

# Network Layout

*Maneesh Agrawala*

**CS 448B: Visualization  
Fall 2021**

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## Reading Response Questions/Thoughts

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For the final project, do you have a recommendation of a place to go to view other data visualization research papers that conducted user studies?

As animations contain more and more data, is it possible that we can overload or overstimulate the user? Can animations be harmful by being too distracting? If so, how can we safeguard our designs to make sure they don't cause this overstimulation?

Is there a more formal or mathematical rule set governing which colors to use to highlight information, and which to contrast? Or is it mostly a combination of multiple factors that you need to see to know? In a similar vein, do colors need to be different in shade as well as color for black and white printing? How do we know to vary transparency with color or just color?

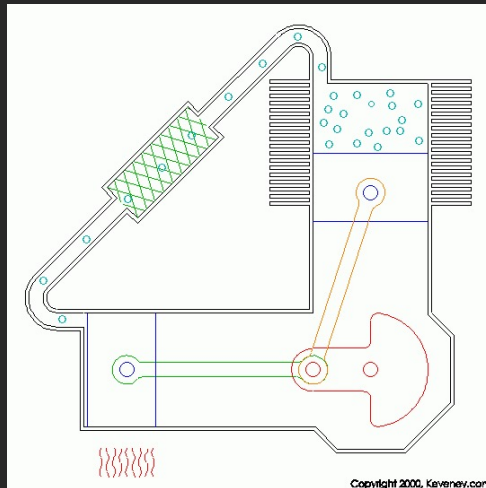
How seriously should we take self-reported stated preferences when evaluating the strength of a visualization? How much should we weight user's expressed preference relative to usability, learning, and recall data when evaluating the efficacy of a visualization?

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## Last Time: Animation Understanding Motion

3

## How does it work?



Two-cylinder Stirling engine

<http://www.keveney.com/Vstirling.html>

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# Problems [Tversky 02]

## Difficulties in understanding animation

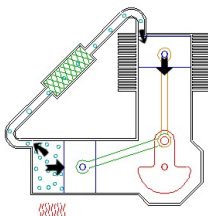
- Difficult to estimate paths and trajectories
- Motion is fleeting and transient
- Cannot simultaneously attend to multiple motions
- Trying to parse motion into events, actions and behaviors
- Misunderstanding and wrongly inferring causality
- Anthropomorphizing physical motion may cause confusion or lead to incorrect conclusions

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## Solution I: Break into static steps

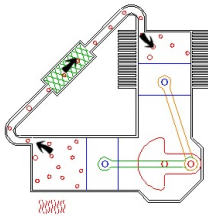
1

**Expansion.** At this point, most of the gas in the system has just been driven into the hot cylinder. The gas heats and expands driving both pistons inward.



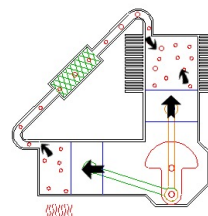
2

**Transfer.** At this point, the gas has expanded (about 3 times in this example). Most of the gas (about 2/3rds) is still located in the hot cylinder. Flywheel momentum carries the crankshaft the next 90 degrees, transferring the bulk of the gas to the cool cylinder.



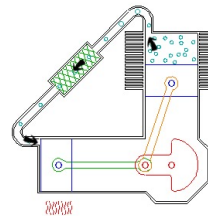
3

**Contraction.** Now the majority of the expanded gas has been shifted to the cool cylinder. It cools and contracts, drawing both pistons outward.



4

**Transfer.** The now contracted gas is still located in the cool cylinder. Flywheel momentum carries the crank another 90 degrees, transferring the gas to back to the hot cylinder to complete the cycle.



Two-cylinder Stirling engine

<http://www.keveney.com/Vstirling.html>

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# Challenges

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## Choosing the set of steps

- How to segment process into steps?
- Note: Steps often shown sequentially for clarity, rather than showing everything simultaneously

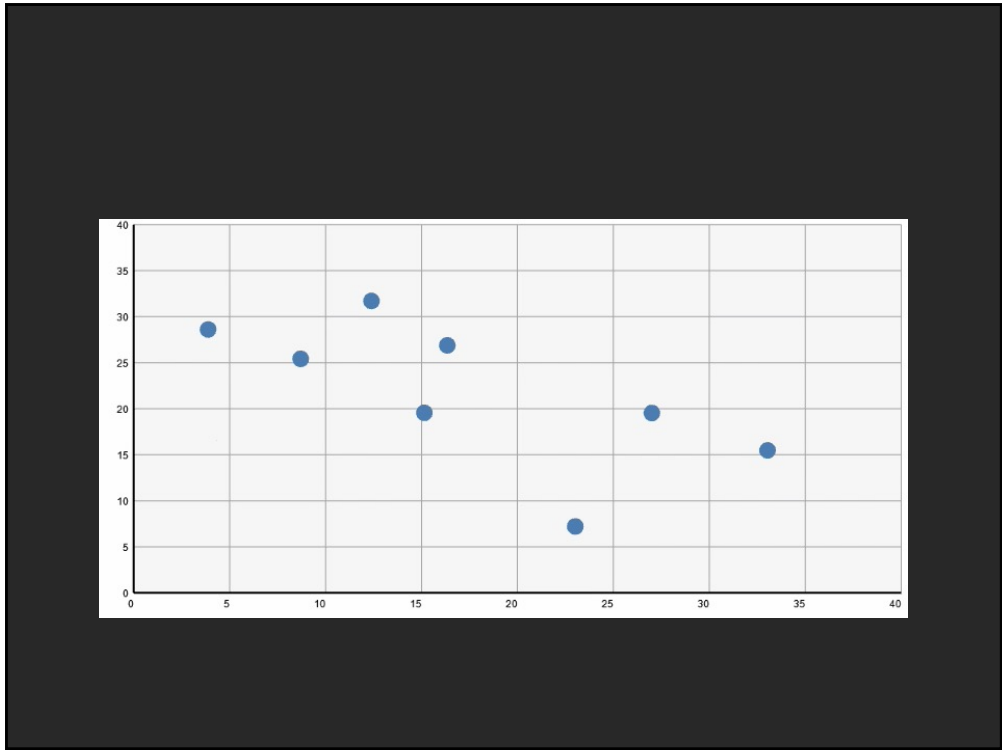
## Tversky suggests

- Coarse level – segment based on objects
- Finer level – segment based on actions
  - Static depictions often do not show finer level segmentation

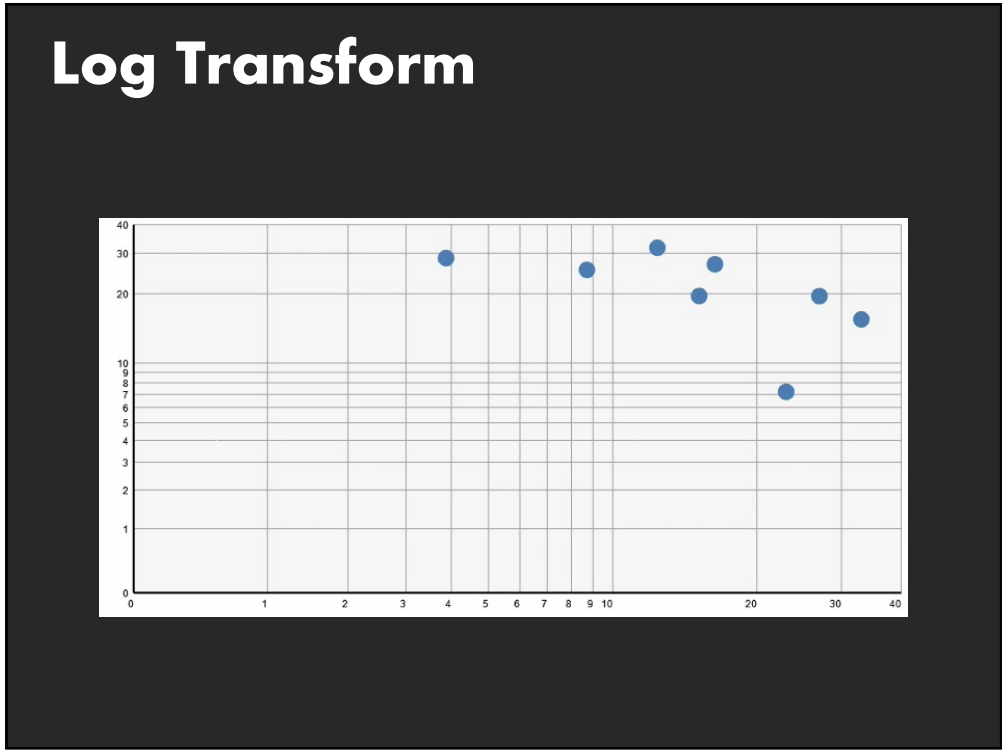
7

# Animated Transitions in Statistical Graphics

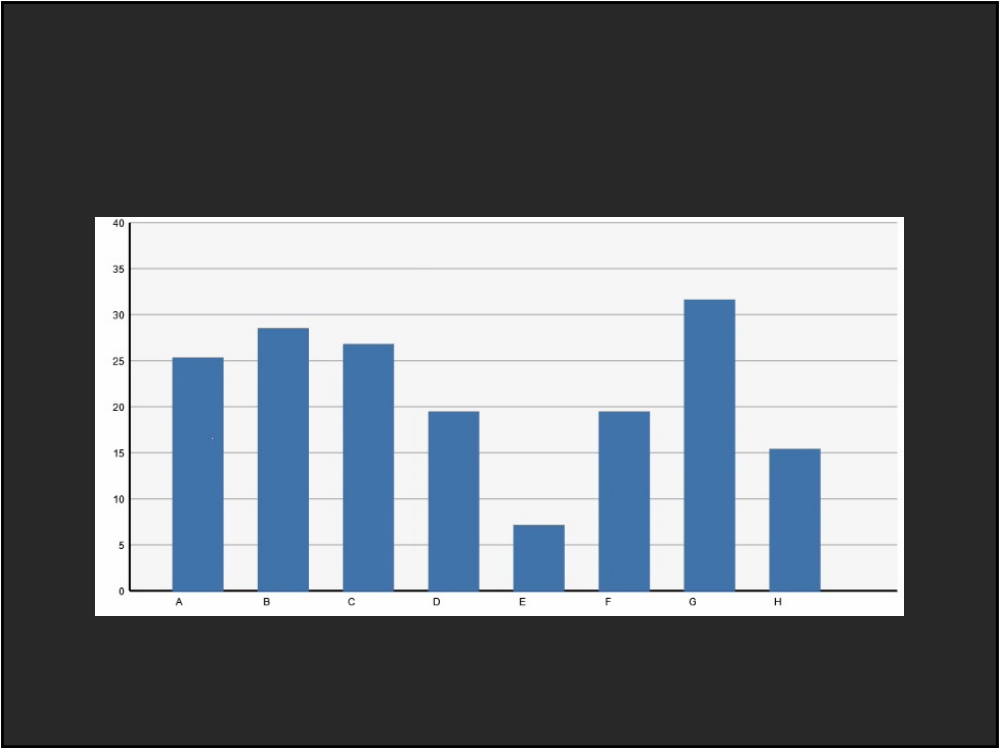
8



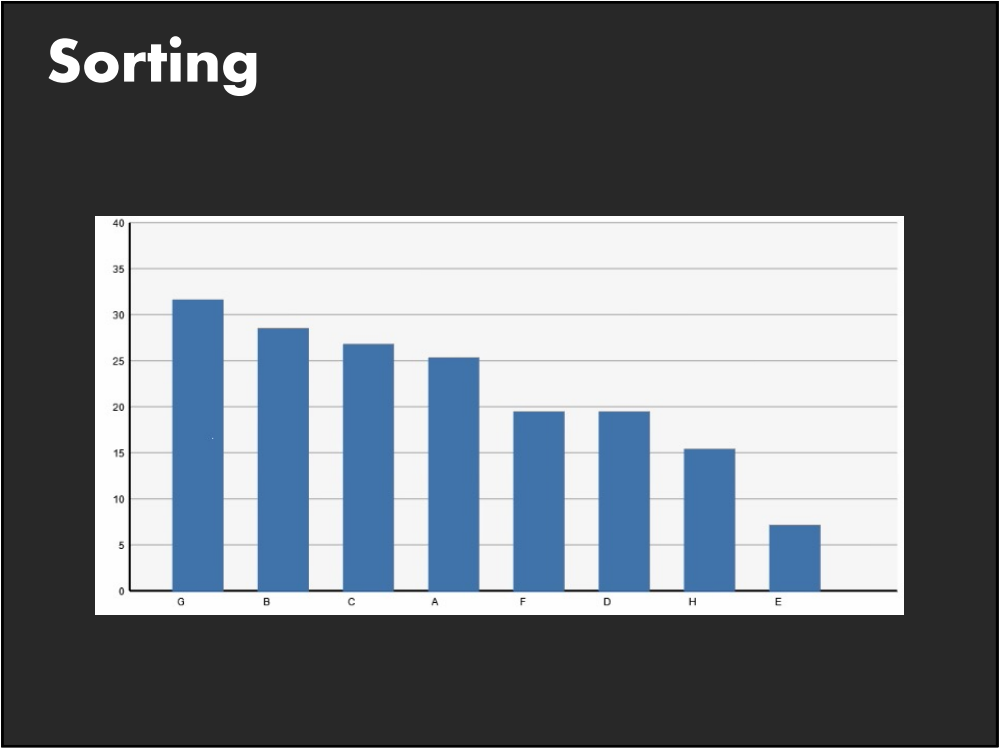
9



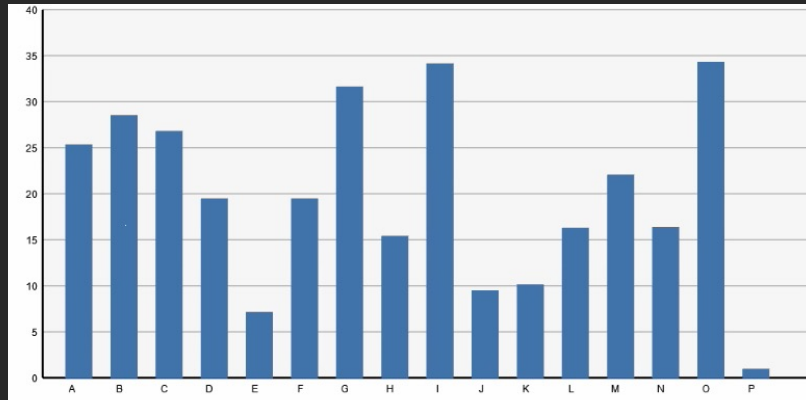
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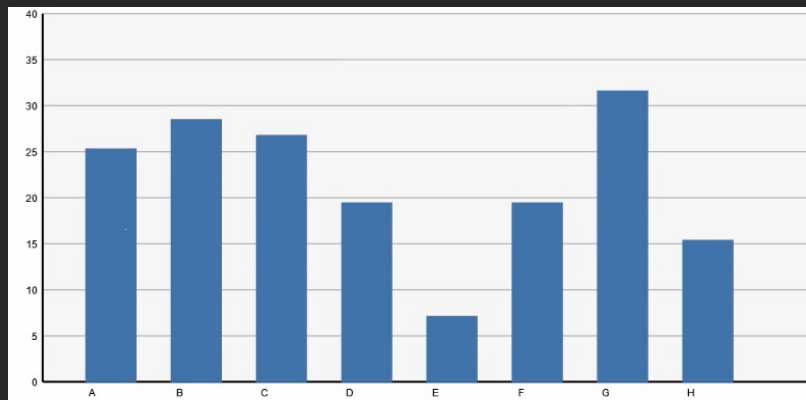


12

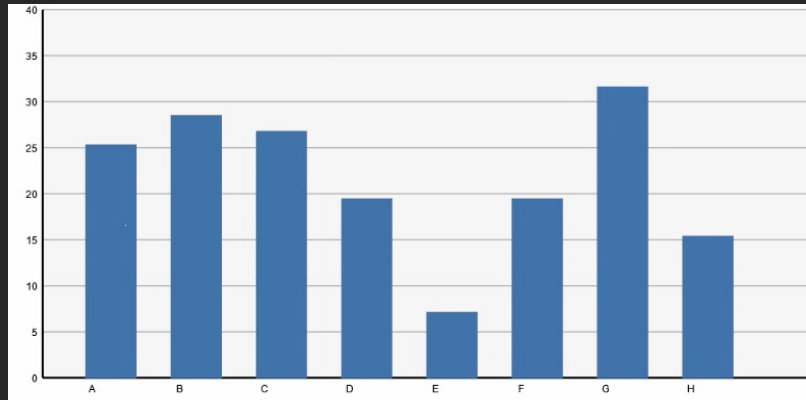


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## Filtering

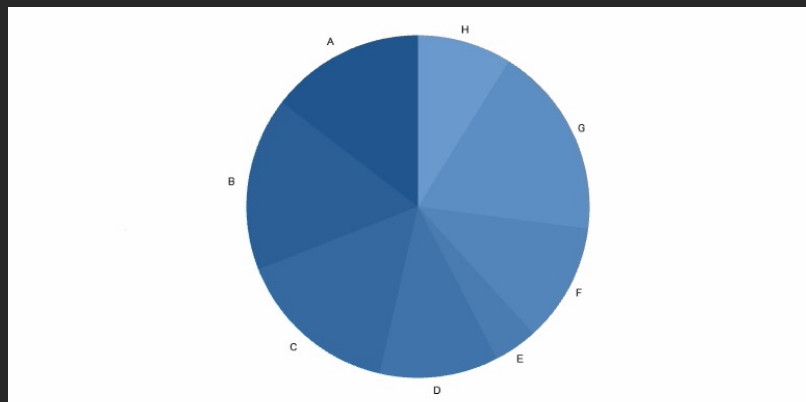


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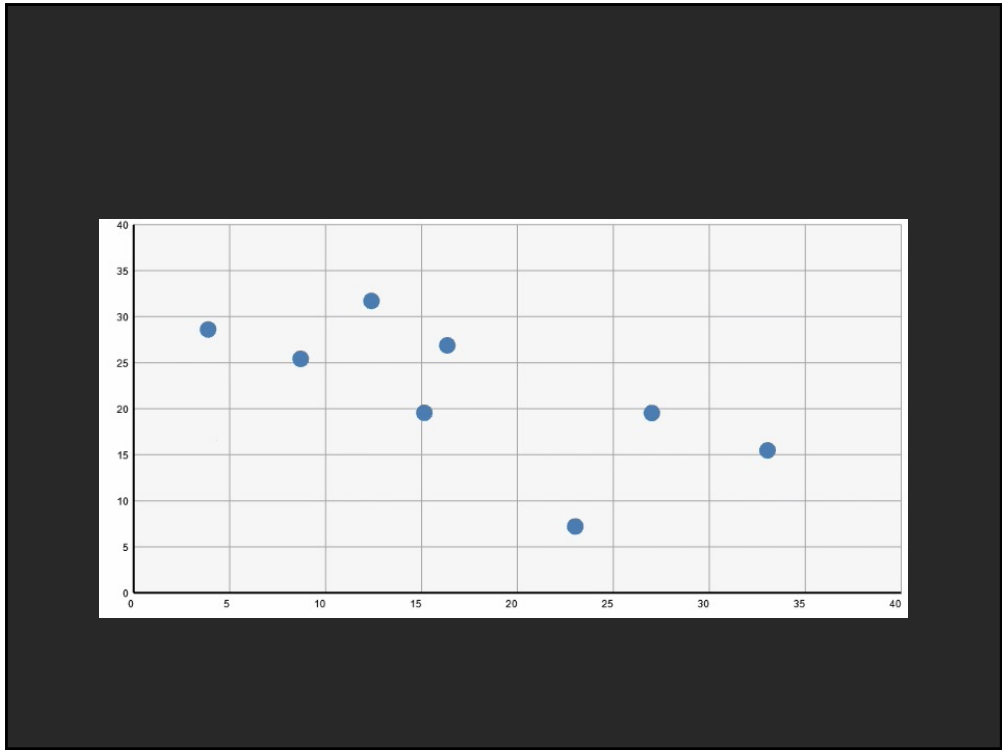
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## Change Encodings

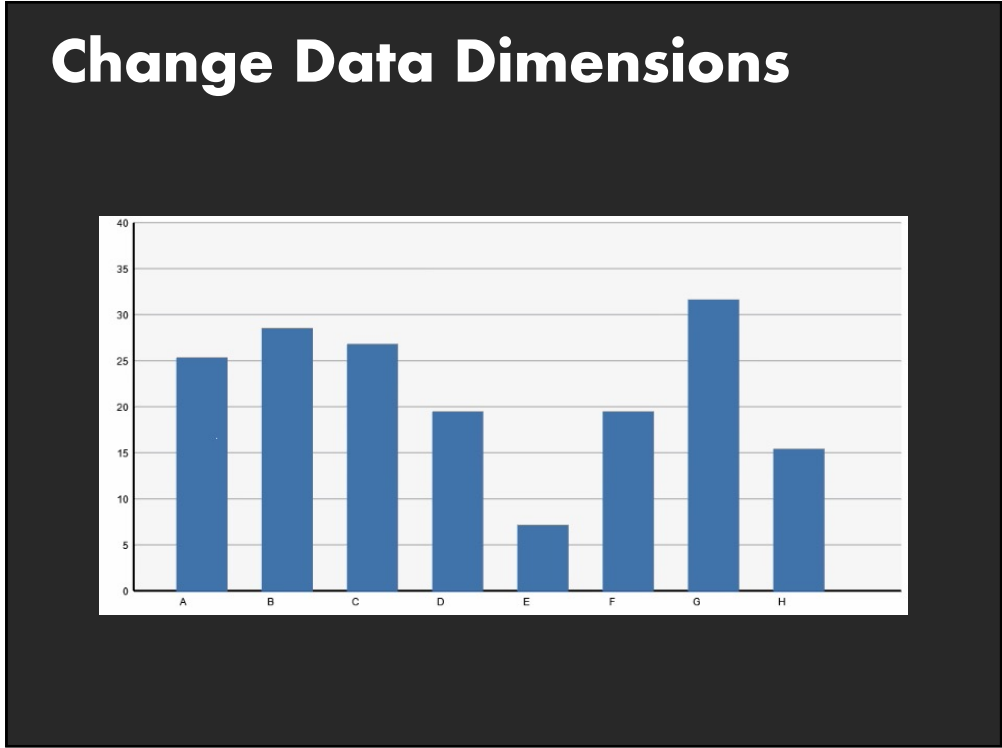


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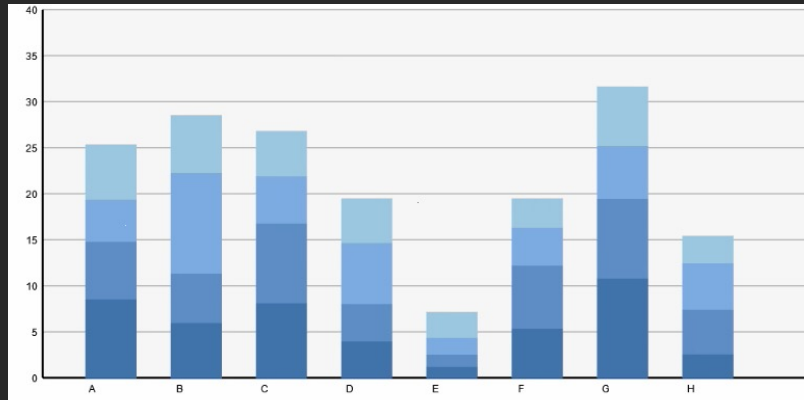


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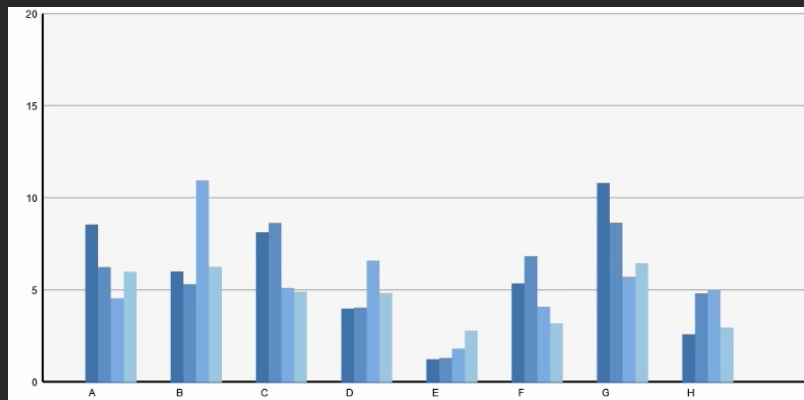
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## Change Data + Encodings



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## Change Encodings + Axis Scales

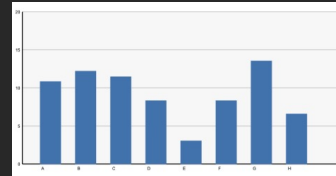


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# Data Graphics & Transitions

Category	Sales	Profit
A	11	7
B	13	10
C	12	6
D	8	5
E	3	1

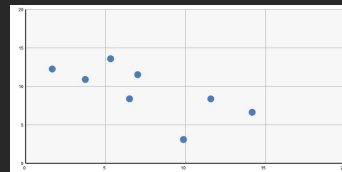
Visual Encoding



Change selected data dimensions or encodings

Animation to communicate changes?

Category	Sales	Profit
A	11	7
B	13	10
C	12	6
D	8	5
E	3	1



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## Animated Transitions in Statistical Data Graphics

Jeffrey Heer  
George G. Robertson

Microsoft  
**Research**

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## Study Conclusions

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Appropriate animation improves graphical perception

Use simple staged transitions, *but* doing one thing at a time  
not always best

Axis re-scaling hampers perception

Avoid if possible (use common scale)

Maintain landmarks better (delay fade out of gridlines)

Subjects preferred animated transitions

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## Implementing Animation

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# Animation Approaches

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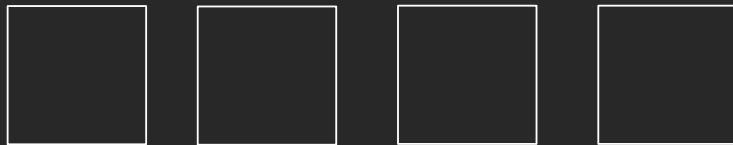
## Frame-based Animation

Redraw scene at regular interval (e.g., 16ms)  
Developer defines the redraw function

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# Frame-based Animation

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1

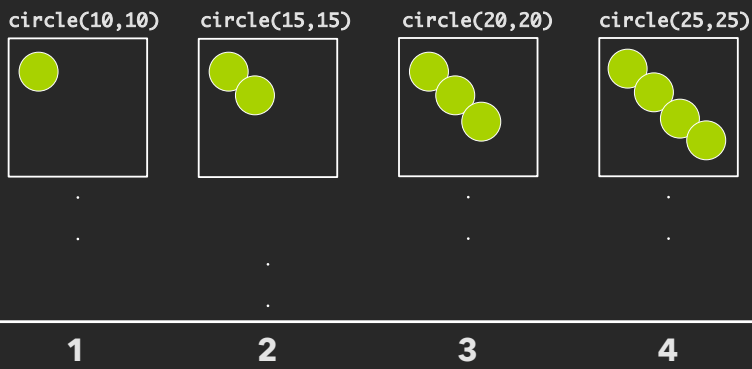
2

3

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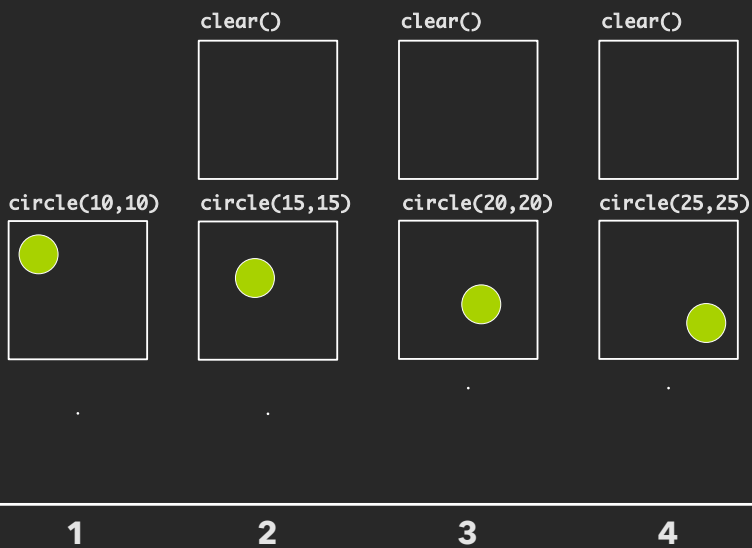
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# Frame-based Animation



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# Frame-based Animation



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# Animation Approaches

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Redraw scene at regular interval (e.g., 16ms)  
Developer defines the redraw function

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# Animation Approaches

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## Frame-based Animation

Redraw scene at regular interval (e.g., 16ms)  
Developer defines the redraw function

## Transition-based Animation (Hudson & Stasko '93)

Specify property value, duration & easing (tweening)  
Typically computed via interpolation

$$\text{step}(fraction) \{ x_{now} = x_{start} + fraction * (x_{end} - x_{start}); \}$$

Timing & redraw managed by UI toolkit

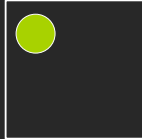
47

# Transition-based Animation

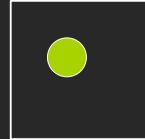
from: (10,10) to: (25,25) duration: 3sec

$$dx=25-10$$

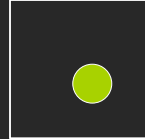
$$x=10+(t/3)*dx$$



$$x=10+(t/3)*dx$$



$$x=10+(t/3)*dx$$



$$x=10+(t/3)*dx$$



0s

1s

2s

3s

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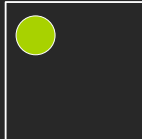
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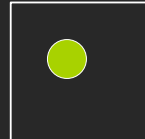
*Toolkit handles frame-by-frame updates*

$$dx=25-10$$

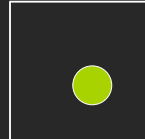
$$x=10+(t/3)*dx$$



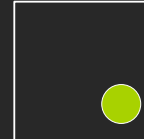
$$x=10+(t/3)*dx$$



$$x=10+(t/3)*dx$$



$$x=10+(t/3)*dx$$



0s

1s

2s

3s

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## D3 Transitions

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Any *d3 selection* can be used to drive animation.

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## D3 Transitions

---

Any *d3 selection* can be used to drive animation.

```
// Select SVG rectangles and bind them to data values  
var bars = svg.selectAll("rect.bars").data(values);
```

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## D3 Transitions

---

Any *d3 selection* can be used to drive animation.

```
// Select SVG rectangles and bind them to data values.  
var bars = svg.selectAll("rect.bars").data(values);  
  
// Static transition: update position and color of bars.  
bars  
  .attr("x", (d) => xScale(d.foo))  
  .attr("y", (d) => yScale(d.bar))  
  .style("fill", (d) => colorScale(d.baz));
```

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## D3 Transitions

---

Any *d3 selection* can be used to drive animation.

```
// Select SVG rectangles and bind them to data values.  
var bars = svg.selectAll("rect.bars").data(values);  
  
// Animated transition: interpolate to target values using default timing  
bars.transition()  
  .attr("x", (d) => xScale(d.foo))  
  .attr("y", (d) => yScale(d.bar))  
  .style("fill", (d) => colorScale(d.baz));
```

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## D3 Transitions

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Any d3 *selection* can be used to drive animation.

```
// Select SVG rectangles and bind them to data values.
var bars = svg.selectAll("rect.bars").data(values);

// Animated transition: interpolate to target values using default timing
bars.transition()
  .attr("x", (d) => xScale(d.foo))
  .attr("y", (d) => yScale(d.bar))
  .style("fill", (d) => colorScale(d.baz));

// Animation is implicitly queued to run!
```

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## D3 Transitions, Continued

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```
bars.transition()
  .duration(500)           // animation duration in ms
  .delay(0)                // onset delay in ms
  .ease(d3.easeBounce)    // set easing (or "pacing") style
  .attr("x", (d) => xScale(d.foo))
  ...
```

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## D3 Transitions, Continued

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```
bars.transition()
  .duration(500)           // animation duration in ms
  .delay(0)                // onset delay in ms
  .ease(d3.easeBounce)    // set easing (or "pacing") style
  .attr("x", (d) => xScale(d.foo))
  ...

bars.exit().transition() // animate elements leaving display
  .style("opacity", 0)   // fade out to fully transparent
  .remove();             // remove from DOM upon completion
```

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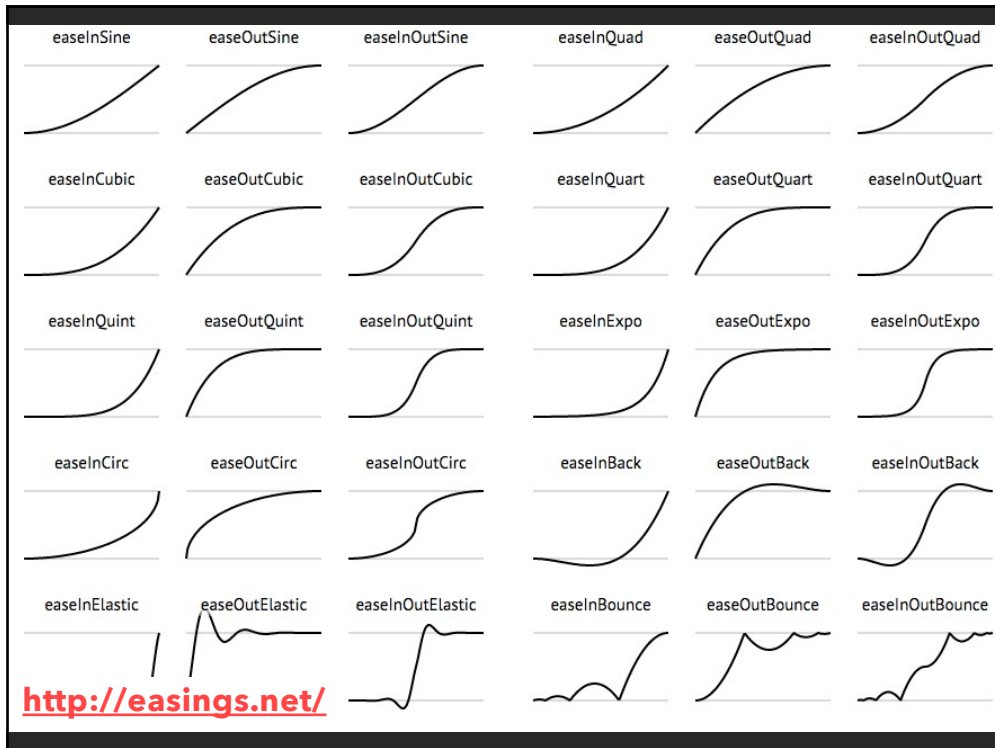
## Easing Functions

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Goals: stylize animation, improve perception.

Basic idea is to warp time: as *duration* goes from start (0%) to end (100%), dynamically adjust the *interpolation fraction* using an easing function.

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## Summary

Animation is a salient visual phenomenon  
 Attention, object constancy, causality, timing

For processes, step-by-step static images may be preferable  
 For transitions, animation has some benefits, but consider  
 task and timing

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# Announcements

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## Final project

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### Data analysis/explainer or conduct research

- **Data analysis:** Analyze dataset in depth & make a visual explainer
- **Research:** Pose problem, Implement creative solution

### Deliverables

- **Data analysis/explainer:** Article with multiple different interactive visualizations
- **Research:** Implementation of solution and web-based demo if possible
- **Short video (2 min)** demoing and explaining the project

### Schedule

- Project proposal: **Wed 11/3**
- Design Review and Feedback: **10<sup>th</sup> week of quarter**
- Final code and video: **Fri 12/10 11:59pm**

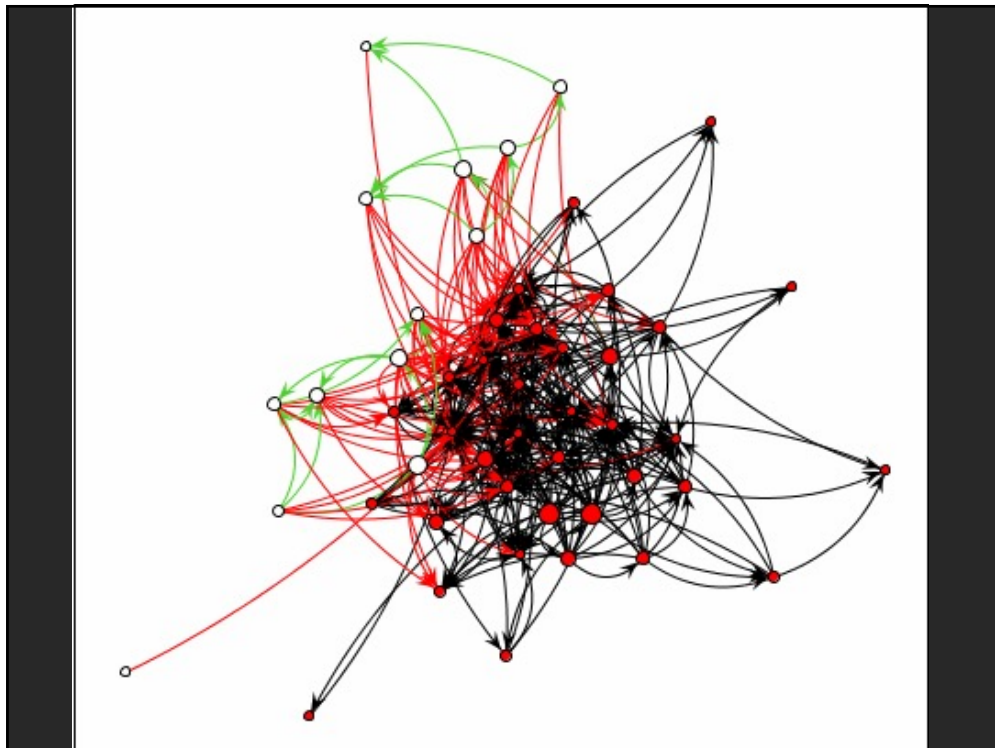
### Grading

- Groups of **up to 3 people**, graded individually
- Clearly report responsibilities of each member

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# Network Layout

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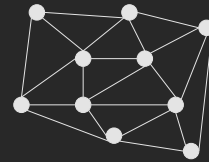
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# Graphs and Trees

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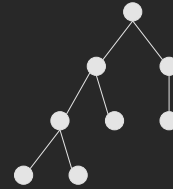
## Graphs

Model relations among data  
*Nodes and edges*



## Trees

Graphs with hierarchical structure  
Connected graph with  $N-1$  edges  
*Nodes as parents and children*



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# Tree Layout

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# Tree Visualization

## Indentation

- Linear list, indentation encodes depth



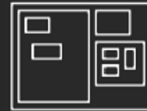
## Node-Link diagrams

- Nodes connected by lines/curves



## Enclosure diagrams

- Represent hierarchy by enclosure



## Layering

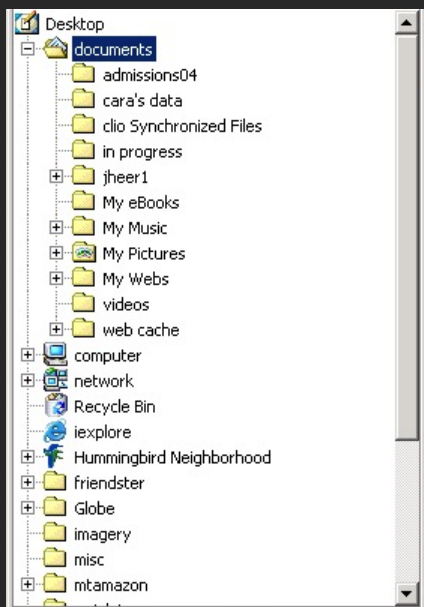
- Layering and alignment



**Tree layout is fast:  $O(n)$  or  $O(n \log n)$ , enabling real-time layout for interaction**

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# Indentation



Items along vertically spaced rows

Indentation shows parent/child relationships

Often used in interfaces

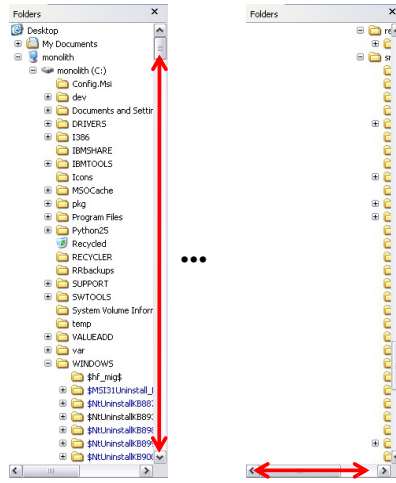
Breadth/depth contend for space

Often requires scrolling



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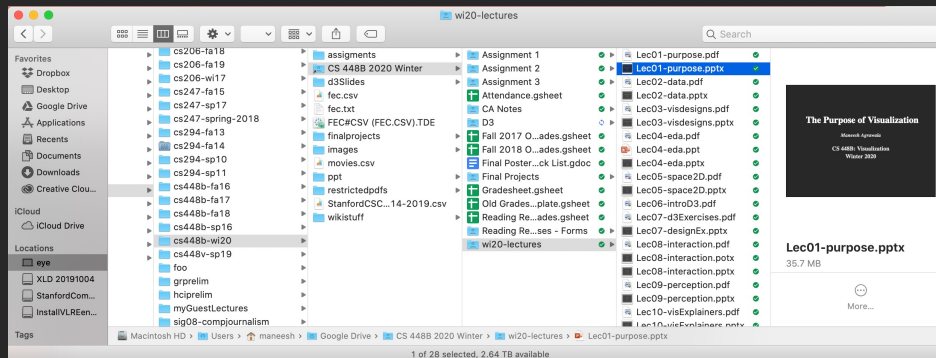
# Visualizing Large Hierarchies



Indented Layout

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# Single-Focus (Accordion) List



Separate breadth & depth in 2D  
Focus on single path at a time

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## Node-Link Diagrams

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Nodes distributed in space, connected by lines

Use 2D space to break apart breadth and depth

Space used to communicate hierarchical orientation

Typically towards authority or generality



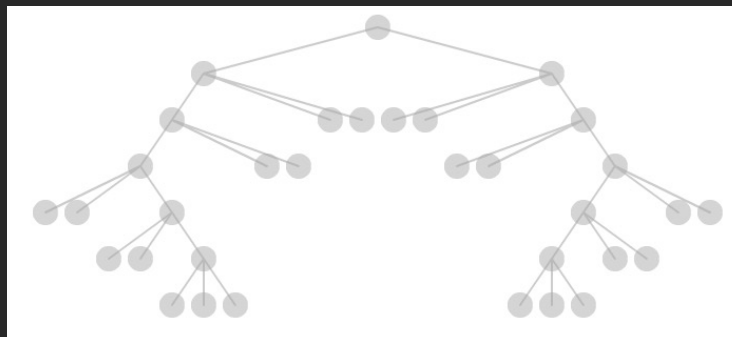
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## Basic Recursive Approach

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**Repeatedly divide space for subtrees by leaf count**

- Breadth of tree along one dimension
- Depth along the other dimension

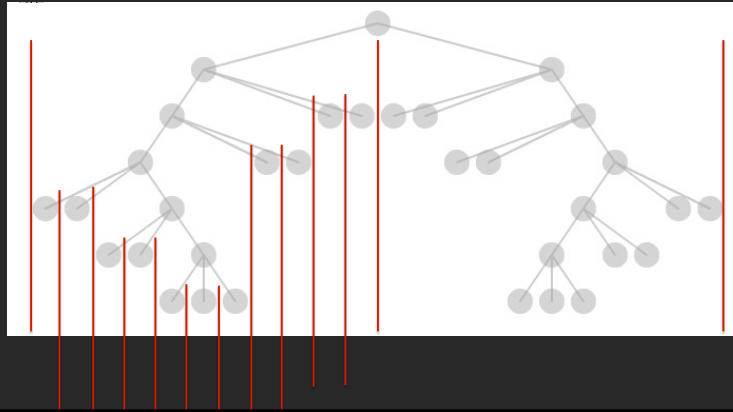


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# Basic Recursive Approach

Repeatedly divide space for subtrees by leaf count

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- Depth along the other dimension



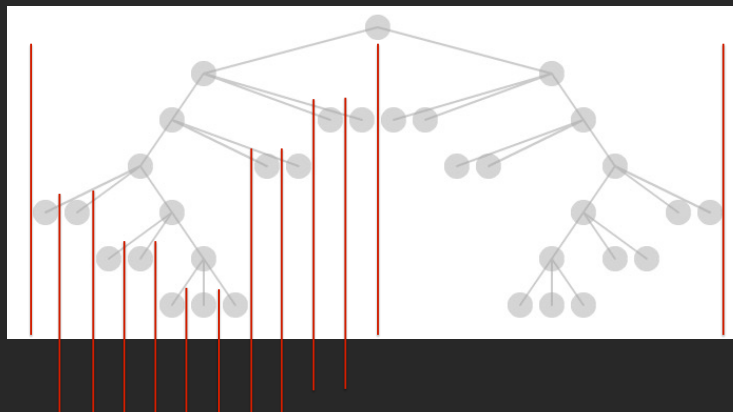
82

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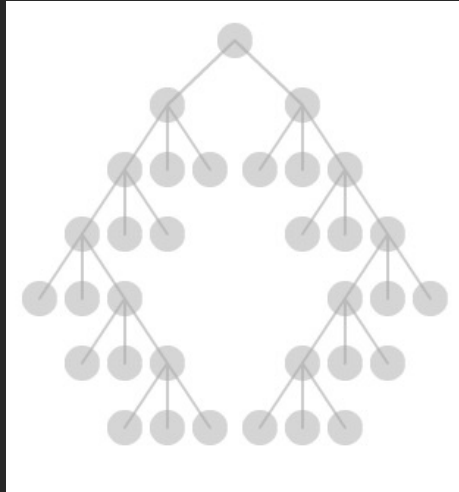
Problem: Exponential growth of breadth



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## Reingold & Tilford's Tidier Layout

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**Goal:** maximize density and symmetry.

Originally for binary trees, extended by Walker to cover general case.

This extension was corrected by Buchheim et al. to achieve a linear time algorithm

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## Reingold-Tilford Layout

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### Design concerns

Clearly encode depth level

No edge crossings

Isomorphic subtrees drawn identically

Ordering and symmetry preserved

*Compact layout (don't waste space)*

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# Reingold-Tilford Algorithm

## Initial bottom-up (postorder) tree traversal

- Set y-coordinate based on depth
- Initialize x-coordinate to zero

## At each parent node, merge left and right subtrees

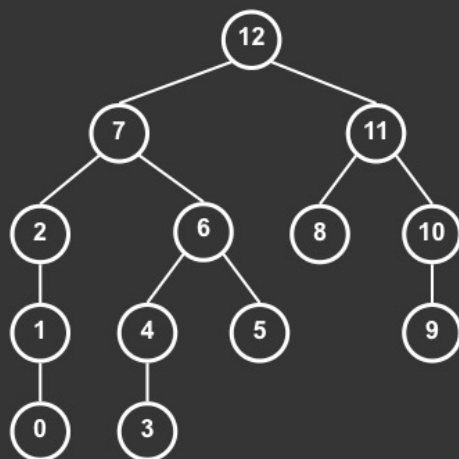
- Shift right subtree as close as possible to left
  - Computed efficiently by maintaining subtree contours
- Center parent nodes above children
- Record "Shift" in position offset for right subtree

## Final top-down (preorder) traversal to set x-coordinates

- Sum aggregated shift

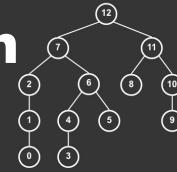
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# Reingold-Tilford Algorithm



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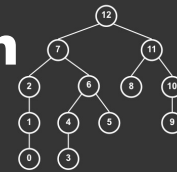
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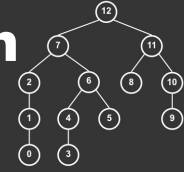
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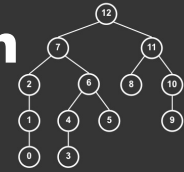
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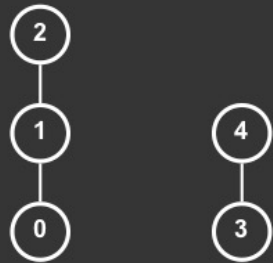
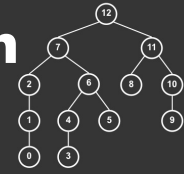
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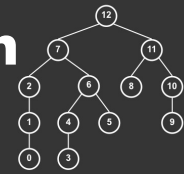
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## Final top-down (preorder) traversal to set x-coords

- Sum aggregated shift

92

# Reingold-Tilford Algorithm



## Initial bottom-up (postorder) tree traversal

- Set y-coordinate based on depth
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## At each parent node, merge left and right subtrees

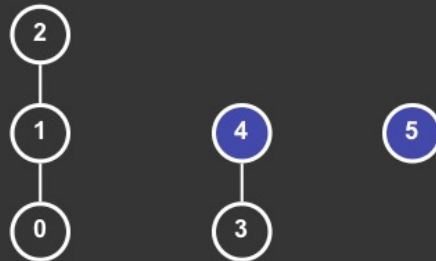
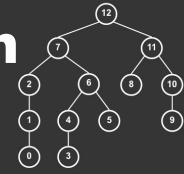
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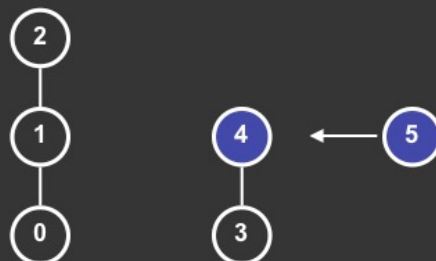
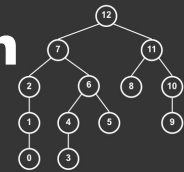
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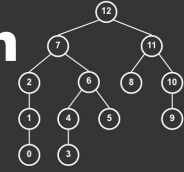
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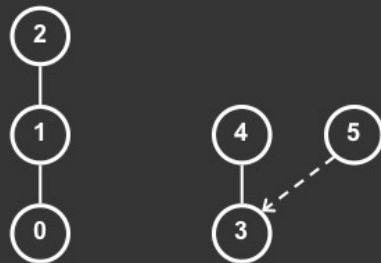
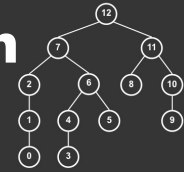
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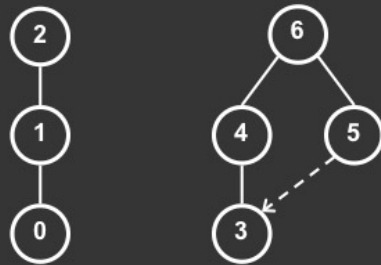
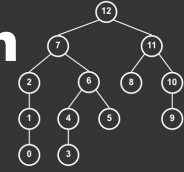
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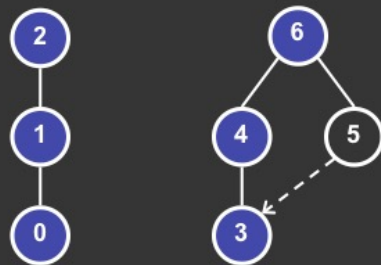
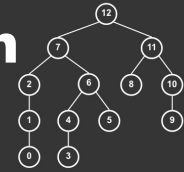
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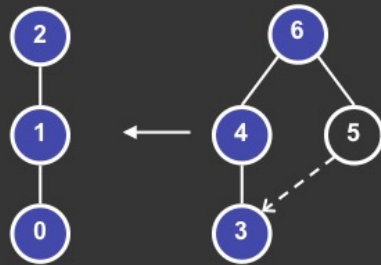
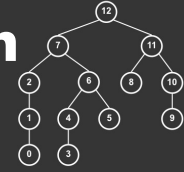
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99

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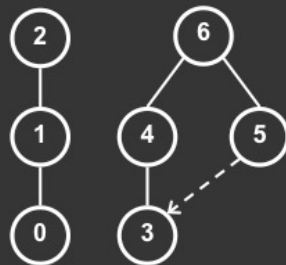
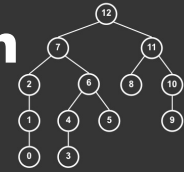
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100

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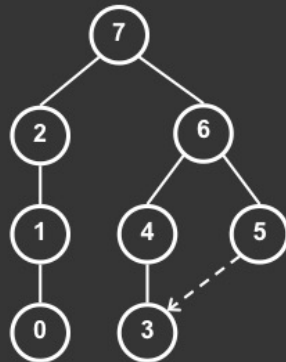
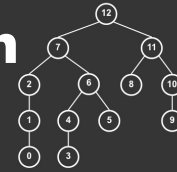
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101

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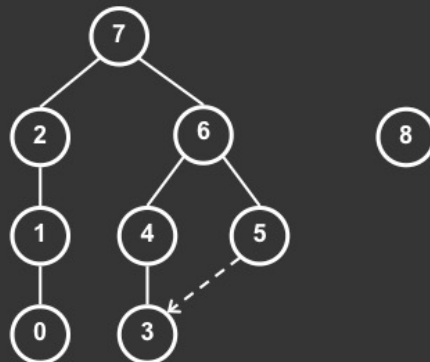
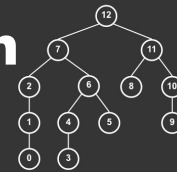
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102

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- Set y-coordinate based on depth
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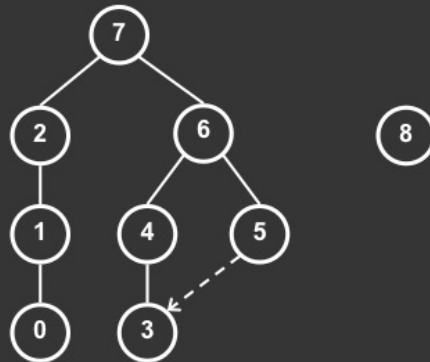
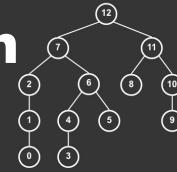
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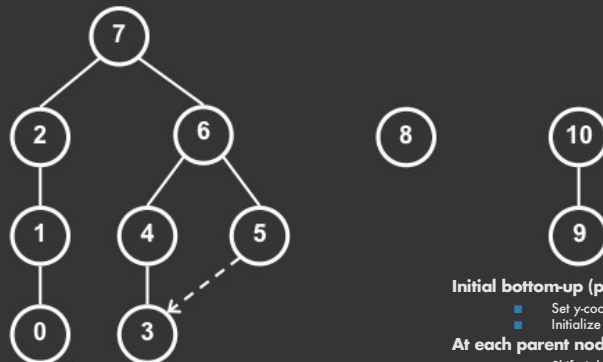
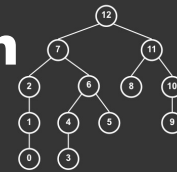
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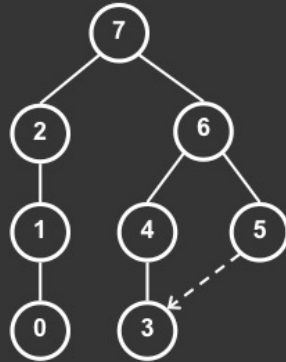
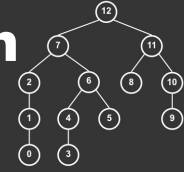
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105

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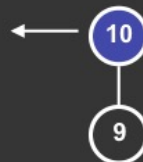
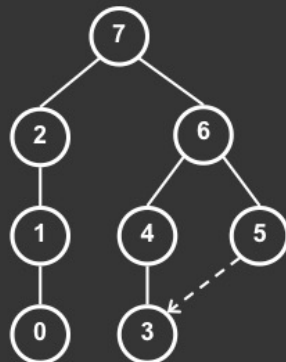
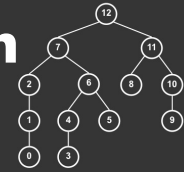
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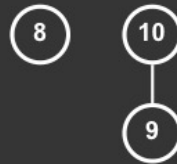
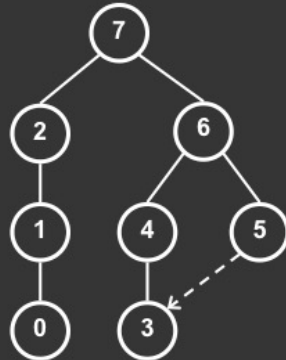
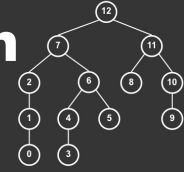
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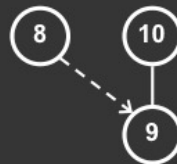
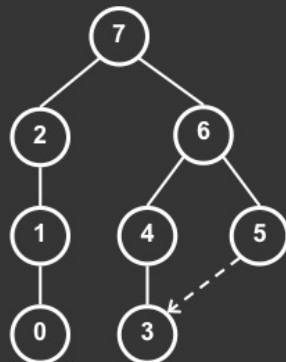
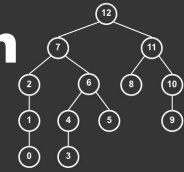
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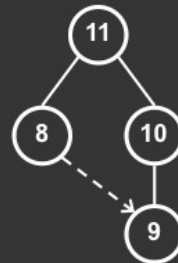
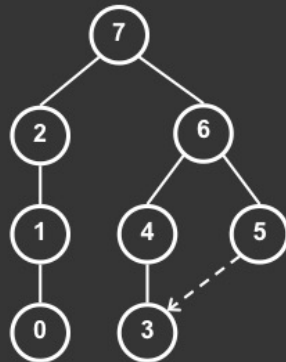
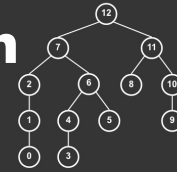
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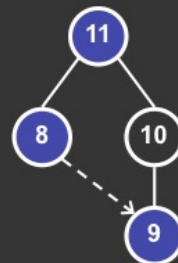
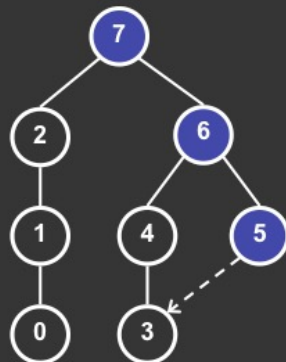
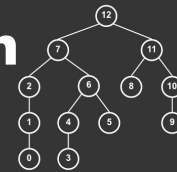
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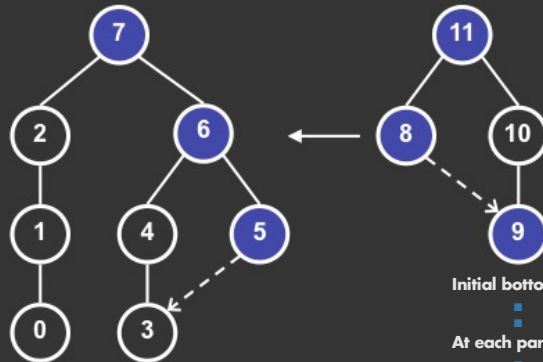
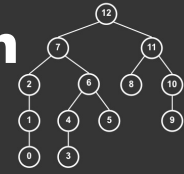
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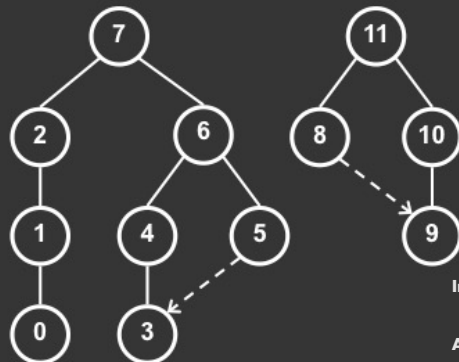
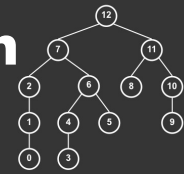
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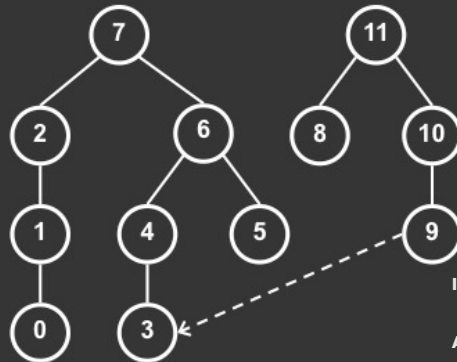
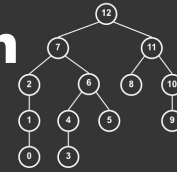
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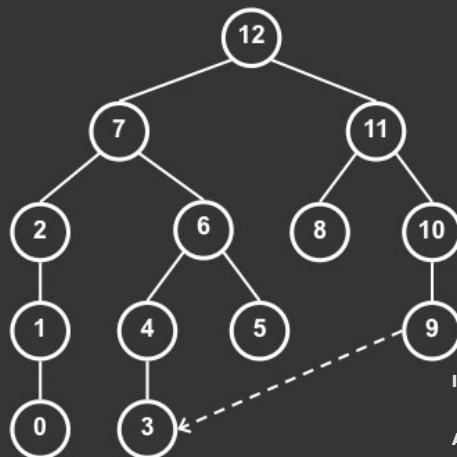
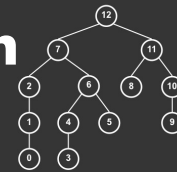
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114

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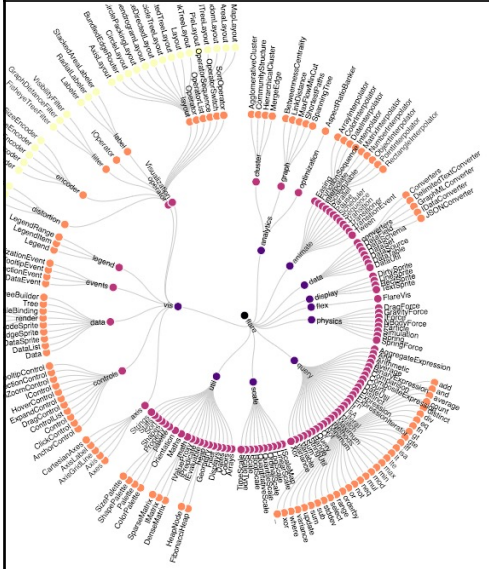
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# Radial Layout



Node-link diagram in polar coords

Radius encodes depth root at center

Angular sectors assigned to subtrees  
(recursive approach)

Reingold-Tilford approach can also be  
applied here

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# Problems with Node-Link Diagrams

## Scale

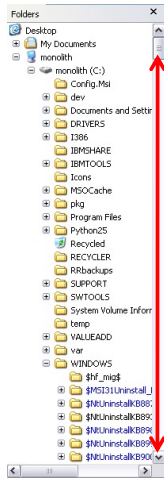
Tree breadth often grows exponentially  
Even with tidier layout, quickly run out of space

## Possible solutions

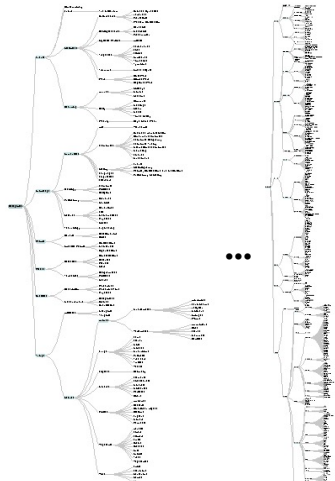
- Filtering
- Focus+Context
- Scrolling or Panning
- Zooming
- Aggregation

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# Visualizing Large Hierarchies



Indented Layout



Reingold-Tilford Layout

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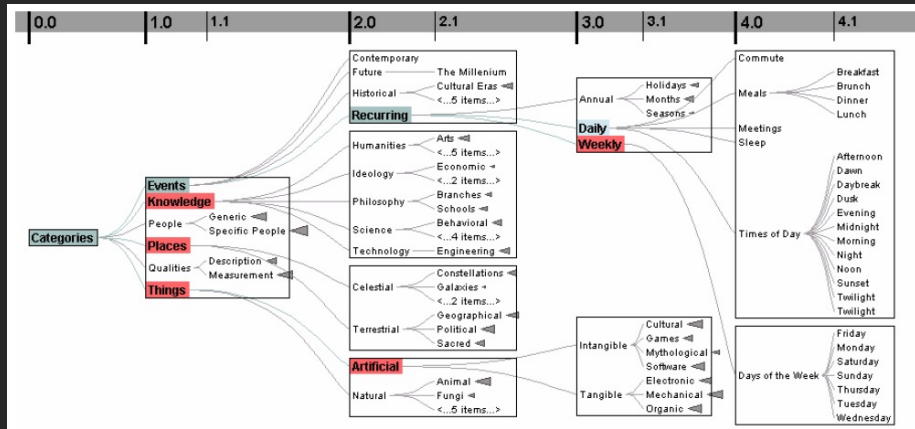


MC Escher, Circle Limit IV

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# Degree-of-Interest Trees



Cull “un-interesting” nodes on a per block basis until all blocks on a level fit within bounds

Center child blocks under parents

<https://www.youtube.com/watch?v=RTQ0N4QY0yc>

<https://observablehq.com/@d3/collapsible-tree>

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# Enclosure Diagrams

Encode structure using spatial enclosure  
Popularly known as TreeMaps



## Benefits

- Provides a single view of an entire tree
- Easier to spot large/small nodes

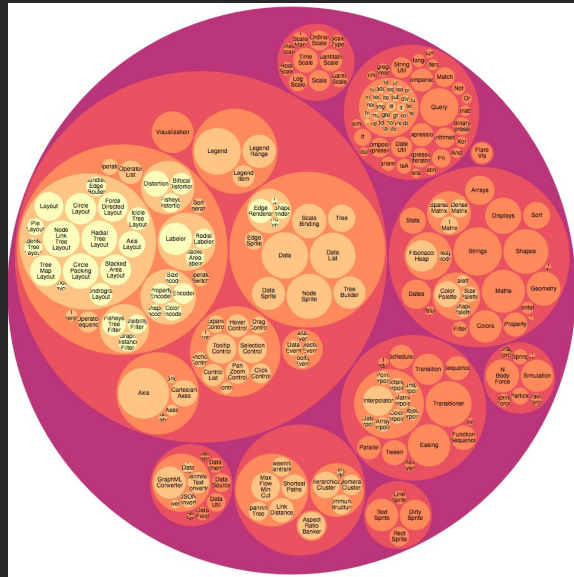
## Problems

- Difficult to accurately read depth

127



# Circle Packing Layout



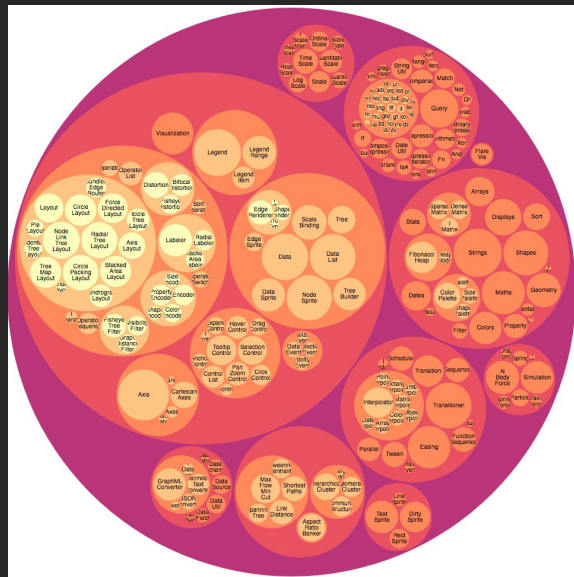
Nodes represented as sized circles

Nesting to show parent-child relationships

**Problems:**

128

# Circle Packing Layout



Nodes represented as sized circles

Nesting to show parent-child relationships

**Problems:**

Inefficient use of space

Parent size misleading

129

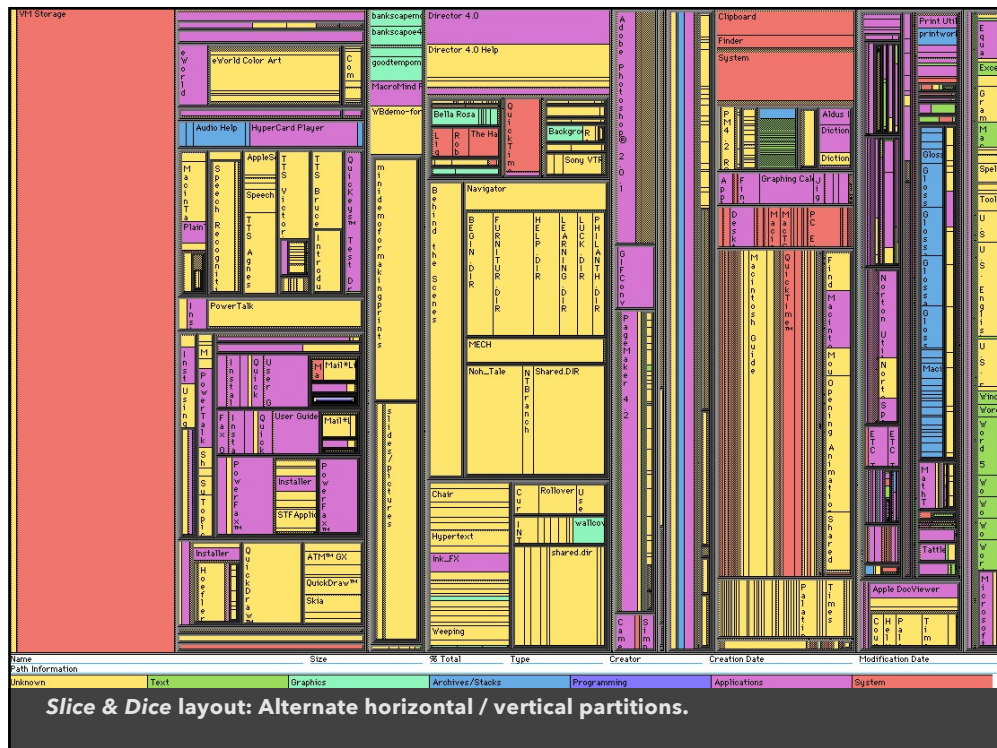
# Treemaps

Hierarchy visualization that emphasizes values of nodes via area encoding

Partition 2D space such that leaf nodes have sizes proportional to data values

First layout algorithms proposed by [Shneiderman et al. in 1990](#), with focus on showing file sizes on a hard drive

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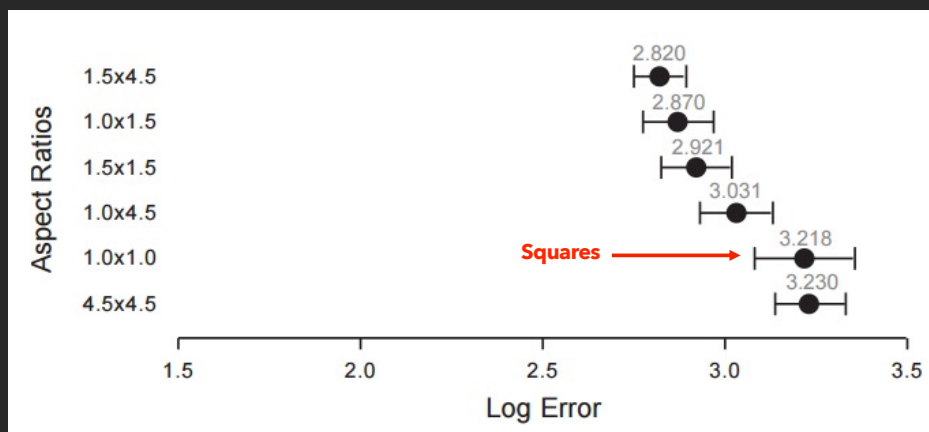
# Why Squares

## Posited Benefits of 1:1 Aspect Ratios

1. Minimize perimeter, reducing border ink.
2. Easier to select with a mouse cursor.  
*Validated by empirical research & Fitt's Law!*
3. Similar aspect ratios are easier to compare.  
*Seems intuitive, but is this true?*

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# Error vs. Aspect Ratio [Kong 10]



1. Comparison of squares has higher error!
2. Squarify works because it fails to meet its objective?

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# Why Squares

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*Seems intuitive, but is this true?*  
*Extreme ratios & squares-only more inaccurate.*  
*Balanced ratios better? Target golden ratio?*