## Perception

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CS 448B: Visualization
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## Lasł Time: Exploratory Data Analysis

## Will Burtin, 1951



| Bacteria | Penicillin | Antibiotic Streptomycin | Neomycin | Gram stain |
| :---: | :---: | :---: | :---: | :---: |
| Aerobacter aerogenes | 870 | 1 | 1.6 | - |
| Brucella abortus | 1 | 2 | 0.02 | - |
| Bacillus anthracis | 0.001 | 0.01 | 0.007 | + |
| Diplococcus pneumoniae | 0.005 | 11 | 10 | + |
| Escherichia coli | 100 | 0.4 | 0.1 | - |
| Klebsiella pneumoniae | 850 | 1.2 | 1 | - |
| Mycobacterium tuberculosis | 800 | 5 | 2 | - |
| Proteus vulgaris | 3 | 0.1 | 0.1 | - |
| Pseudomonas aeruginosa | 850 | 2 | 0.4 | - |
| Salmonella (Eberthella) typhosa | 1 | 0.4 | 0.008 | - |
| Salmonella schottmuelleri | 10 | 0.8 | 0.09 | - |
| Staphylococcus albus | 0.007 | 0.1 | 0.001 | + |
| Staphylococcus aureus | 0.03 | 0.03 | 0.001 | + |
| Streptococcus fecalis | 1 | 1 | 0.1 | + |
| Streptococcus hemolyticus | 0.001 | 14 | 10 | + |
| Streptococcus viridans | 0.005 | 10 | 40 | + |

How do the drugs compare?


## Lessons

## Explorafory Process

1 Construct graphics to address questions
2 Inspect "answer" and assess new questions
3 Repeat!
Transform the data appropriately (e.g॰, invert, log)
"Show data variation, noł design variation"
-Tufte

## Formulating a Hypothesis

Null Hypothesis $\left(\mathrm{H}_{0}\right): \quad \quad \mu_{\mathrm{m}}=\mu_{\mathrm{f}}$ (population)
Alternate Hypothesis $\left(\mathbf{H}_{\mathrm{a}}\right): \quad \mu_{\mathrm{m}} \neq \mu_{\mathrm{f}}$ (population)
A statistical hypothesis test assesses the likelihood of the null hypothesis.

What is the probability of sampling the observed data assuming population means are equal?
This is called the $p$ value


Choropleth maps of cancer deaths in Texas.
One plot shows a real data sets. The others are simulated under the null hypothesis of spatial independence.

Can you spot the real data? If so, you have some evidence of spatial dependence in the data.

## Tableau



## Polaris/Tableau Approach

Insight: simultaneously specify both database queries and visualization

Choose data, then visualization, not vice versa
Use smart defaults for visual encodings

Recently: aułomate visualization design (ShowMe - Like APT)

## Specifying Table Configurations

Operands are names of database fields Each operand interpreted as a set \{...\} Dała is either Ordinal or Quantitative

## Three operators:

```
concatenation (+)
cross product (x)
nest (/)
```


## Table Algebra: Operands

Ordinal fields: interpret domain as a set that partitions table into rows and columns
Quarter $=\left\{(\text { Qtr } 1)_{r}(\text { Qłr2 })_{r}(\text { Qtr3 })_{r}(\right.$ Qtr 4$\left.)\right\} \rightarrow$

| Qtr1 | Qtr2 | Qtr3 | Qtr4 |
| :---: | :---: | :---: | :---: |
| 95892 | 101760 | 105282 | 98225 |

Quantitative fields: treat domain as single element set and encode spatially as axes
Profit $=\{($ Profit[-4 10,650] $)\} \rightarrow$


## Concatenation (+) Operator

Ordered union of set interpretations
Quarter + Product Type
$=\{($ Qtr 1$),($ Qtr2 $),($ Qtr3 $),($ Qtr 4$)\}+\{(C o f f e e), ~(E s p r e s s o)\} ~$
= \{(Qtr 1),(Qtr2),(Qtr3),(Qtr4),(Coffee),(Espresso)\}

| Qtr1 | Qtr2 | Qtr3 | Qtr4 | Coffee | Espresso |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 48 | 59 | 57 | 53 | 151 | 21 |

Profit + Sales $=\{(\operatorname{Profit}[-310,620]),($ Sales[0, 1000] $)\}$


## Cross (x) Operator

Cross-product of set interpretations
Quarter x Product Type
= \{(Qtr1,Coffee), (Qtr 1, Tea), (Qtr2, Coffee), (Qtr2, Tea), (Qtr3, Coffee), (Qtr3, Tea), (Qtr4, Coffee), (Qtr4,Tea) \}

| Qtr 1 |  | Qtr2 |  | Qtr3 |  | Qtr 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coffee | Espresso | Coffee | Espresso | Coffee | Espresso | Coffee | Espresso |
| 131 | 19 | 160 | 20 | 178 | 12 | 134 | 33 |

Product Type x Profit =

| Coffee |  |  |  |  | Espresso |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | © - |  |  | - | - | - |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| 0 | 100 | 200 | 300 | 400 | 0 | 100 | 200 | 300 | 400 |
| Profit |  |  |  |  | Profit |  |  |  |  |

## Nest (/) Operator

Cross-product filtered by existing records
Quarter x Month
creates twelve entries for each quarter. i.e., (Ctr 1, December)

Quarter / Month creates three entries per quarter based on tuples in database (not semantics)

## Polaris/Tableau Table Algebra

The operators ( + , $\mathbf{x}, /$ ) and operands $(\mathbf{O}, \mathbf{Q})$ provide an algebra for tabular visualization.

Algebraic statements are then mapped to:
Queries - selection, projection, group-by aggregation
Visualizations - trellis plot partitions, visual encodings
In Tableau, users make statements via drag-and-drop Note that this specifies operands NOT operators! Operators are inferred by data type ( $\mathbf{O}, \mathbf{Q}$ )

## Ordinal - Ordinal

| Grate | Coffee | Produ Espresso | ct Type <br> Herbal Tea | Tea |
| :---: | :---: | :---: | :---: | :---: |
| Colorado | - | - | - | - |
| Connecticut | - | - | - | - |
| Florida | - | - | - | - |
| Illinois | - | , | - | - |
| Iowa | - | - | - | + |
| Louisiana | - | - | - |  |
| Massachusetts | - | - | - | - |
| Missouri | - | $\bullet$ | - | $\bullet$ |
| Nevada | - | - |  | - |
| New Hampshire | - | - | - | - |
| New Mexico | $\bullet$ | $\bullet$ | - |  |
| New York | - | - | - | - |
| Ohio | - | - | - | - |
| Oklahoma | - | - | - |  |
| Oregon | - | - | - | - |
| Texas | - | - | $\bullet$ |  |
| Utah | - | - | - | - |
| Washington | - | - | - | - |
| Wisconsin | $\bigcirc$ | - | $\bullet$ | $\bullet$ |

## Quantitative - Quantitative



## Ordinal - Quantitative



## Summary

Explorałory analysis may combine graphical methods, and statistics

Use questions to uncover more questions

Formal methods may be used to confirm

Interaction is essential for exploring large multidimensional dafasets

## Announcements

## A2: Exploratory Data Analysis

Use Tableau to formulate $\&$ answer questions
First steps

- Step 1: Pick a domain
- Step 2: Pose questions
- Step 3: Find data
- Iterate

Create visualizations

- Interact with data
- Question will evolve
- Tableau


Make wiki notebook

- Keep record of all steps you took to answer the questions

Due before class on Oct 15, 2018

## Perception

## Mackinlay's ranking of encodings

| QUANTITATIVE | ORDINAL | NOMINAL |
| :--- | :--- | :--- |
| Position | Position | Position |
| Length | Density (Val) | Color Hue |
| Angle | Color Sat | Texture |
| Slope | Color Hue | Connection |
| Area (Size) | Texture | Containment |
| Volume | Connection | Density (Val) |
| Density (Val) | Containment | Color Sat |
| Color Sat | Length | Shape |
| Color Hue | Angle | Length |
| Texture | Slope | Angle |
| Connection | Area (Size) | Slope |
| Containment | Volume | Area |
| Shape | Shape | Volume |

## Topics

Signal Detection
Magnitude Estimation
Pre-Attentive Visual Processing
Using Multiple Visual Encodings
Gestalt Grouping
Change Blindness

## Detection

## Detecting brightness



Which is brighter?

## Detecting brightness

$(128,128,128)$

(130, 130, 130)


Which is brighter?

## Just noticeable difference

JND (Weber's Law)

$$
\Delta S=k \frac{\Delta I}{I}
$$

- Ratios more important than magnitude
- Most continuous variations in stimuli are perceived in discrete steps



## Information in color and value

Value is perceived as ordered
$\therefore$ Encode ordinal variables (O)

$\therefore$ Encode continuous variables (Q) [not as well]


Hue is normally perceived as unordered
$\therefore$ Encode nominal variables ( $\mathbf{N}$ ) using color


## Steps in font size

Sizes standardized in $16^{\text {th }}$ century

$$
\begin{array}{llllllll}
a & a & a & \propto & a & \propto & \propto & \bullet
\end{array}
$$

$\bullet$

$$
67
$$

$$
\begin{array}{llllllllllll}
6 & 7 & 8 & 9 & 10 & 11 & 12 & 14 & 16 & 18 & 21 & 24
\end{array}
$$

## Estimating Magnitude



## Steven's power law

$$
S=I^{p}
$$

$p<1$ : underestimate p > 1 : overestimate

[graph from Wilkinson 99, based on Stevens 61]

## Exponents of power law

| Sensation | Exponent |
| :---: | :---: |
| Loudness | 0.6 |
| Brightness | 0.33 |
| Smell | 0.55 (Coffee) -0.6 (Heptane) |
| Taste | 0.6 (Saccharine) -1.3 (Salt) |
| Temperature | 1.0 (Cold) -1.6 (Warm) |
| Vibration | 0.6 (250 Hz) -0.95 ( 60 Hz ) |
| Duration | 1.1 |
| Pressure | 1.1 |
| Heaviness | 1.45 |
| Electic Shock | 3.5 |

## Apparent magnitude scaling


[Carłography: Thematic Map Design, Figure 8.6, p. 170, Dent, 96]

$$
S=0.98 A^{0.87} \text { [from Flannery 71] }
$$

## Proportional symbol map

Newspaper Circulation


## Graduated sphere map



FIGURE 7.4. An eye-catching map created using three-dimensional geometric symbols. (After Smith, 1928. First published in The Geographical Review, 18(3), plate 4. Reprinted with permission of the American Geographical Society.)

## Cleveland and McGill


[Cleveland and McGill 84]


Figure 3. Graphs from position-angle experiment.
[Cleveland and McGill 84]


## Relative magnitude estimation

| Most accurate | Position (common) scale <br> Position (non-aligned) scale |  |
| :--- | :--- | :--- |
|  | Slongth |  |
| Least accurate | Angle |  |
|  |  | Colume |
|  |  |  |

## Mackinlay's ranking of encodings

QUANTITATIVE
Position
Length
Angle
Slope
Area (Size)
Volume
Density (Val)
Color Sat
Color Hue
Texture
Connection
Containment
Shape

ORDINAL
Position
Density (Val)
Color Sat
Color Hue
Texture
Connection
Containment
Length
Angle
Slope
Area (Size)
Volume
Shape

NOMINAL
Position
Color Hue
Texture
Connection
Containment
Density (Val)
Color Sat
Shape
Length
Angle
Slope
Area
Volume

## Preattentive vs. Attentive

## How many 3's

> 1281768756138976546984506985604982826762 9809858458224509856458945098450980943585 9091030209905959595772564675050678904567 8845789809821677654876364908560912949686

## How many 3's

$$
\begin{aligned}
& 1281768756138976546984506985604982826762 \\
& 9809858458224509856458945098450980943585 \\
& 9091030209905959595772564675050678904567 \\
& 8845789809821677654876364908560912949686
\end{aligned}
$$

## Visual pop-out: Color


http://www.csc.ncsu.edu/faculty/healey/PP/index.html

## Visual pop-out: Shape


htip://www.csc.ncsu.edu/faculty/healey/PP/index.html

## Feałure conjunctions


http://www.csc.ncsu.edu/faculty/healey/PP/index.html

## Preattentive features



Addition

[Information Visualization. Figure 5. 5 Ware 04]

## More preattentive features

| Line (blob) orientation | Julesz \& Bergen [1983]; Wolfe et al. [1992] |
| :---: | :---: |
| Length | Triesman \& Gormican [1988] |
| Width | Julesz [1985] |
| Size | Triesman \& Gelade [1980] |
| Curvature | Triesman \& Gormican [1988] |
| Number | Julesz [1985]; Trick \& Pylyshyn [1994] |
| Terminators | Julesz \& Bergen [1983] |
| Intersection | Julesz \& Bergen [1983] |
| Closure | Enns [1986]; Triesman \& Souther [1985] |
| Colour (hue) | Nagy \& Sanchez [1990, 1992]; <br> D'Zmura [1991]; Kawai et al. [1995]; |
|  | Bauer et al. [1996] |
| Intensity | Beck et al. [1983]; |
|  | Triesman \& Gormican [1988] |
| Flicker | Julesz [1971] |
| Direction of motion | Nakayama \& Silverman [1986]; Driver \& McLeod [1992] |
| Binocular lustre | Wolfe \& Franzel [1988] |
| Stereoscopic depth | Nakayama \& Silverman [1986] |
| 3-D depth cues | Enns [1990] |
| Lighting direction | Enns [1990] |

## Feature-integration theory



Feature maps for orientation \& color [Green]

Treisman's feature integration model [Healey04]

## Multiple Attributes

## One-dimensional: Lightness

0

$\square$
$\square$ White

Black
Black


White


## One-dimensiond: Shape

$\square$
$\square$


Square<br>Circle<br>Circle<br>Square<br>Circle



Circle
Circle

Square

Circle

Circle

## Correlated dims: Shape or lightness



|  | Circle |
| :--- | :--- |
|  | Square |
|  | Square |
|  | Circle |
|  | Square |


|  | Circle |
| :--- | :--- |
|  | Square |
|  | Square |
|  | Square |
|  | Circle |

## Orthogonal dims: Shape \& lightness

## -|ण

| - | Circle |
| :--- | :--- |
|  | Square |
|  | Square |
|  | Circle |
|  | Square |

## Speeded classification

Redundancy gain
Facilitation in reading one dimension when the other provides redundant information

Filtering interference
Difficulty in ignoring one dimension while attending to the other

## Speeded classification



## Types of dimensions

## Integral

Filtering interference and redundancy gain

## Separable

No interference or gain

## Configural

Only interference, but no redundancy gain

## Asymmetrical

One dimension separable from other, not vice versa
Stroop effect - Color naming influenced by word identity, but word naming not influenced by color

## Correlałed dims: Size and value



VALUE IN MILLIONS OF DOLLARS



VALUE IN MILLIONS OF DOLLARS

W. S. Dobson, Visual information processing and cartographic communication: The role of redundant stimulus dimensions, 1983 (reprinted in MacEachren, 1995)

## Othogonal dims: Aspect ratio



FIGURE 3.38. An example of the use of an ellipse as a map symbol in which the horizontal and vertical axes represent different (but presumably related) variables.

## Orientation and Size (Single Mark)



FIGURE 3.36. A map of temperature and precipitation using symbol size and orientation to represent data values on the two variables.

How well can you see temperature or precipitation? Is there a correlation between the two?

## Shape and Size



FIGURE 3.40. The bivariate temperature-precipitation map of Figure 3.36, this time using point symbols that vary in shape and size to represent the two quantities.

Easier to see one shape across multiple sizes than one size of across multiple shapes?

## Summary of Integral-Separable



[Figure 5.25, Color Plate 10, Ware 00]

