## Using Space Effectively: 2D

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## Announcements

## Assignment 3: Dynamic Queries

Create a small interactive dynamic query application similar to Homefinder, but for SF Restaurant Data.

1. Implement interface and produce final writeup
2. Submit the application and a final writeup on canvas


Can work alone or in pairs Due before class on Oct 29, 2018

## Final project

New visualization research or data analysis

- Pose problem, Implement creative solution
- Design studies/evaluations

Deliverables

- Implementation of solution
- 6-8 page paper in format of conference paper submission
- Project progress presentations


## Schedule

- Project proposal: Mon 11/5
- Project progress presentation: $11 / 12$ and $11 / 14$ in class ( $3-4 \mathrm{~min}$ )
- Final poster presentation: 12/5 Location: Lathrop 282
- Final paper: 12/9 11:59pm


## Grading

- Groups of up to 3 people, graded individually
- Clearly report responsibilities of each member


## Using Space Effectively: 2D

## Topics

Displaying data in graphs
Selecting aspect ratio
Fitting data and depicting residuals
Graphical calculations
Focus + Context
Cartographic distortion

## Graphs and Lines

## Effective use of space

Which graph is better?


Government payrolls in 1937 [Huff 93]

## Aspect ratio

Fill space with data
Don' $\ddagger$ worry about showing zero



Yearly CO2 concentrations [Cleveland 85]

## Clearly mark scale breaks




## Scale break vs. Log scale


[Cleveland 85]

## Scale break vs. Log scale


[Cleveland 85]
Both increase visual resolution

- Log scale - easy comparisons of all data
- Scale break - more difficult to compare across break


## Linear scale vs. Log scale



## Linear scale vs. Log scale

Linear scale

- Absolute change


Log scale

- Small fluctuations
- Percent change
$d(10,20)=d(30,60)$



## Semilog graph: Exponential growth

Exponential functions ( $\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}$ ) transform into lines $\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{mx}$ Intercepł: $\log (k)$
Slope: $\log (a) m$


$y=6^{0.5 x}$, slope in semilog space: $\log (6)^{*} 0.5=0.3891$

## Semilog graph: Exponential decay

Exponential functions ( $\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}$ ) transform into lines
$\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{mx}$
Intercept: $\log (k)$
Slope: $\log (a) m$

$y=0.5^{2 x}$, slope in semilog space: $\log (0.5)^{*} 2=-0.602$

## Log-Log graph

Power functions ( $\mathrm{y}=\mathrm{kx} \mathrm{a}^{\mathrm{a}}$ ) transform into lines Example - Steven's power laws:

$$
S=k I^{p} \Rightarrow \log S=\log k+p \log I
$$




## Selecting Aspect Ratio

## Aspect ratio

Fill space with data
Don' $\ddagger$ worry about showing zero



Yearly CO2 concentrations [Cleveland 85]


## Banking to $\mathbf{4 5}^{\circ}$ [Cleveland]

To facilitate perception of trends, maximize the discriminability of line segment orientations


Two line segments are maximally discriminable when avg. absolute angle between them is $45^{\circ}$
Optimize the aspect rattio to bank to $45^{\circ}$

## Aspect-ratio banking techniques

| Medion-Absolute-Slope | Average-Absolute-Slope |
| :---: | :---: |
| $\alpha=\operatorname{median}\left\|S_{i}\right\| R_{x} / R_{y}$ | $\begin{aligned} & \qquad \alpha=\text { mean }\left\|s_{i}\right\| R_{x} / R_{y} \\ & \text { Has Closed Form Solution } \end{aligned}$ |
| Average-Absolute-Orientation | Max-Orientation-Resolution |
| Unweighted |  |
| $\sum \frac{\left\|\theta_{i}(\alpha)\right\|}{n}=45^{\circ}$ | $\sum \sum\left\|\theta_{i}(\alpha)-\theta_{j}(\alpha)\right\|^{2}$ |
| Weighted ${ }^{i} \quad n$ | Locail ( ${ }^{i}$ (over adjacent segments) |

$$
\frac{\sum_{i}\left|\theta_{i}(\alpha)\right| l_{i}(\alpha)}{\sum_{i} l_{i}(\alpha)}=45^{\circ}
$$

$$
\sum_{i}\left|\theta_{i}(\alpha)-\theta_{i+1}(\alpha)\right|^{2}
$$

Requires Iterative
Optimization

## Perceptual model based aspect ratio



Ask people to estimate slope ratios for different conditions Use data to fit a model derived from perceptual theory
$\hat{p}_{i j}=\left\{\begin{array}{llll}\frac{\sin \left(\theta_{i}\right) l_{i}}{\sin \left(\theta_{j}\right) l_{j}} \times 100 & +\gamma & +\varepsilon_{i j}^{h} & \text { if HEIGHT } \\ \frac{\theta_{i}}{\theta_{j}} \times 100 & +\left(\mu+\beta \theta_{m}\right) & +\varepsilon_{i j}^{a} & \text { if ANGLE }\end{array}\right.$


## Multi-Scale Banking to $45^{\circ}$

Idea: Use Spectral Andysis to identify trends
Find strong frequency components
Lowpass filter to create trend lines


## Fitting the Data


[The Elements of Graphing Data. Cleveland 94]




[The Elements of Graphing Data. Cleveland 94]

## Transforming data

How well does curve fit data?

[Cleveland 85]

## Transforming data

## Residual graph

- Plot vertical distance from best fit curve
- Residual graph shows accuracy of fit

[Cleveland 85]


## Most powerful brain?






## Most powerful brain



Beautiful Evidence [Tufte]

## Graphical Calculations

## Nomograms



Sailing: The Rule of Three

## Nomograms



1. Compute in any direction; fix $\mathbf{n}^{\mathbf{- 1}}$ params and read nth aram
2. Illustrate sensitivity to perturbation of inputs
3. Clearly show domain of validity of computation

## Theory

$\left|\begin{array}{ccc}x_{1}(u) & y_{1}(u) & w_{1}(u) \\ x_{2}(v) & y_{2}(v) & w_{2}(v) \\ x_{3}(s, t) & y_{3}(s, t) & w_{3}(s, t)\end{array}\right|=0$
http://www.projectrho.com/nomogram/

## Slide rule



Model 1474-66 Electrotechnica 18 Scales

Tehnolemn Timisoara Slide Rule Archive
http://pubpages.unh.edu/~jwc/tehnolemn/



## Lambert's graphical construction



Johannes Lambert used graphs to study the rate of water evaporation as
function of temperature [from Tufte 83]



## Degree-of-Interest [Furnas 81, 06]

Estimate the saliency of information to display Can affect what is shown and/or how to show it

DOI ~ f(Current Focus, A Priori Importance)
Example: Google Search
Current Focus = Query Hits (e.g., TF.IDF score)
A Priori Importance = PageRank
Whats Top N results, How: List

## TableLens <br> [Rao \& Card 94]


http://www.youtube.com/watch?v=qWaTrRAC52U

## Datelens


[Bederson et al. 04]

## Single view detail + context

- Focus area - local details
- De-magnified area - surrounding context
- Like a rubber sheeł with borders tacked down


Nonlinear Magnification Infocenter [http://www.cs.indiana.edu/\~łkeahey/research/nIm/nlm.html]

## 6 types of distortions Cappasados <br> Montagnese 011



Gaussian, Cosine, Hemisphere, Linear, Inverse Cosine and Manhattan. Top row shows transition from focus to distortion, bottom row from distortion to context.

## Perspective allows more context



Perspective Wall [Mackinlay et al. 91]

## Distortions

## 



## Cartograms: Distort areas



Attendance per State, 1970-1977

## Election 2016 map


htip://www-personal.umich.edu/~ mejn/election/

## Election 2016 map


http://www-personal.umich.edu/~ mejn/election/

## Election 2016 map


http://www-personal.umich.edu/ ${ }^{\text {mejn/election/ }}$

## NYT Election 2016 (based on 2012)



## Statistical map with shading


rates per 100,000 population

## Framed rectangle chart



## Rectangular cartogram



American population [van Kreveld and Speckmann 04]

## Rectangular cartogram



Native American population [van Kreveld and Speckmann 04]

## New York Times Election 2004



## New York Times Election 2016

## 2016 Electoral Map Forecast

The Upshot's forecast for the presidential race, based on the latest national and state polls.
By JOSH KAIZ and ADAM PEARCE UPDATED November 2. 2016

70 to win


## Dorling cartogram



