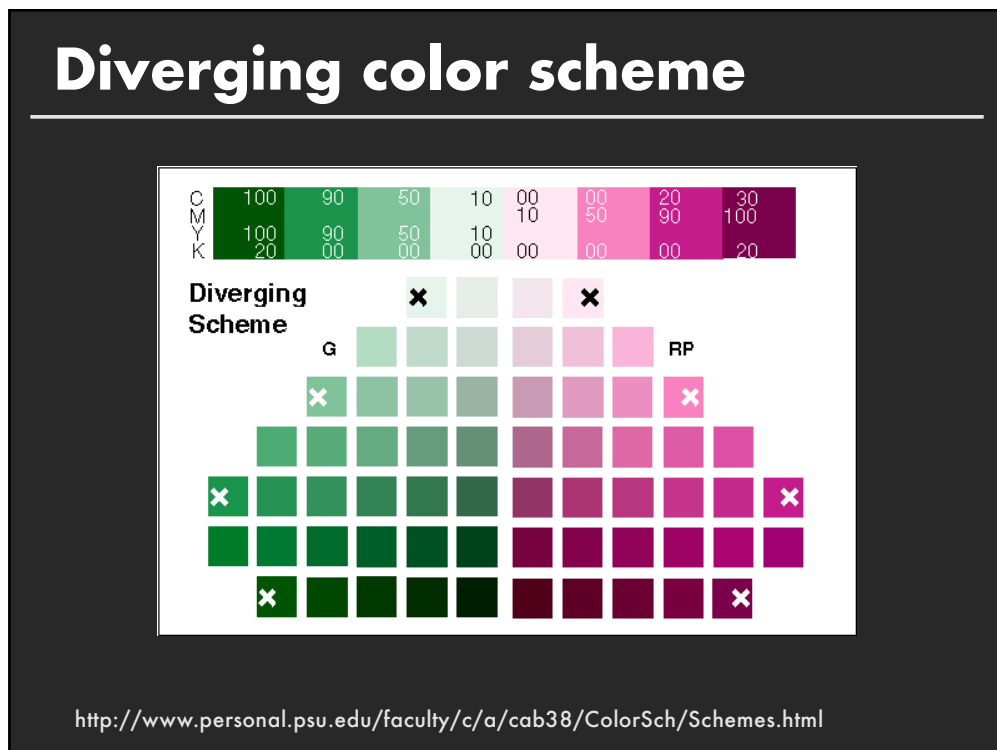
139

# Sequential Scale Multi Hue



140

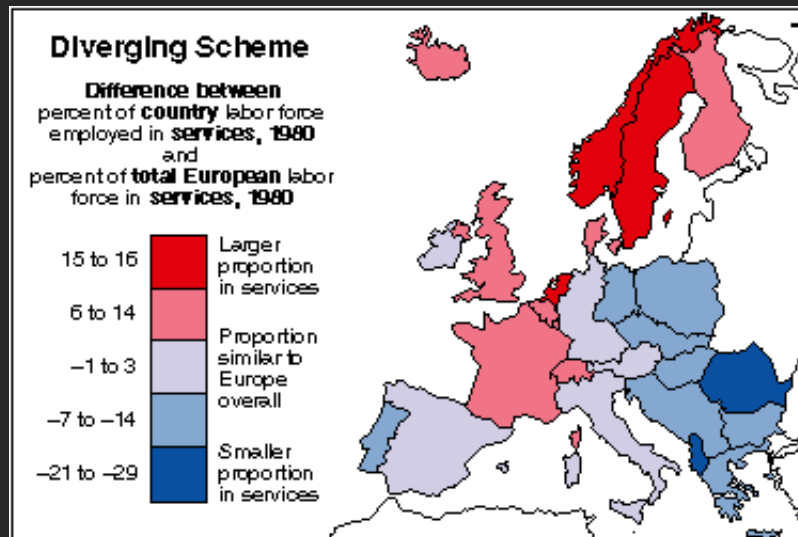
# Diverging color scheme



141



## Diverging color scheme



143

## Diverging color scheme

### Hue Transition

### Carefully handle midpoint

- Critical class
  - Low, Average, High
  - 'Average' should be gray
- Critical breakpoint
  - Defining value e.g. 0
  - Positive & negative should use different hues

Extremes saturated, middle desaturated

144

## Summary: Color Design Principles

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Control value (darkness/lightness)

- Ensure legibility
- Avoid unwanted emphasis

Use a limited hue palette (~ 6 colors)

- Control color “pop out”
- Be aware of perceptual color grouping
- Avoid clutter from too many competing colors

Use neutral backgrounds

- Control impact of color
- Minimize simultaneous contrast