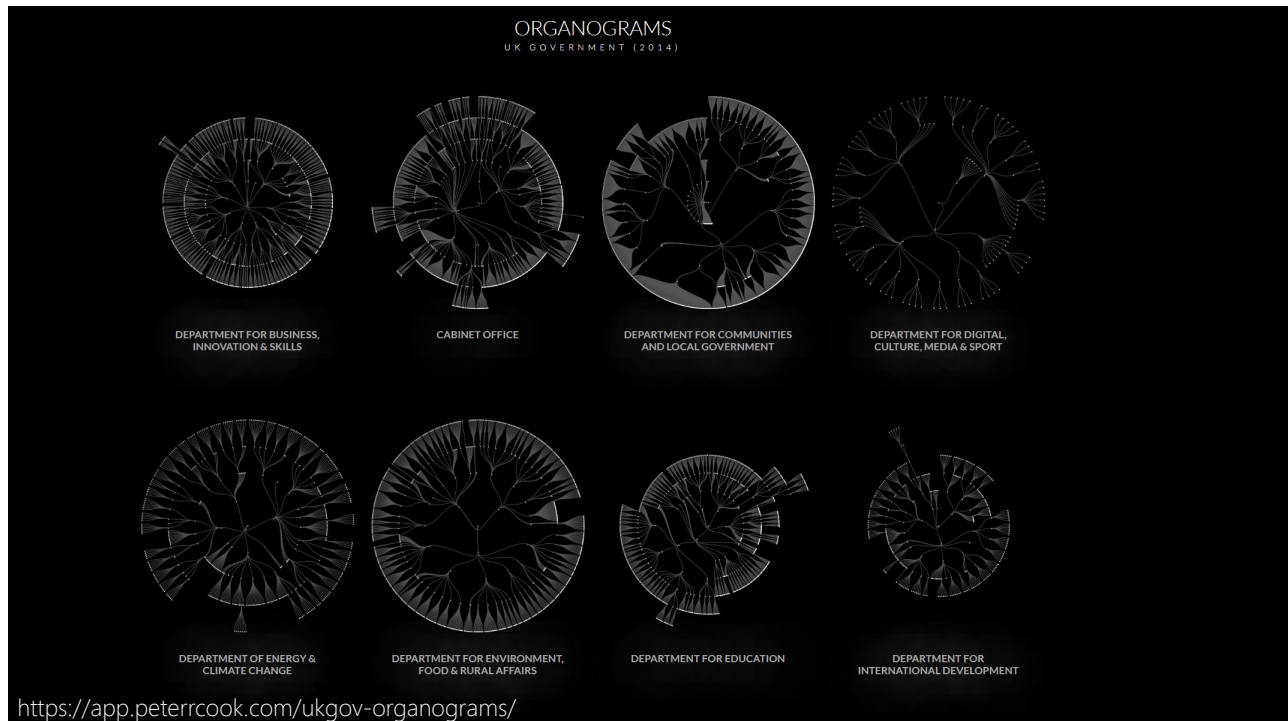


# NETWORK VISUALIZATION

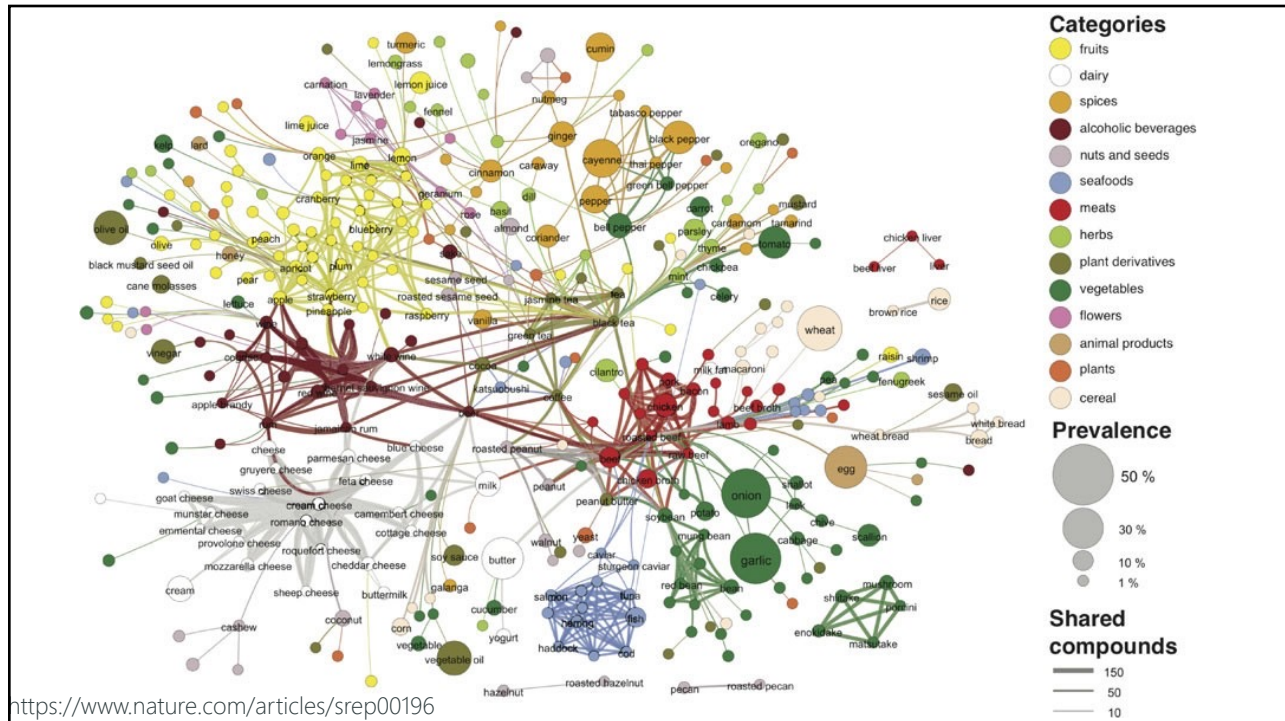
CS 448B | Fall 2023

MANEESH AGRAWALA

1



4



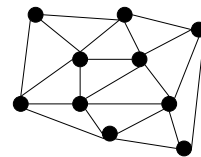
5

# GRAPHS AND TREES

## Graphs

Model relations among data

Nodes and edges

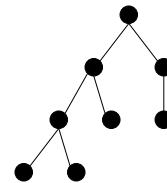


## Trees

Graphs with hierarchical structure

Connected graph with  $N-1$  edges

Nodes as *parents* and *children*



6

## SPATIAL LAYOUT

**Primary concern – positioning of nodes and edges**

**Often (but not always) goal is to depict structure**

- Connectivity, path-following
- Topological distance
- Clustering/grouping
- Ordering (e.g., hierarchy level)

7

## NETWORK ANALYSIS TASKS [Pretorius 2013]

**Structure-based:** relationships and connectivity

**Attribute-based:** properties associated with node or link

**Browsing:** follow paths in the data

**Estimation:** summarization and temporal changes

9

## NETWORK ANALYSIS TASKS [Pretorius 2013]

### **Structure-based:** relationships and connectivity

Find all the friends of friends of Kermit

Find all the people who are friends of Animal and Gonzo

Find shortest path between two people: Six degrees of separation

### **Attribute-based:** properties associated with node or link

### **Browsing:** follow paths in the data

### **Estimation:** summarization and temporal changes

10

## NETWORK ANALYSIS TASKS [Pretorius 2013]

### **Structure-based:** relationships and connectivity

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Find all friends of Fozzie that are students at Stanford (node property)

Find all friends of Fozzie that are their family (link property)

### **Browsing:** follow paths in the data

### **Estimation:** summarization and temporal changes

11

## NETWORK ANALYSIS TASKS [Pretorius 2013]

### **Structure-based:** relationships and connectivity

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Find all friends of Fozzie that are their family (link property)

### **Browsing:** follow paths in the data

Find Kermit's friend with first name Beaker and then find Beaker's mentor Bunsen

### **Estimation:** summarization and temporal changes

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## NETWORK ANALYSIS TASKS [Pretorius 2013]

### **Structure-based:** relationships and connectivity

Find all the friends of friends of Kermit

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Find all friends of Fozzie that are their family (link property)

### **Browsing:** follow paths in the data

Find Kermit's friend with first name Beaker and then find Beaker's mentor Bunsen

### **Estimation:** summarization and temporal changes

How does Miss Piggy's friend group change over the course of a year

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# TODAY

## Learning Objectives

1. Techniques for visualizing trees
2. Techniques of laying out graphs
3. Alternative techniques for visualizing node-link data

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# TREE VISUALIZATION

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## COMMON TYPES OF TREE VISUALIZATION

### Indentation

Linear list, indentation encodes depth



### Node-Link diagrams

Nodes connected by lines/curves



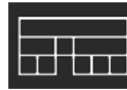
### Enclosure diagrams

Represent hierarchy by enclosure



### Layering

Layering and alignment



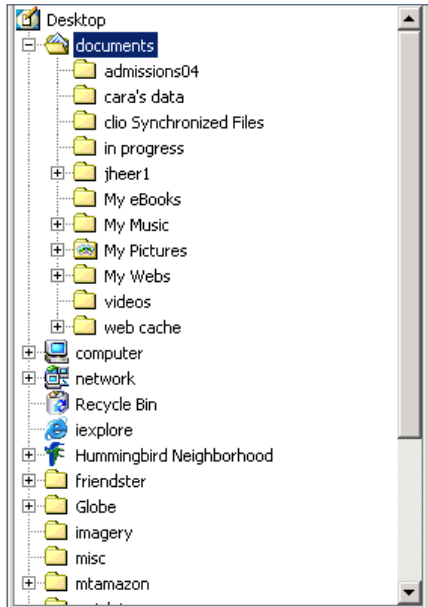
Tree layout is fast:  $O(n)$  or  $O(n \log n)$ , enabling real-time layout for interaction

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## INDENTATION

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# INDENTATION

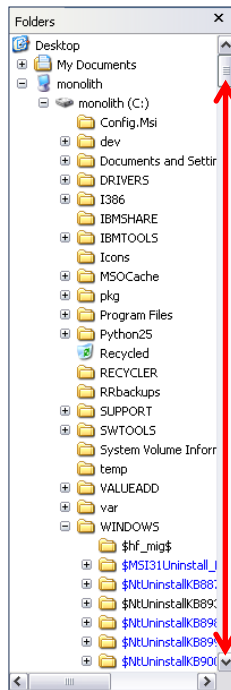


Items along vertically spaced rows  
 Indentation shows parent/child relationships  
 Often used in interfaces  
 Breadth/depth contend for space  
 Often requires scrolling

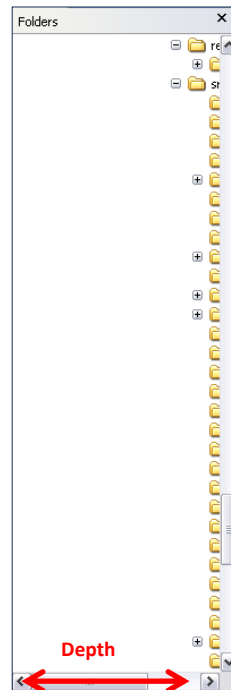


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# INDENTATION



Breadth



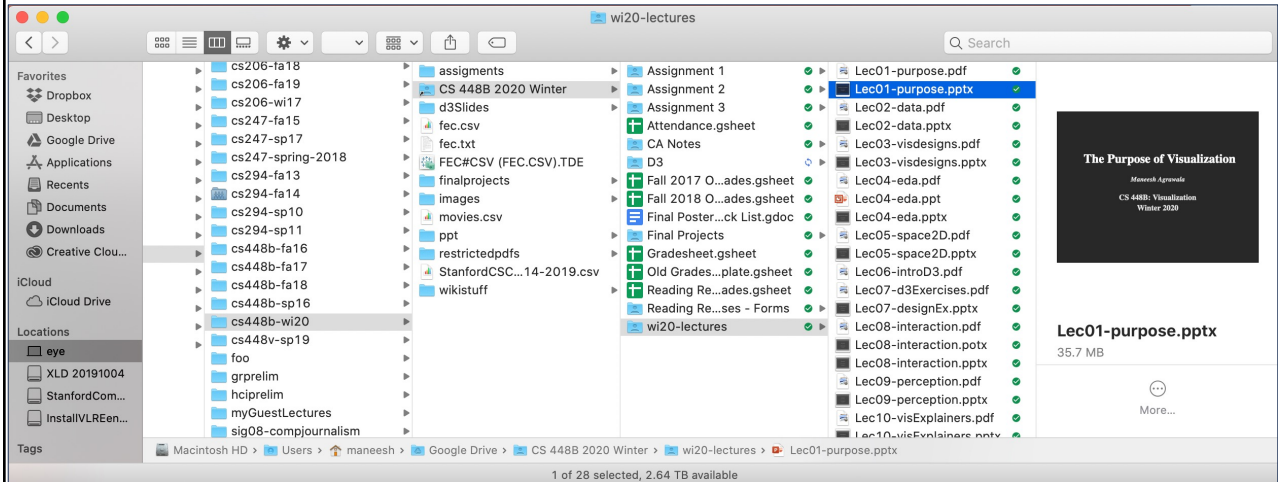
Depth



19



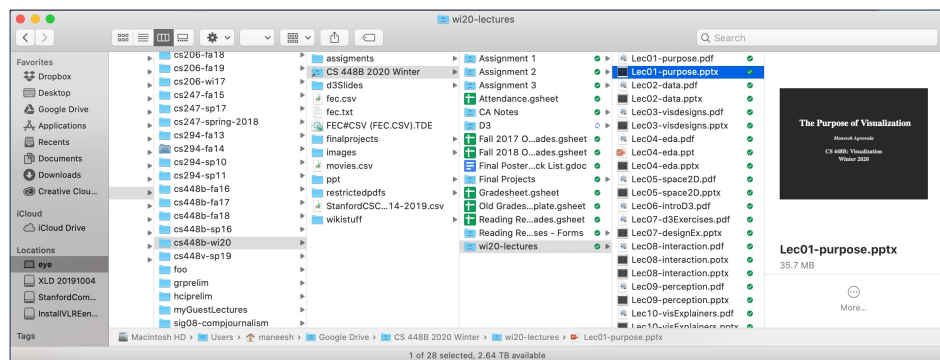
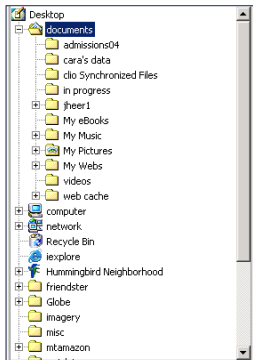
# SINGLE-FOCUS ACCORDION LIST



Separate breadth & depth in 2D  
Focus on single path at a time

20

# WHAT TASKS ARE THESE GOOD FOR?



## Benefits

Navigation + Browsing, Parent-child relationships

## Disadvantages

Network overview, Estimation, Comparison

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# NODE-LINK DIAGRAMS

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## NODE-LINK DIAGRAMS



**Nodes distributed in space, connected by straight or curved lines**

**Use 2D space to break apart breadth and depth**

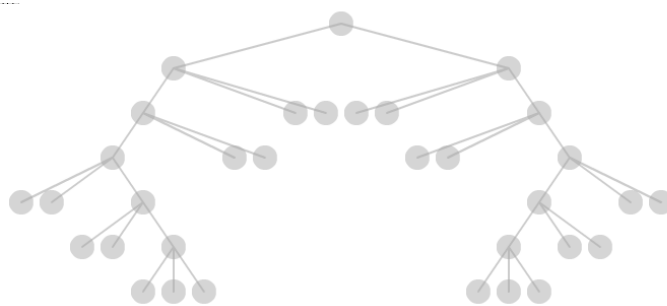
**Space used to communicate hierarchical orientation**

(e.g., towards *authority* or *generality*)

23

## BASIC RECURSIVE LAYOUT

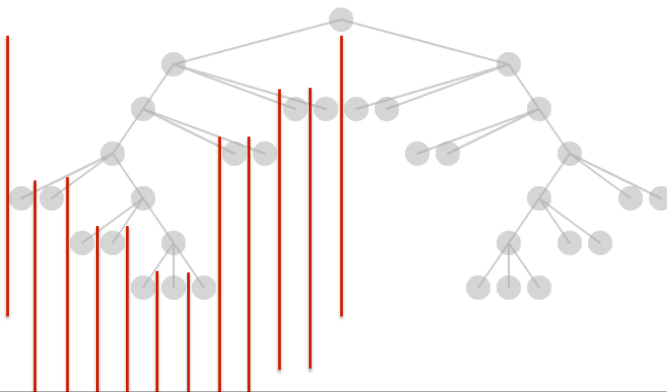
Repeatedly divide space for subtrees by leaf count



24

## BASIC RECURSIVE LAYOUT

Repeatedly divide space for subtrees by leaf count



25

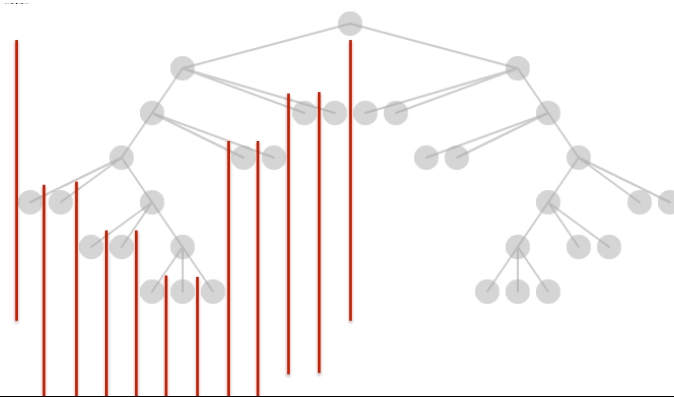
## BASIC RECURSIVE LAYOUT

Repeatedly divide space for subtrees by leaf count

Breadth of tree along one dimension

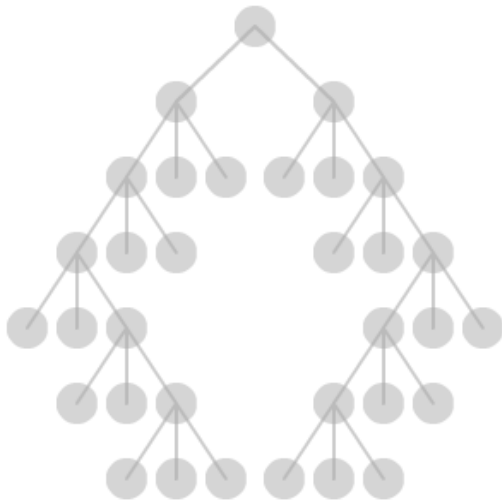
Depth along the other dimension

**Problem:** Exponential growth of breadth



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## REINGOLD & TILFORD'S "TIDY" LAYOUT



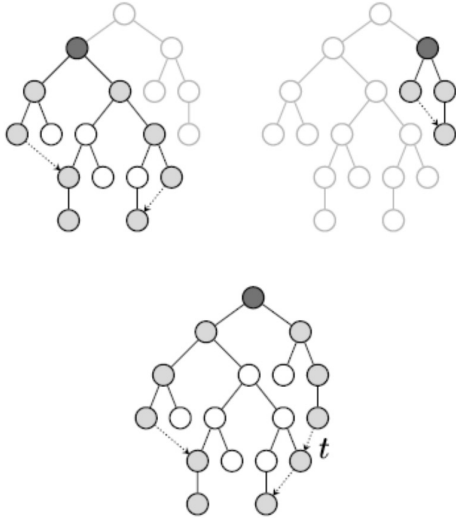
**Goal:** maximize density and symmetry

Originally for binary trees, extended by Walker to cover general case

Corrected by Buchheim et al. to achieve a linear time algorithm

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# REINGOLD & TILFORD LAYOUT

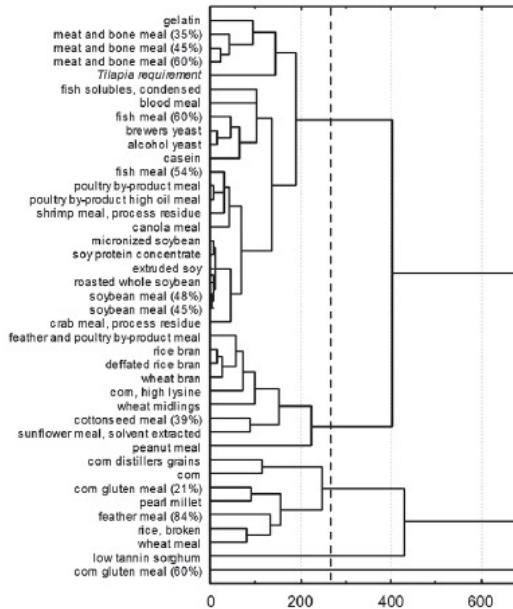


## Design Considerations

- Clearly encode depth
- No edge crossings
- Draw isomorphic subtrees identically (same shape)
- Preserve layout ordering and symmetry
- Compact space saving layout (don't waste space)**

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# CLUSTER DENDROGRAMS



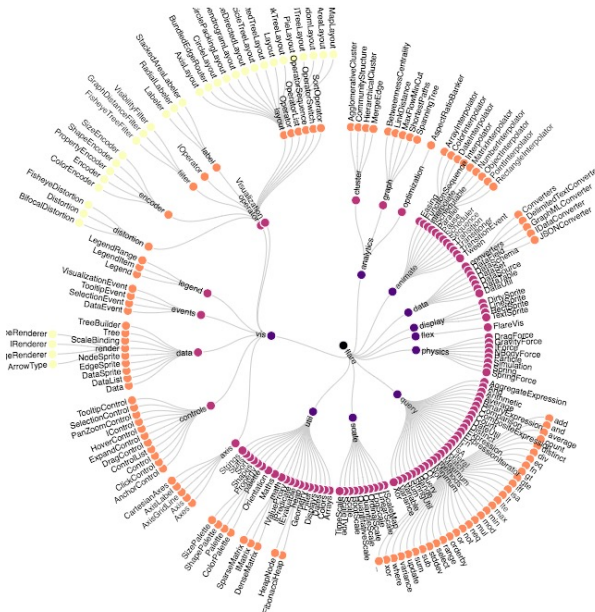
Depicts cluster trees produced by hierarchical clustering algorithms

Leaf nodes arranged in line, internal node depth indicates order/value at which clusters merge

Basic recursive layout with orthogonal two-segment edges

60

# RADIAL LAYOUT



Node-link diagram in polar coordinates

Radius encodes depth, root at center

Angular sectors assigned to subtrees (basic recursive approach)

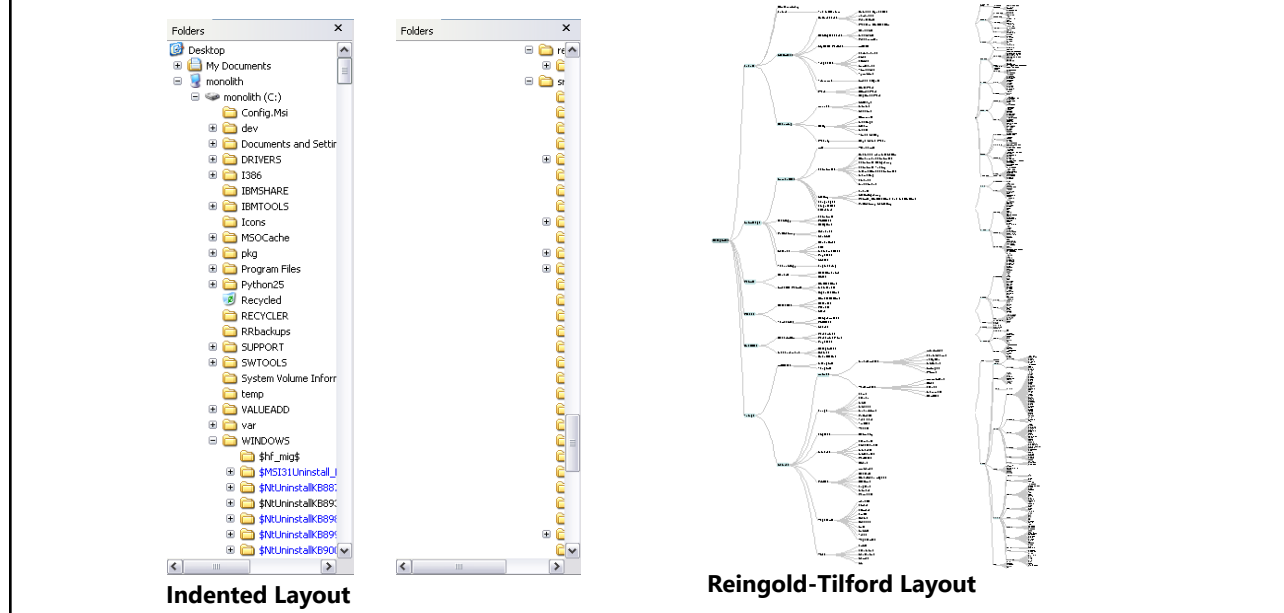
Reingold-Tilford approach can also be applied here

61

# ANALYSIS TASKS: FOCUS + CONTEXT

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# VISUALIZING LARGE HIERARCHIES



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## MORE NODES, MORE PROBLEMS...

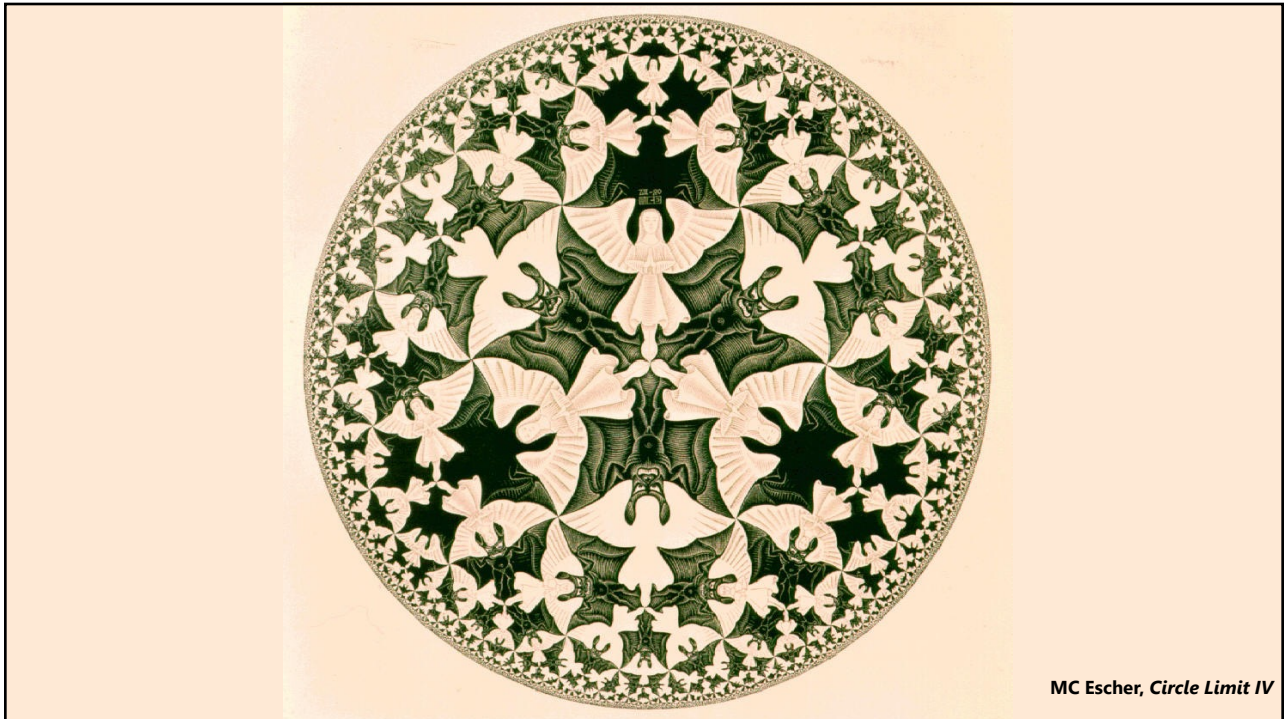
### Scale

Tree breadth often grows exponentially  
Even with tidier layout, quickly run out of space

### Possible solutions

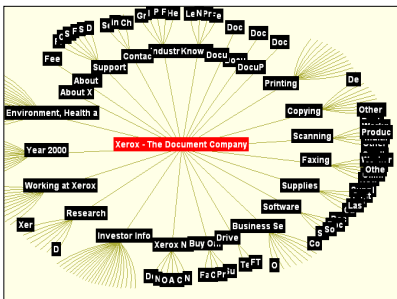
- Filtering
- Scrolling or Panning
- Zooming
- Aggregation
- Focus+Context

64

MC Escher, *Circle Limit IV*

65

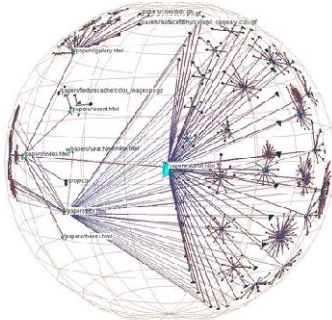
## HYPERBOLIC LAYOUT



Perform tree layout in hyperbolic space, then project the result on to the Euclidean plane

Why? Like tree breadth, the hyperbolic plane expands exponentially!

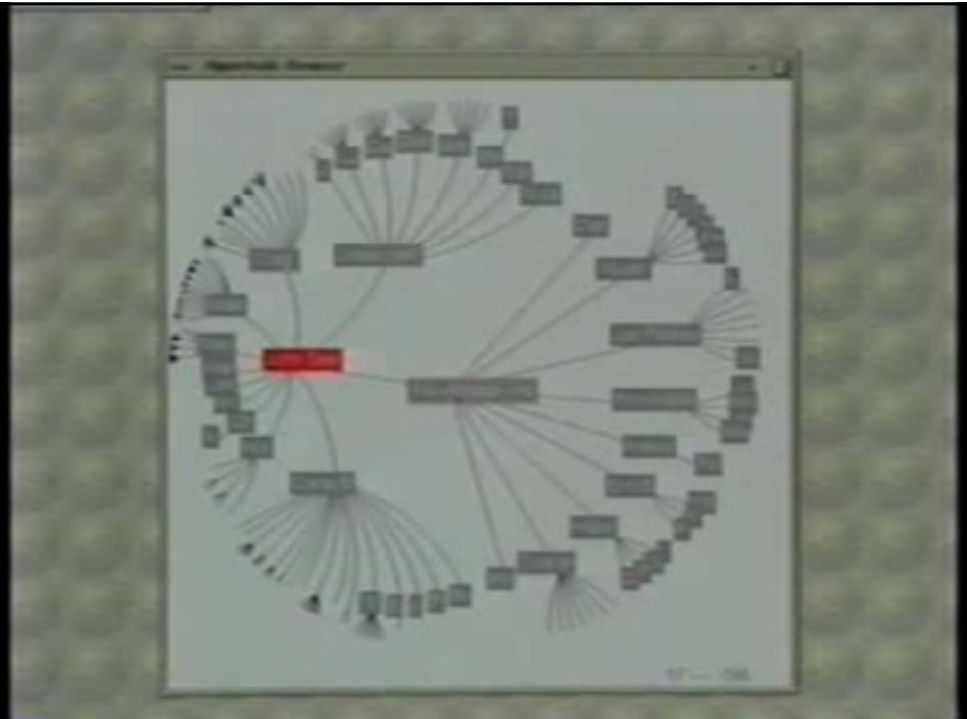
Also computable in 3D, projected into a sphere



66

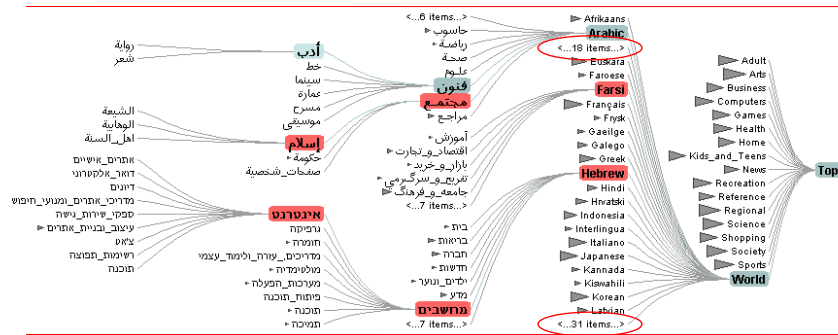


**HYPERBOLIC LAYOUT** [Rao 1995]



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**DEGREE OF INTEREST TREES**

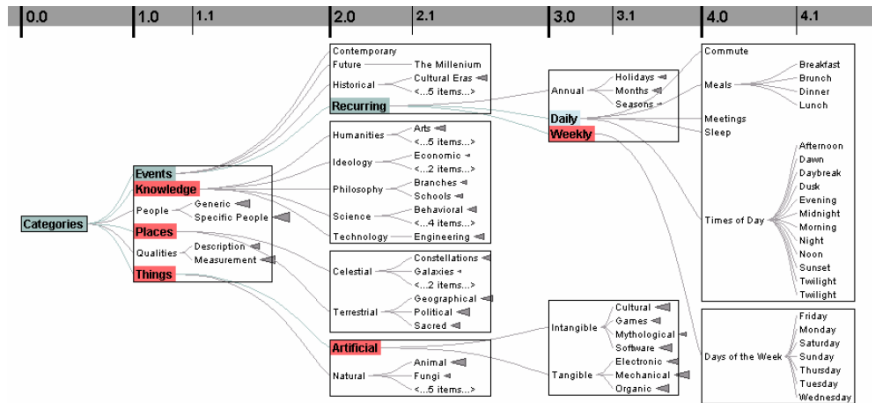


Space-constrained, multi-focal tree layout

<https://www.youtube.com/watch?v=RTQ0N4QY0yc>

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## DEGREE OF INTEREST TREES



Cull “low interest” nodes on a given depth level until all blocks in level fit within bounds  
 Attempt to center child blocks under parents

<https://www.youtube.com/watch?v=RT00N4OY0yc>

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## INDENTATION & NODE-LINK DIAGRAMS

Encode structure in **2D space** (breadth/depth)

### Benefits

Clearly depicts node relationships / structure

Structure-based or browsing tasks

### Problems

Even with tidy layout, quickly run out of space

### Missing

Attribute-based encodings

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# ENCLOSURE

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## ENCLOSURE DIAGRAMS



Encode structure using **spatial enclosure**  
Popularly known as **treemaps**

### Benefits

Provides a single view of an entire tree  
Easier to spot large/small nodes

### Problems

Difficult to accurately read structure/depth

72

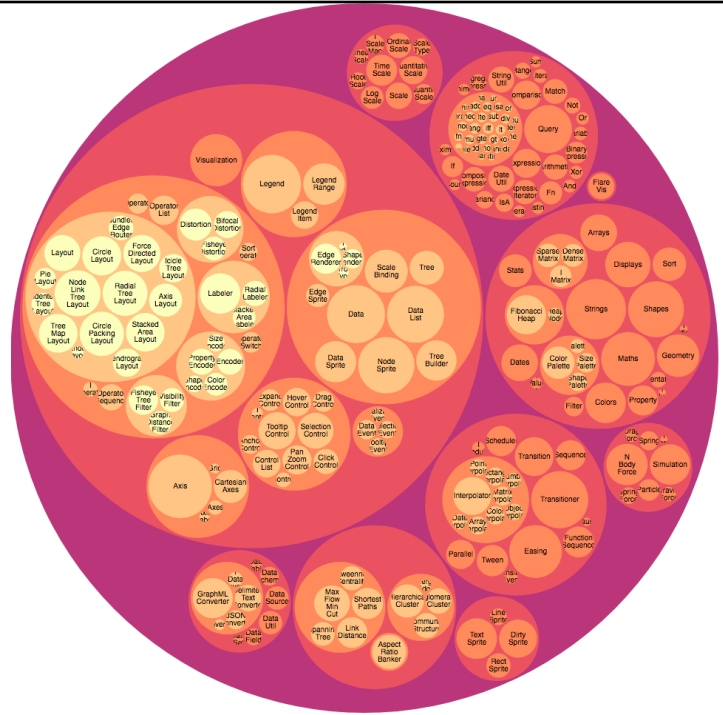
# CIRCLE PACKING LAYOUT

Nodes represented as sized circles

Nesting to show parent-child relationships

## Problems?

- Inefficient use of space
- Parent size misleading?



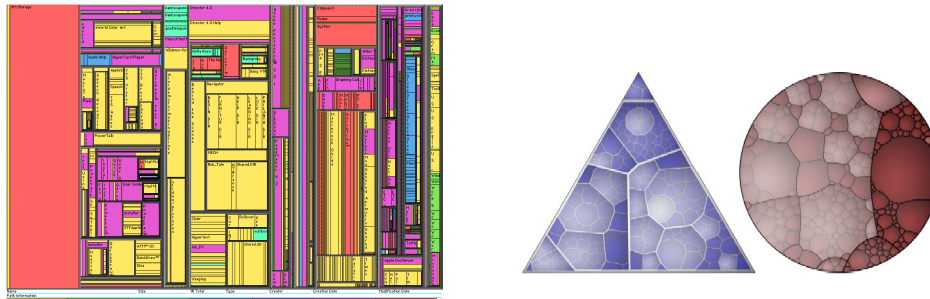
73

# TREEMAPS

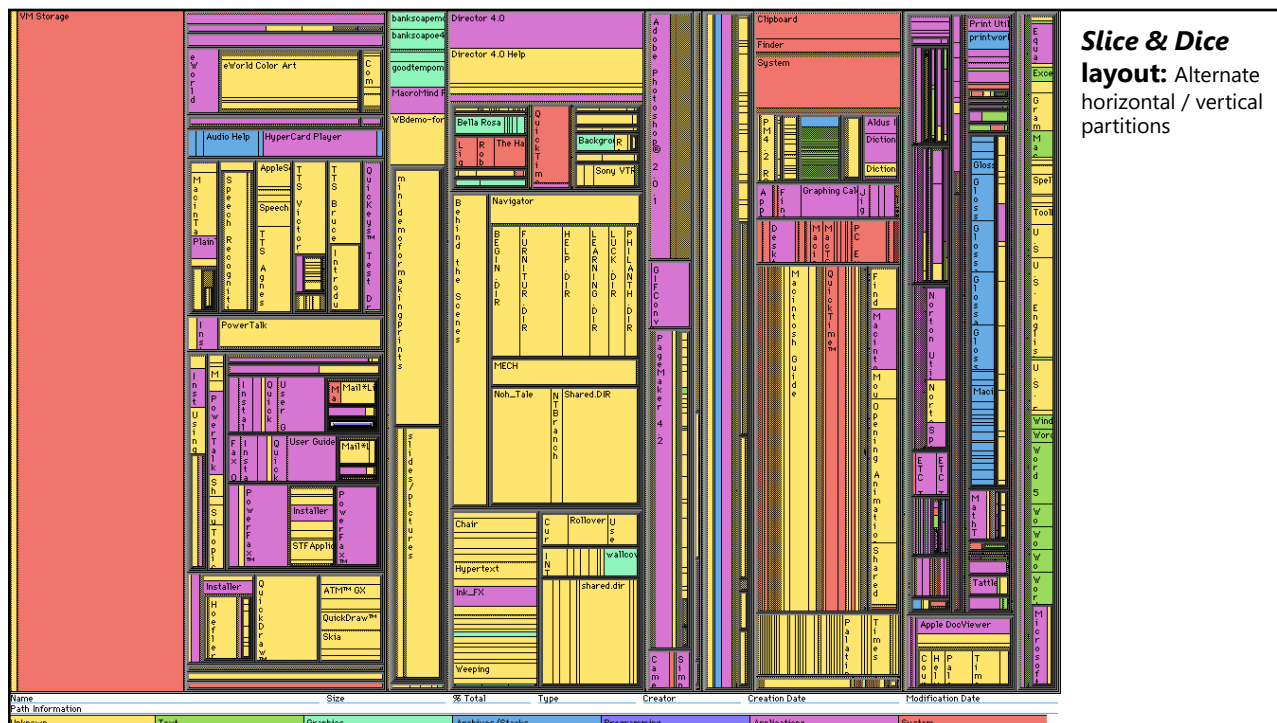
Hierarchy visualization that emphasizes values of nodes via area encoding

Partition 2D space such that leaf nodes have sizes proportional to data values

First algorithms designed to show file sizes on a hard drive [Shneiderman 1990]



75



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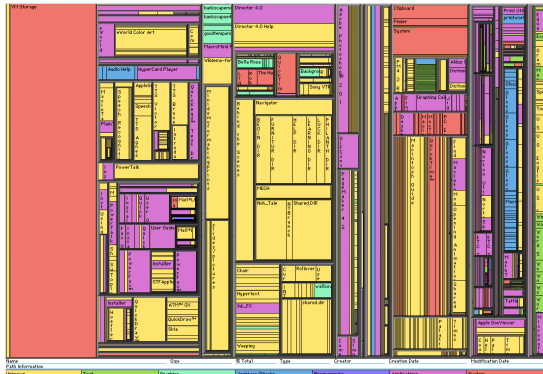


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# SQUARIFIED TREEMAPS [Bruls 2000]

*Slice & Dice* layout suffers from extreme aspect ratios. How might we do better?

*Squarified* layout: greedy optimization with objective of square rectangles. Slice/dice within siblings; alternate whenever ratio worsens



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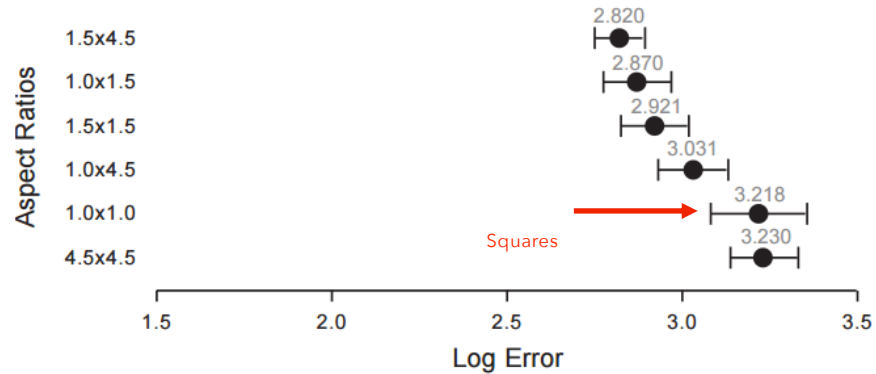
## WHY SQUARES?

### Posited Benefits of 1:1 Aspect Ratios

1. Minimize perimeter, reducing border ink  
*Mathematically true!*
2. Easier to select with a mouse cursor.  
*Validated by empirical research & Fitt's Law!*
3. Similar aspect ratios are easier to compare.  
*Seems intuitive, but is this true?*

79

## COMPARISON: ERROR VS. ASPECT RATIO



### Study by Kong et al. 2010

Comparison of squares has higher error! Comparison of extreme ratios even worse  
Perhaps squarify works well because it fails to meet its objective?

80

## WHY SQUARES?

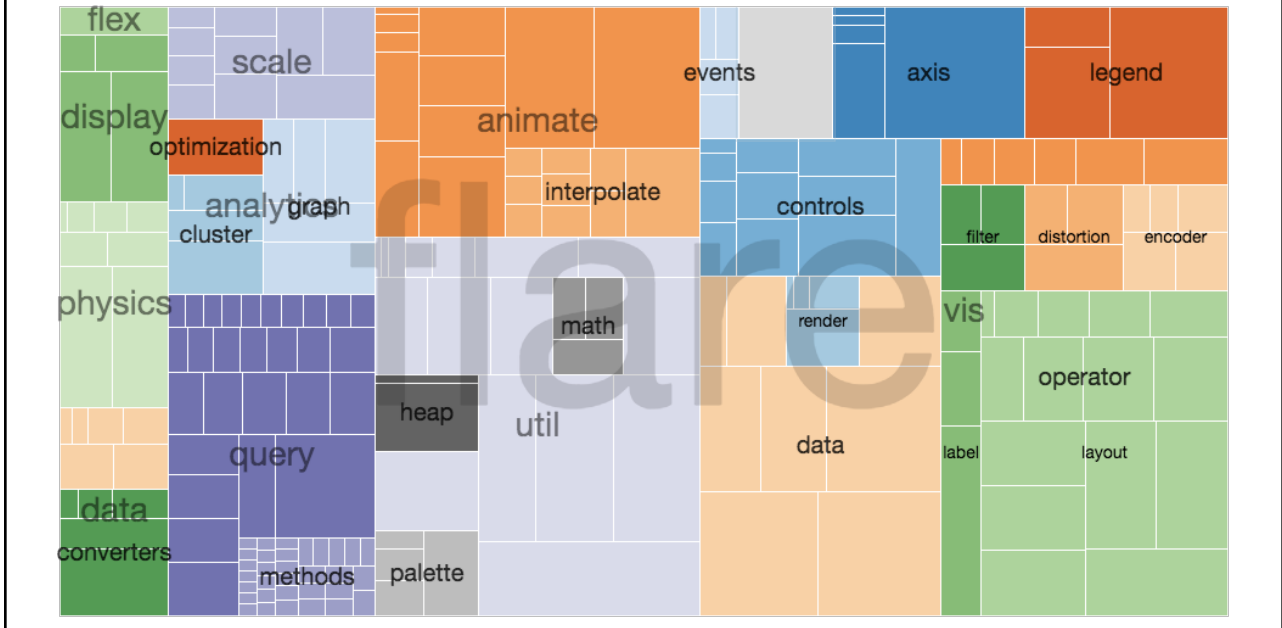
### Posited Benefits of 1:1 Aspect Ratios

1. Minimize perimeter, reducing border ink  
*Mathematically true!*
2. Easier to select with a mouse cursor.  
*Validated by empirical research & Fitt's Law!*
3. Similar aspect ratios are easier to compare.  
~~*Seems intuitive, but is this true?*~~  
*Extreme ratios & squares-only more inaccurate.*  
*Balanced ratios better? Target golden ratio?*

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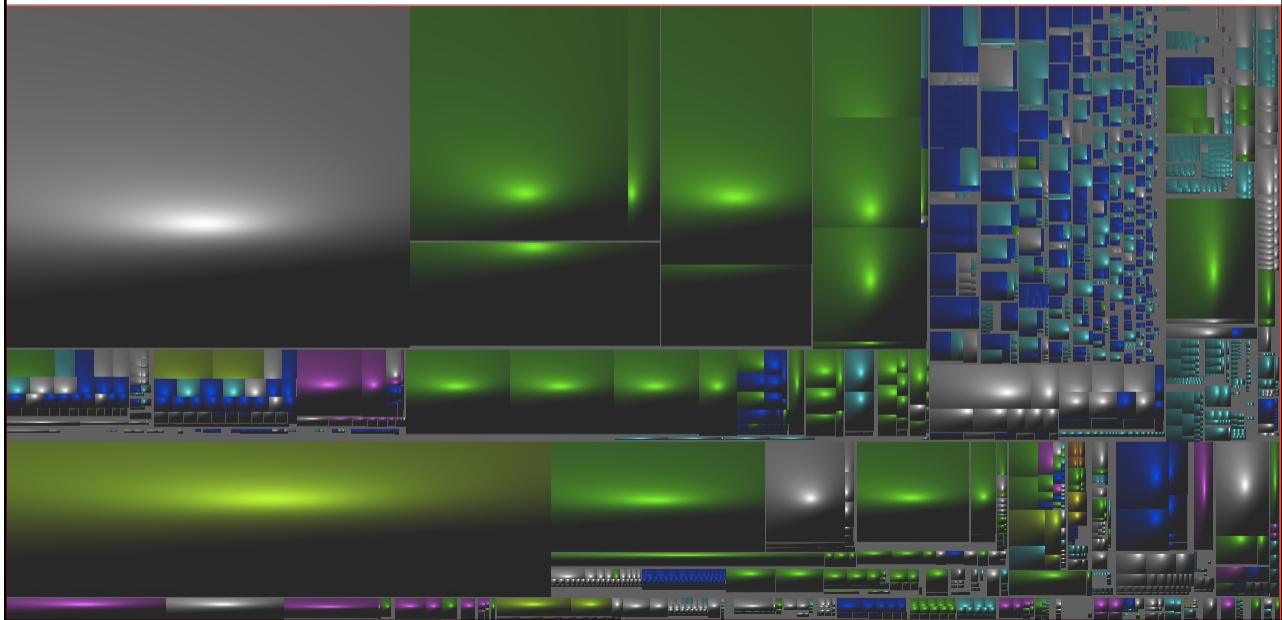
# INTERACTIVE EXAMPLE

<https://vega.github.io/vega/examples/treemap/>



82

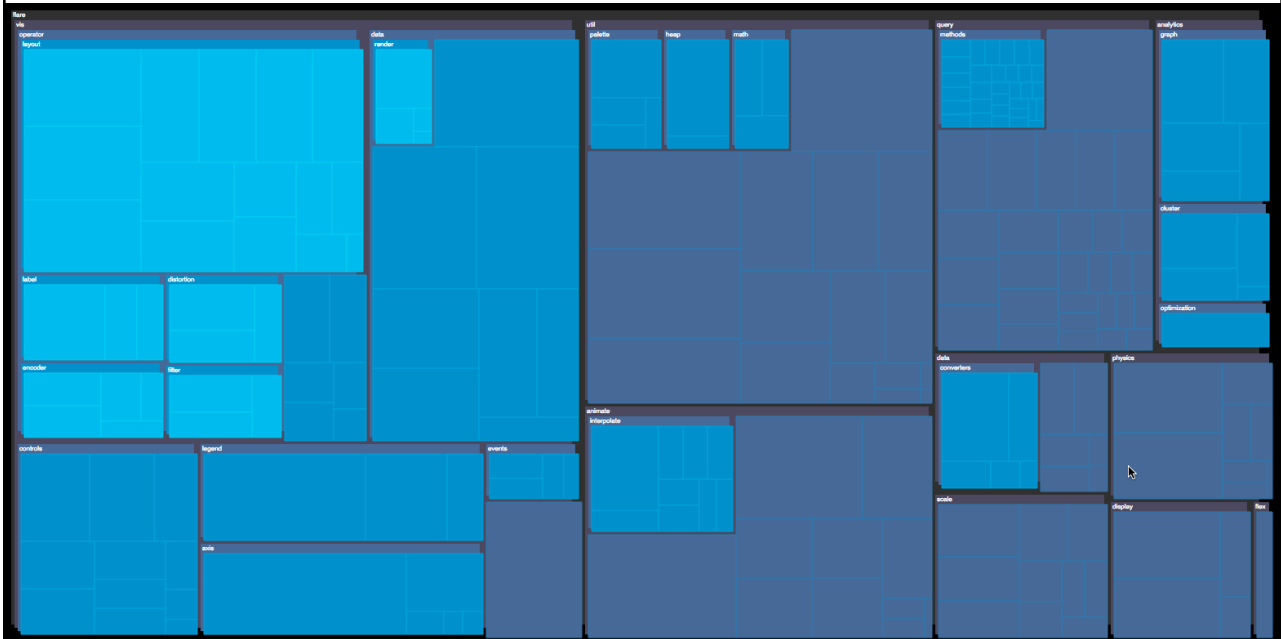
# CUSHION TREEMAPS [van Wijk 1999]



85



## CASCADED TREEMAPS [Lü 2008]

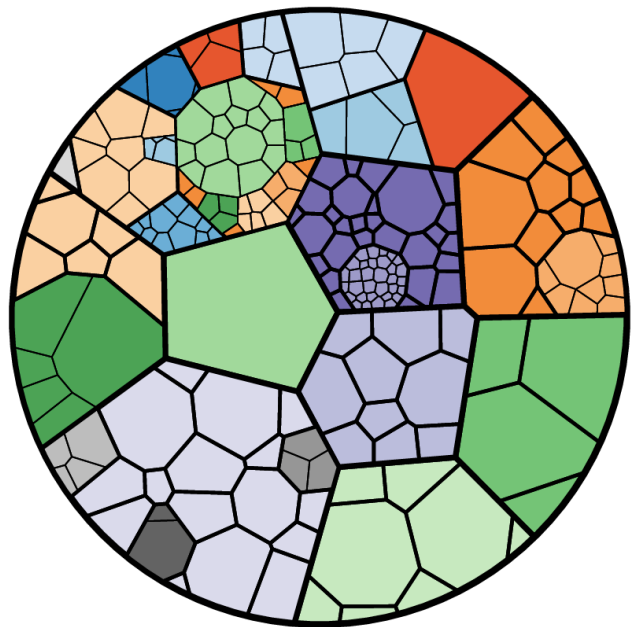


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## VORONOI TREEMAPS [Balzer 2005]

Treemaps with arbitrary polygonal shapes and boundary

Uses iterative, weighted Voronoi tessellations to generate cells with value-proportional areas



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# LAYERING

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## LAYERED DIAGRAMS



### Signify tree structure using

- Layering
- Adjacency
- Alignment

### Involves recursive sub-division of space

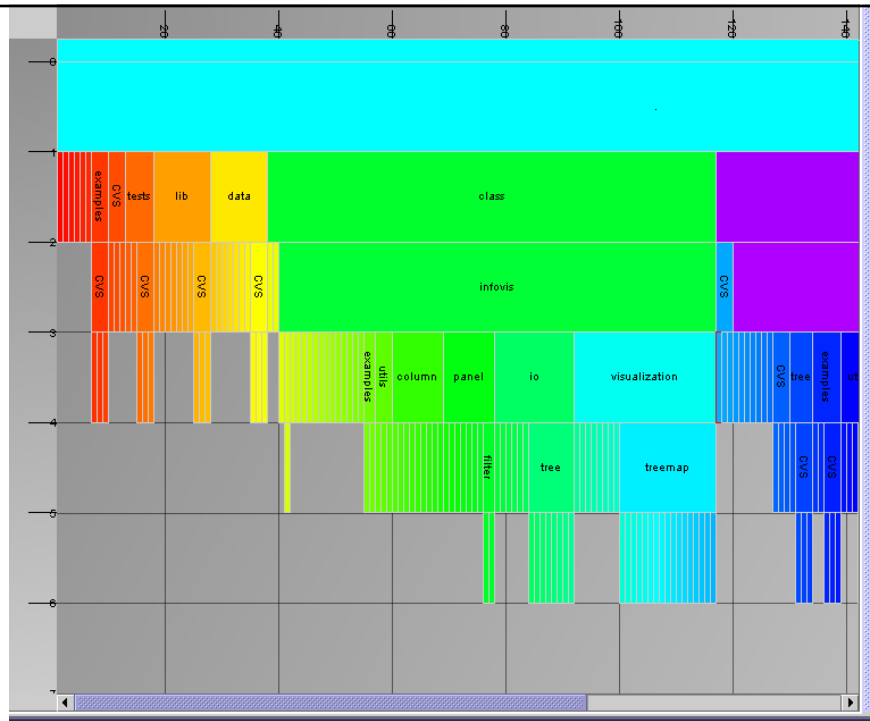
Leaf nodes may be sized by value, parent size visualizes sum of descendant leaf values

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# ICICLE TREES

Parent nodes get a larger layer area, (e.g. horizontal extent)

Child levels are layered, constrained to parent's extent

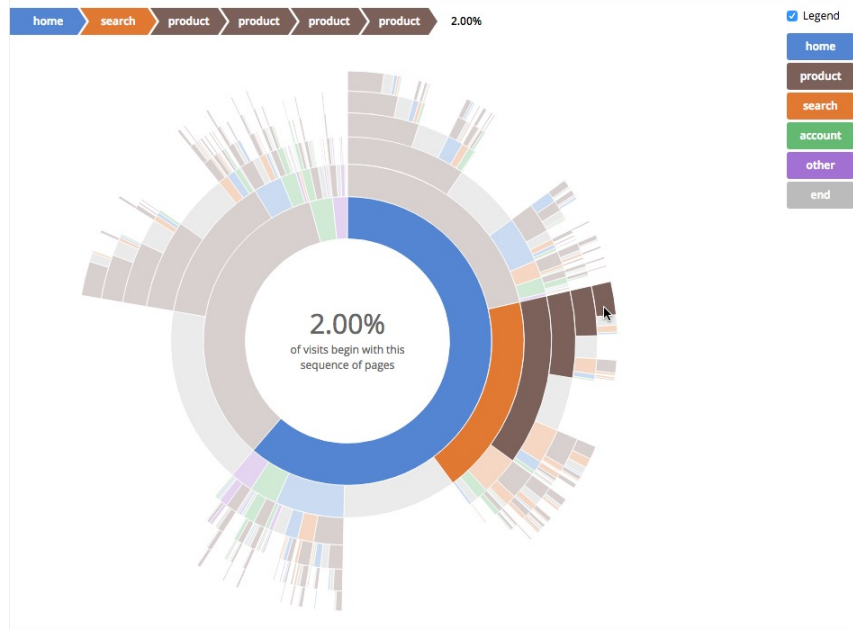


91

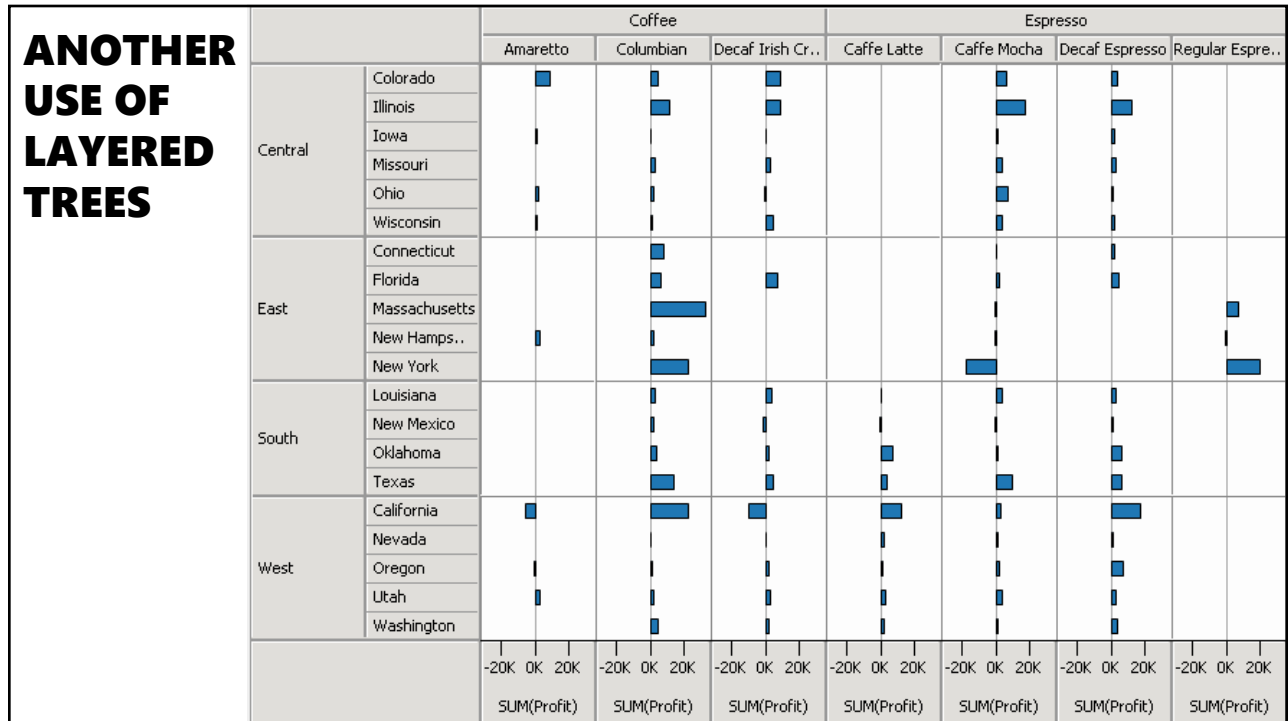
# SUNBURST TREES

Parent nodes get a larger layer area, (e.g. angular extent)

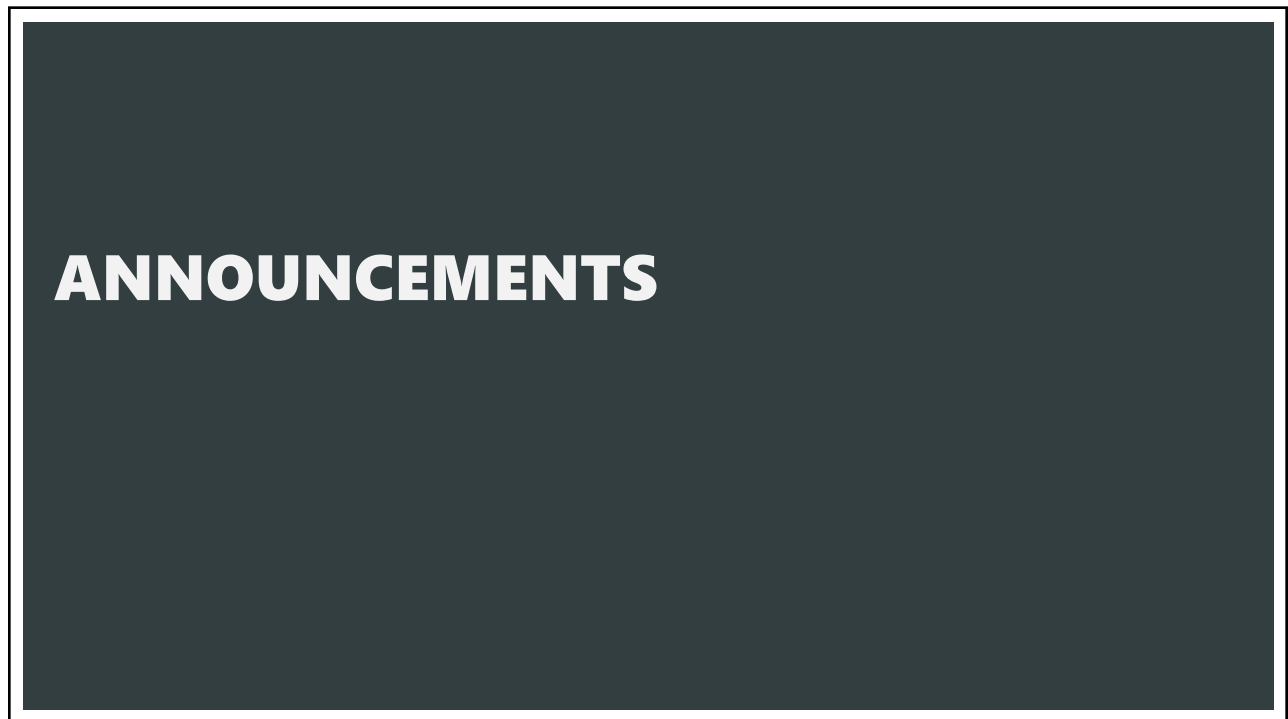
Child levels are layered, constrained to parent's extent



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# FINAL PROJECT

## Design Review Nov 27 and 29

### Data analysis/explainer

Analyze dataset in depth & make a visual explainer

### Deliverables

An article with multiple different interactive visualizations  
Short video (2 min) demoing and explaining the project

### Schedule

Project proposal: Mon 11/6

Design Review and Feedback: 9<sup>th</sup> week of quarter, 11/27 and 11/29

Final code and video: Sun 12/10 8pm

### Grading

Groups of up to 3 people, graded individually  
Clearly report responsibilities of each member

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# FINAL PROJECT GUIDELINES

## Consider the audience

Your visual explainer should be of interest to a group of people beyond your immediate circle (an explainer about your own Spotify data unlikely be of interest to others you don't know)

## Pick relatively less explored topics/datasets

Do some research on what has already been done for the topic/dataset(s)

Certain data like songs (e.g. Spotify) or movies (e.g. IMDB) are already well analyzed and should be avoided, unless you want to try to take a very different angle or use innovative analysis methods

## Develop a narrative

In the early stages of the analysis process, try to uncover patterns to help you form and shape a narrative through-line for the explainer

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# FINAL PROJECT GUIDELINES

## Design visualization interactions

Choose base visualizations that can support a high level of interactivity  
Bubble charts, tree maps, and word clouds typically aren't the most effective choices

Design interactive features that would enable viewers to interact with the data in a way that strengthens your narrative

Tooltip is typically not enough interaction

Draw inspiration from sites like the New York Times and the Pudding

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# NODE-LINK GRAPH LAYOUT

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## **NODE-LINK GRAPH VISUALIZATION**

Nodes connected by lines/curves

**Sugiyama-Style Layout** - arranged by depth

**Force-Directed Layout** - physical simulation

**Attribute-Driven Layout** - arranged by value

**Constraint-Based Layout** – optimization

**Arc Diagrams** - aligned layout

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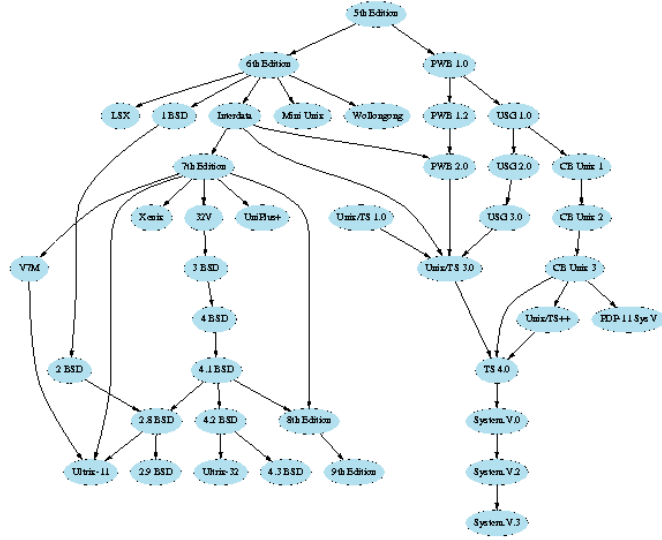
## **SUGIYAMA-STYLE LAYOUT**

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# SUGIYAMA-STYLE GRAPH LAYOUT

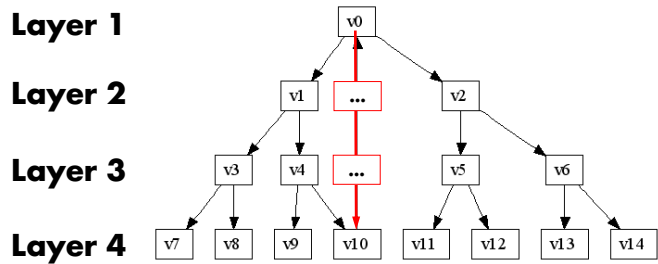
Evolution of the UNIX operating system

Hierarchical layering based on descent



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# SUGIYAMA-STYLE GRAPH LAYOUT

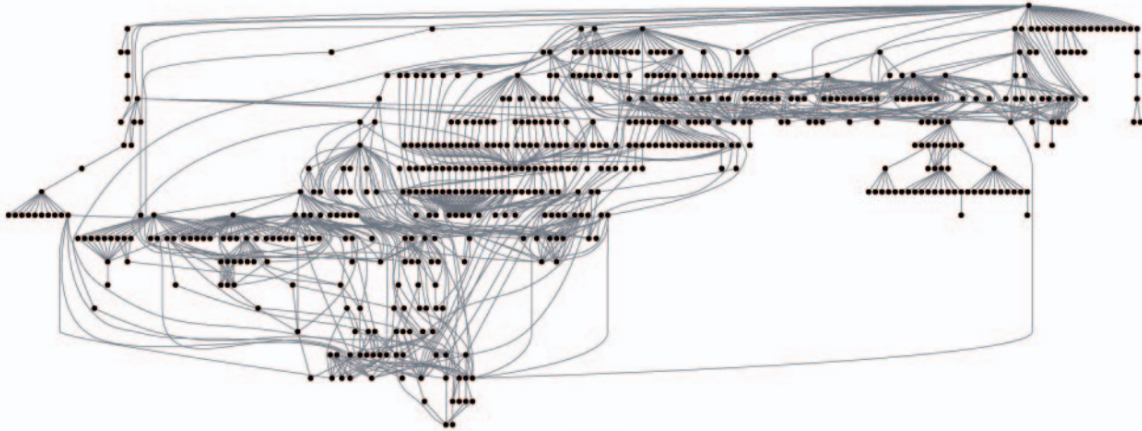


- Reverse some edges to remove cycles
- Assign nodes to hierarchy layers → Longest path layering
  - Create dummy nodes to “fill in” missing layers
- Arrange nodes within layer, minimize edge crossings
  - Route edges – layout splines if needed

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## PRODUCES HIERARCHICAL LAYOUT



### **Sugiyama-style layout emphasizes hierarchy**

However, cycles in the graph may not be as apparent, and hierarchy may mislead  
Long edges can impede perception of proximity